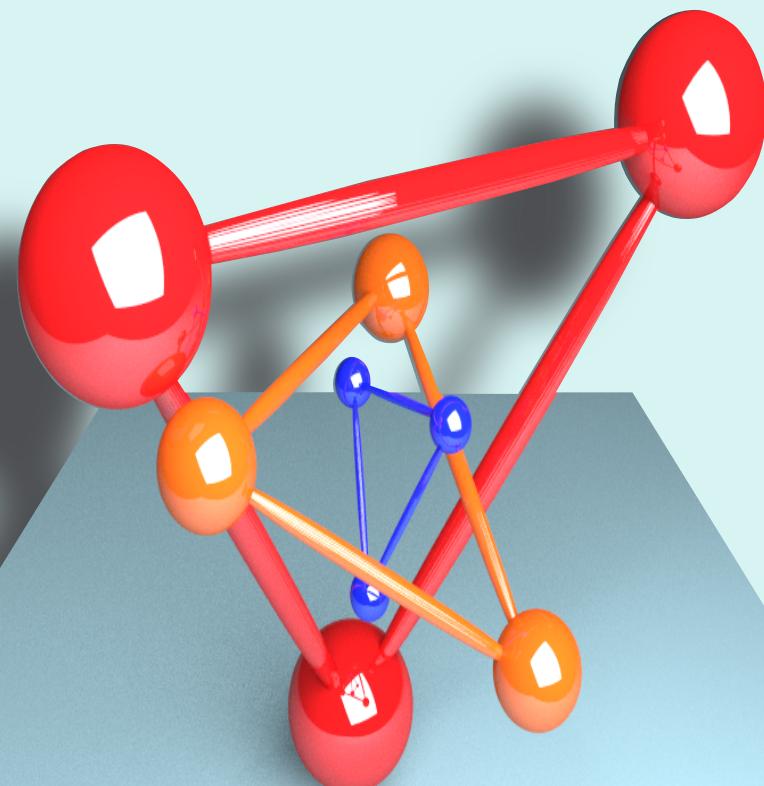


Efimov physics in strongly mass-imbalanced ultracold gases



P. Giannakeas

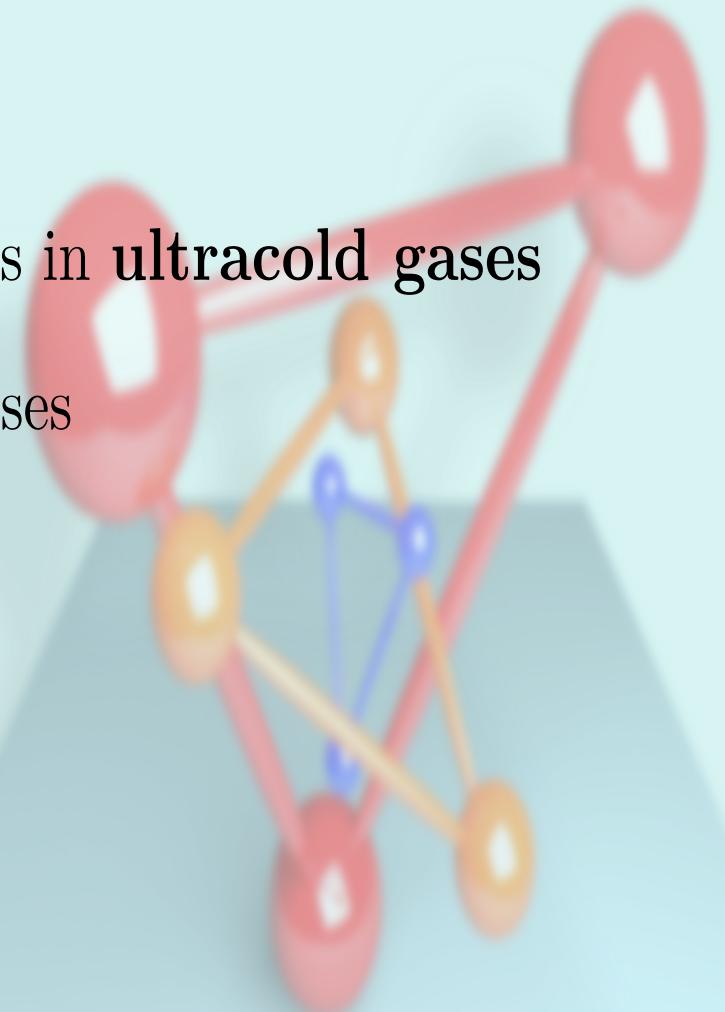
Max Planck Institute for the Physics
of Complex Systems

CLUSHIQ 2020



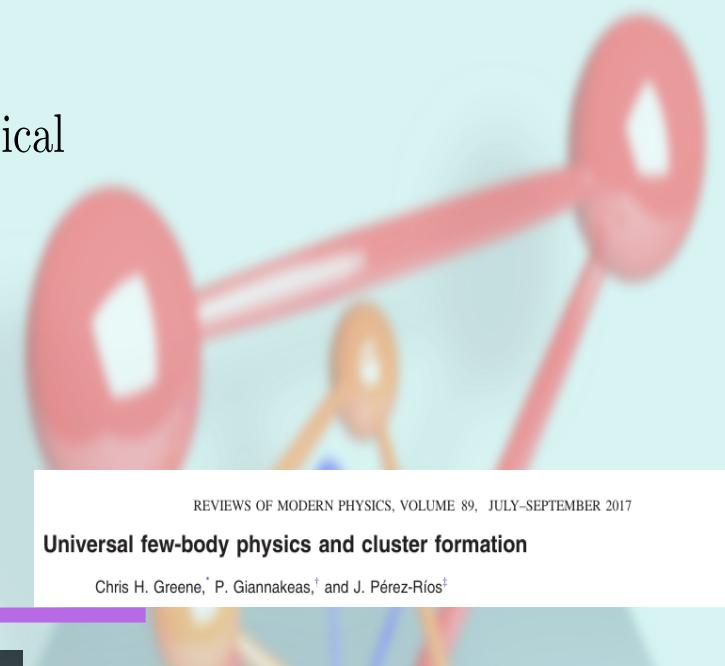
Outline

- Introduction & quick overview of Efimov physics in **ultracold gases**
- Efimov physics in mass imbalanced ultracold gases
- Three-body recombination processes
- Atom-dimer elastic and relaxation processes



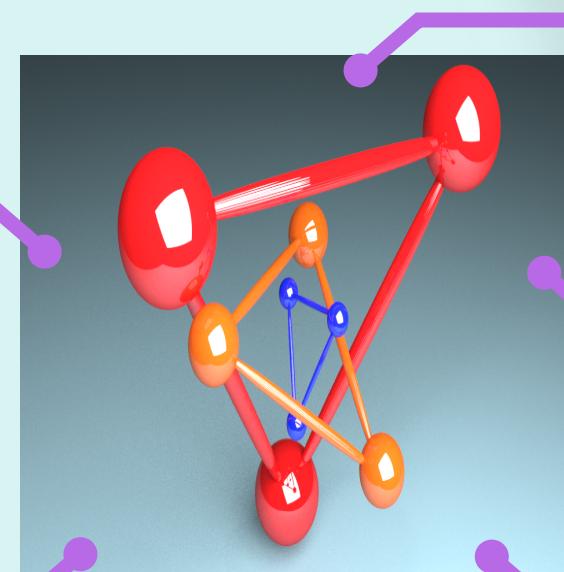
Introduction

- Efimov states: An infinite progression of trimer states even when all two-body subsystems are barely bound.
- Last two decades there is a tremendous experimental and theoretical progress exploring for example
 - the discrete scaling invariance between successive Efimov states
 - universal aspects of the ground Efimovian state



IOP Publishing
Rep. Prog. Phys. **80** (2017) 056001 (78pp)
<https://doi.org/10.1088/1361-6633/aa50e8>

Review
Efimov physics: a review
Pascal Naidon¹ and Shimpei Endo²



REVIEWS OF MODERN PHYSICS, VOLUME 89, JULY–SEPTEMBER 2017
Universal few-body physics and cluster formation
Chris H. Greene,[†] P. Giannakeas,[‡] and J. Pérez-Ríos[§]

ELSEVIER
PHYSICS REPORTS
Physics Reports 347 (2001) 373–459
www.elsevier.com/locate/physrep

The three-body problem with short-range interactions
E. Nielsen^{a,b}, D.V. Fedorov^c, A.S. Jensen^c, E. Garrido^{d,*}

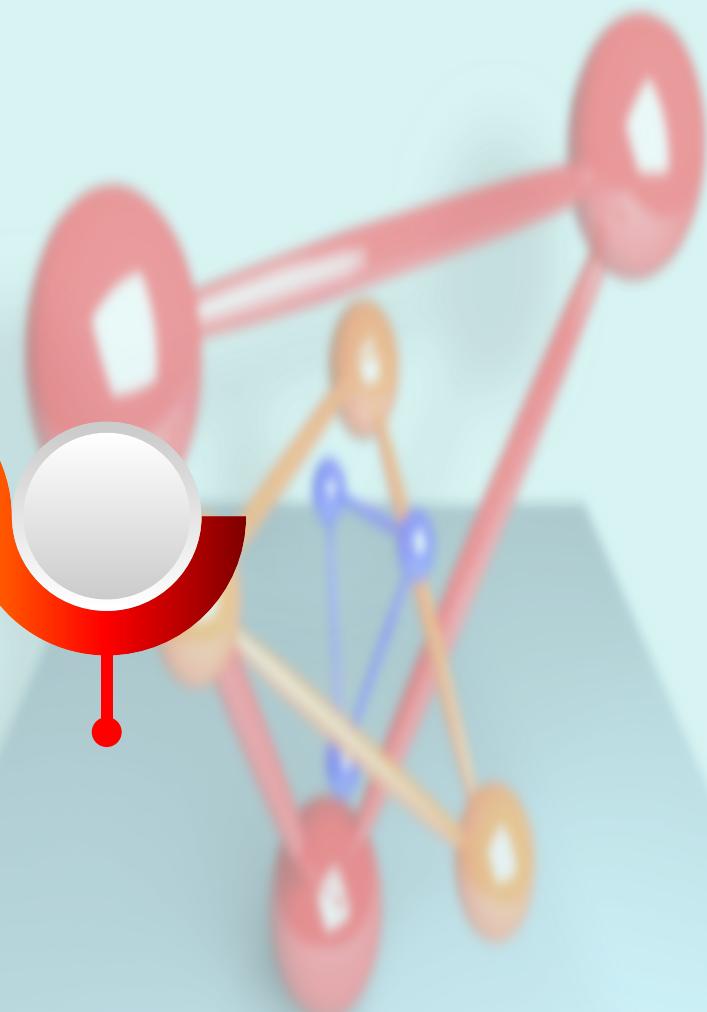
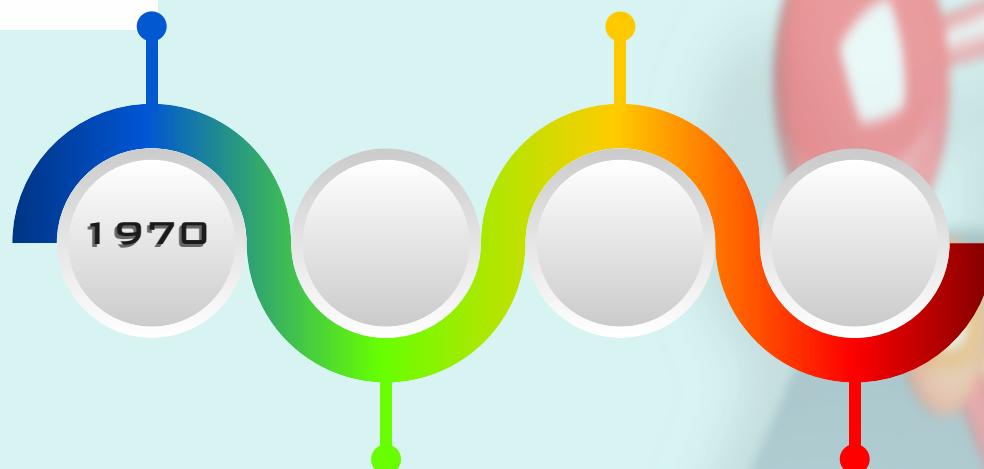
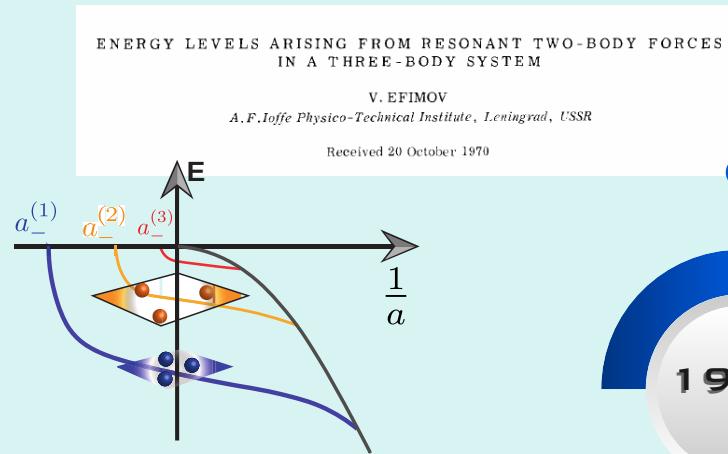
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SCIENCE @ DIRECT[®]
Physics Reports 428 (2006) 259–390
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Universality in few-body systems with large scattering length
Eric Braaten^a, H.-W. Hammer^{b,c,*}

IOP Publishing
J. Phys. B: At. Mol. Opt. Phys. **51** (2018) 043001 (49pp)
<https://doi.org/10.1088/1361-6455/aaa116>

Tutorial
Few-body physics in resonantly interacting ultracold quantum gases
José P D'Incao[†]

Efimov Physics in ultracold gases: A quick overview



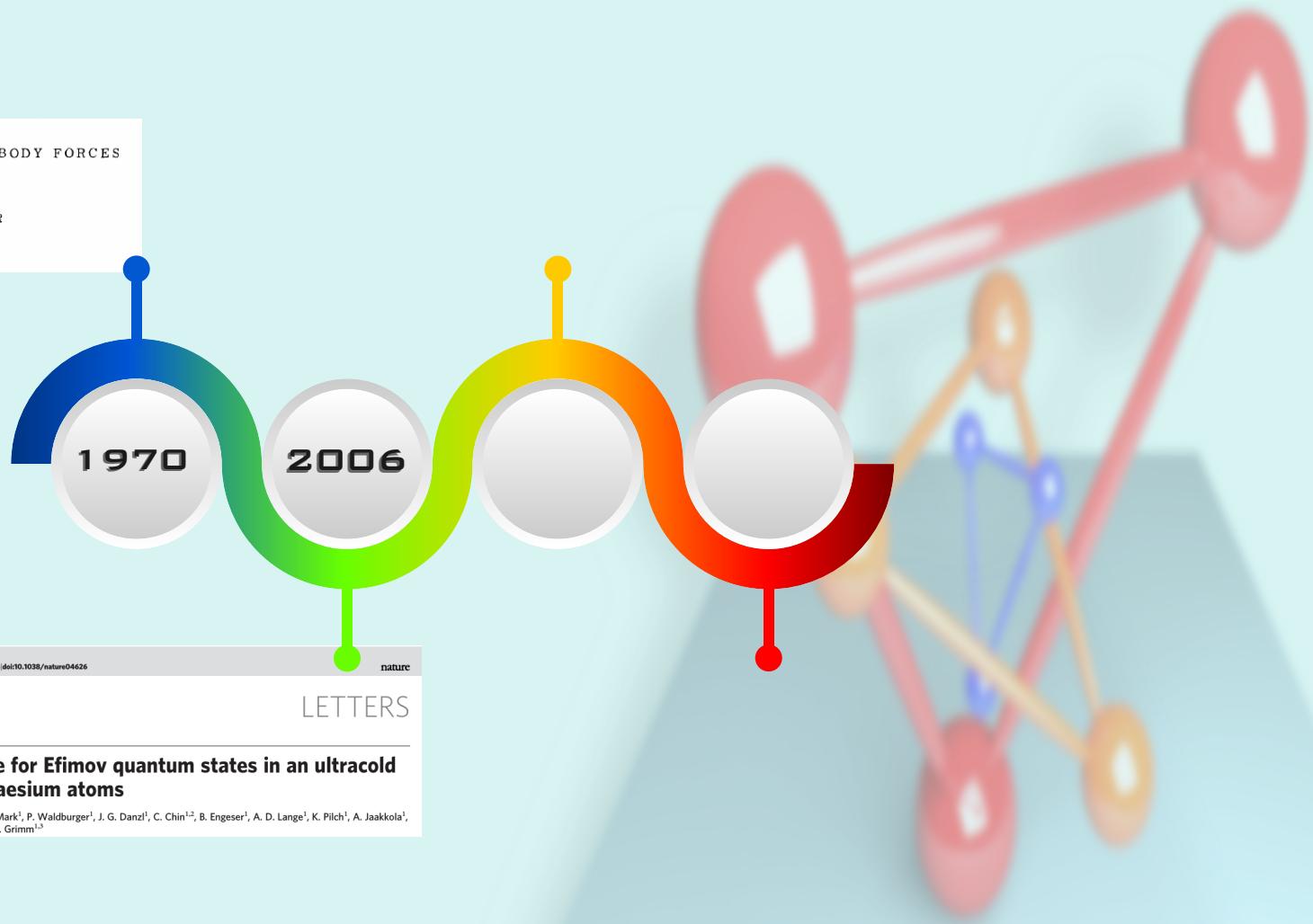
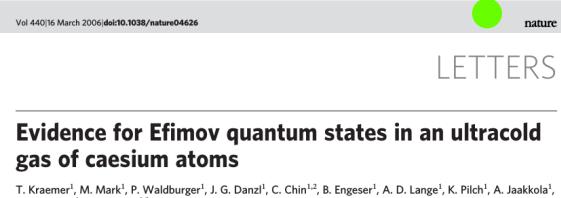
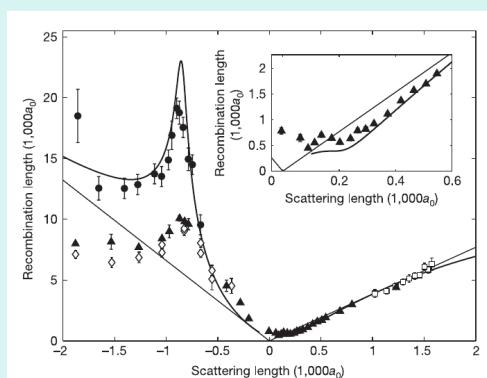
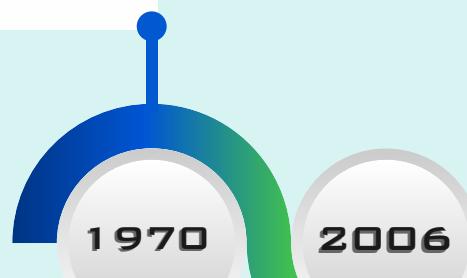
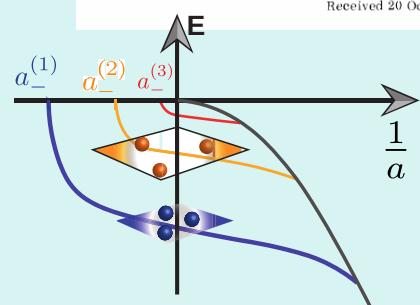
Efimov Physics in ultracold gases: A quick overview

ENERGY LEVELS ARISING FROM RESONANT TWO-BODY FORCES
IN A THREE-BODY SYSTEM

V. EFIMOV

A. F. Ioffe Physico-Technical Institute, Leningrad, USSR

Received 20 October 1970



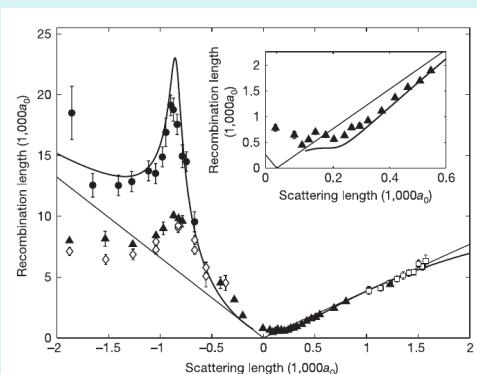
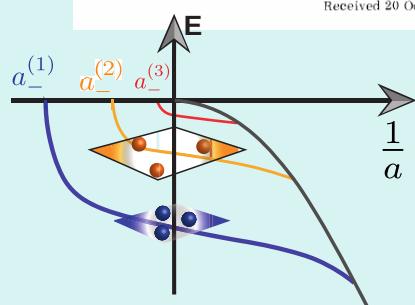
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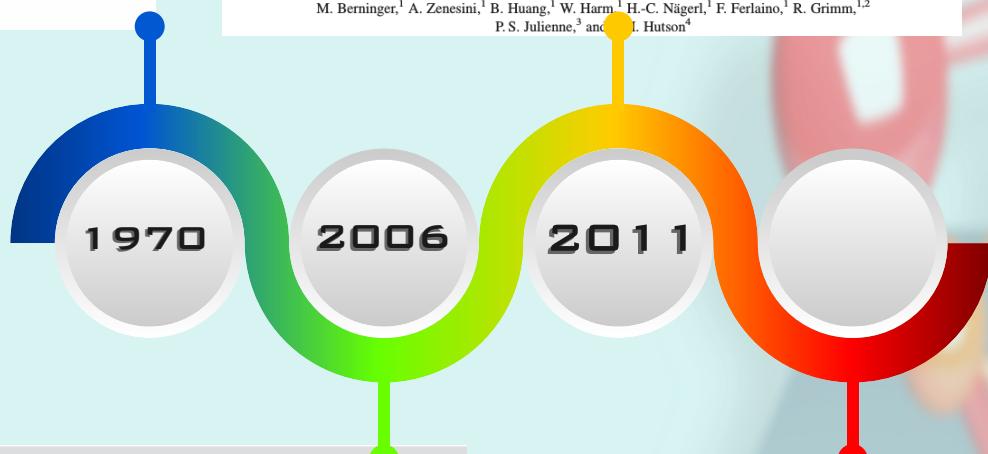
PRL 107, 120401 (2011)

PHYSICAL REVIEW LETTERS

week ending
16 SEPTEMBER 2011

Universality of the Three-Body Parameter for Efimov States in Ultracold Cesium

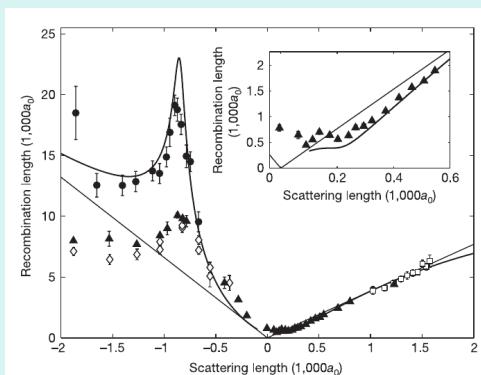
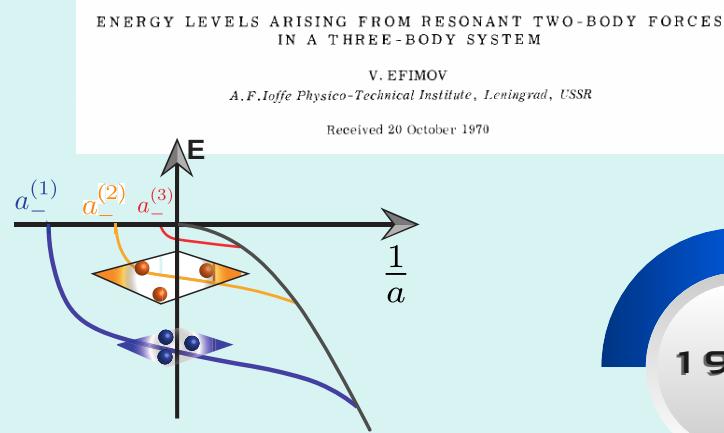
M. Berninger,¹ A. Zenesini,¹ B. Huang,¹ W. Harm,¹ H.-C. Nägerl,¹ F. Ferlaino,¹ R. Grimm,^{1,2}
P. S. Julienne,³ and J. I. Hutson⁴



Evidence for Efimov quantum states in an ultracold
gas of caesium atoms

T. Kraemer¹, M. Mark¹, P. Waldburger¹, J. G. Danzl¹, C. Chin^{1,2}, B. Engeser¹, A. D. Lange¹, K. Pilch¹, A. Jaakkola¹,
H.-C. Nägerl¹ & R. Grimm^{1,3}

Efimov Physics in ultracold gases: A quick overview



PRL 112, 105301 (2014) PHYSICAL REVIEW LETTERS week ending 14 MARCH 2014

Microscopic Origin and Universality Classes of the Efimov Three-Body Parameter

Pascal Naidon,^{1,*} Shimpei Endo,² and Masahito Ueda²

¹RIKEN Nishina Centre, RIKEN, Wako 351-0198, Japan

²Department of Physics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan

PRL 108, 263001 (2012) PHYSICAL REVIEW LETTERS week ending 29 JUNE 2012

Origin of the Three-Body Parameter Universality in Efimov Physics

Jia Wang,¹ J. P. D'Incao,¹ B. D. Esry,² and Chris H. Greene¹

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PRL 107,

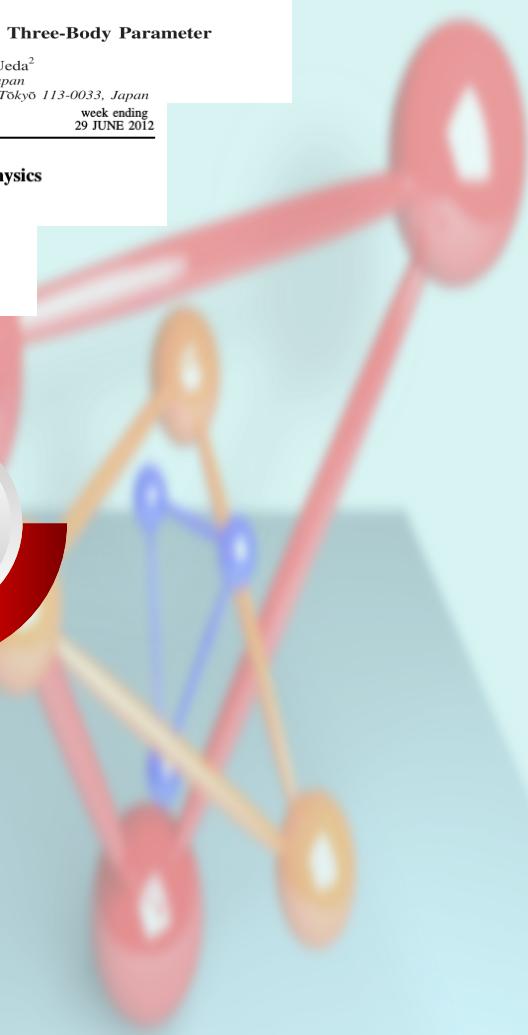
nature

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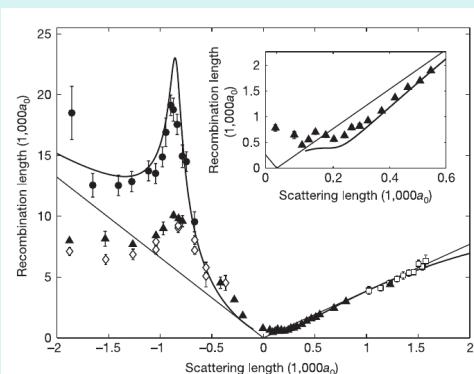
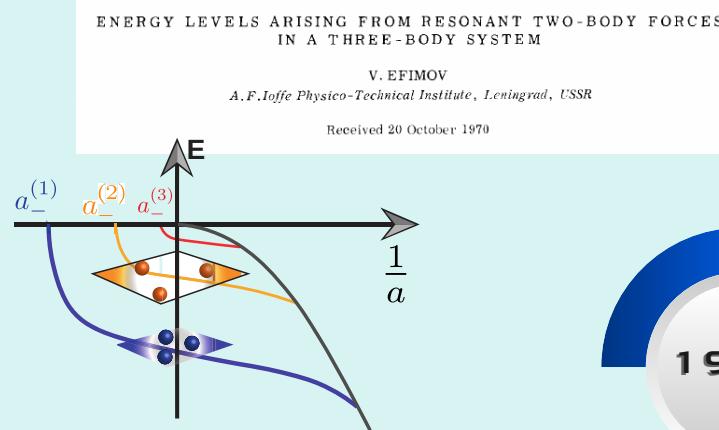
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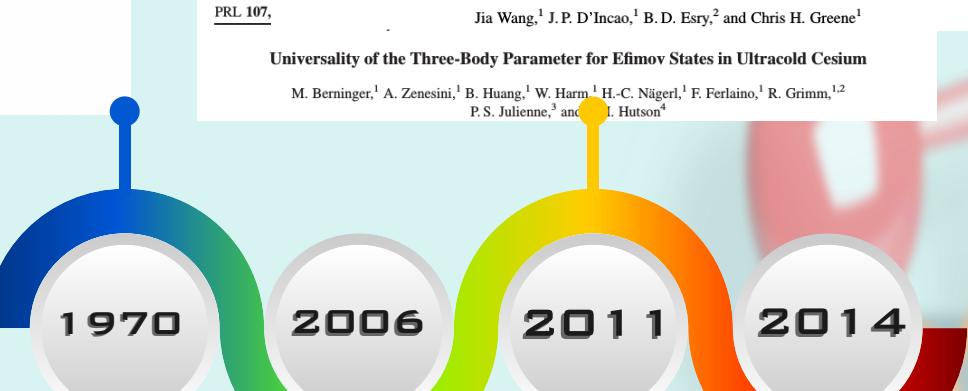


Efimov Physics in ultracold gases: A quick overview



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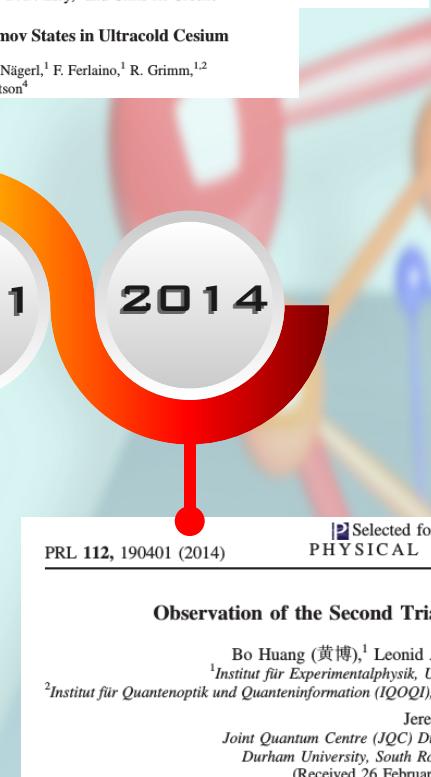
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P. S. Julienne,³ and J. M. Hutson⁴



Observation of the Second Triatomic Resonance in Efimov's Scenario

Bo Huang (黄博),¹ Leonid A. Sidorenkov,^{1,2} and Rudolf Grimm^{1,2}

¹Institut für Experimentalphysik, Universität Innsbruck, 6020 Innsbruck, Austria

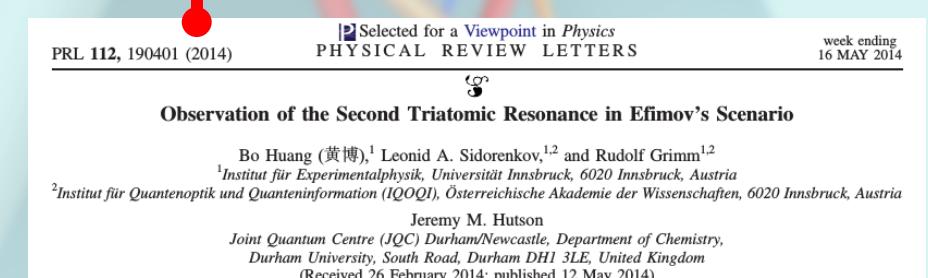
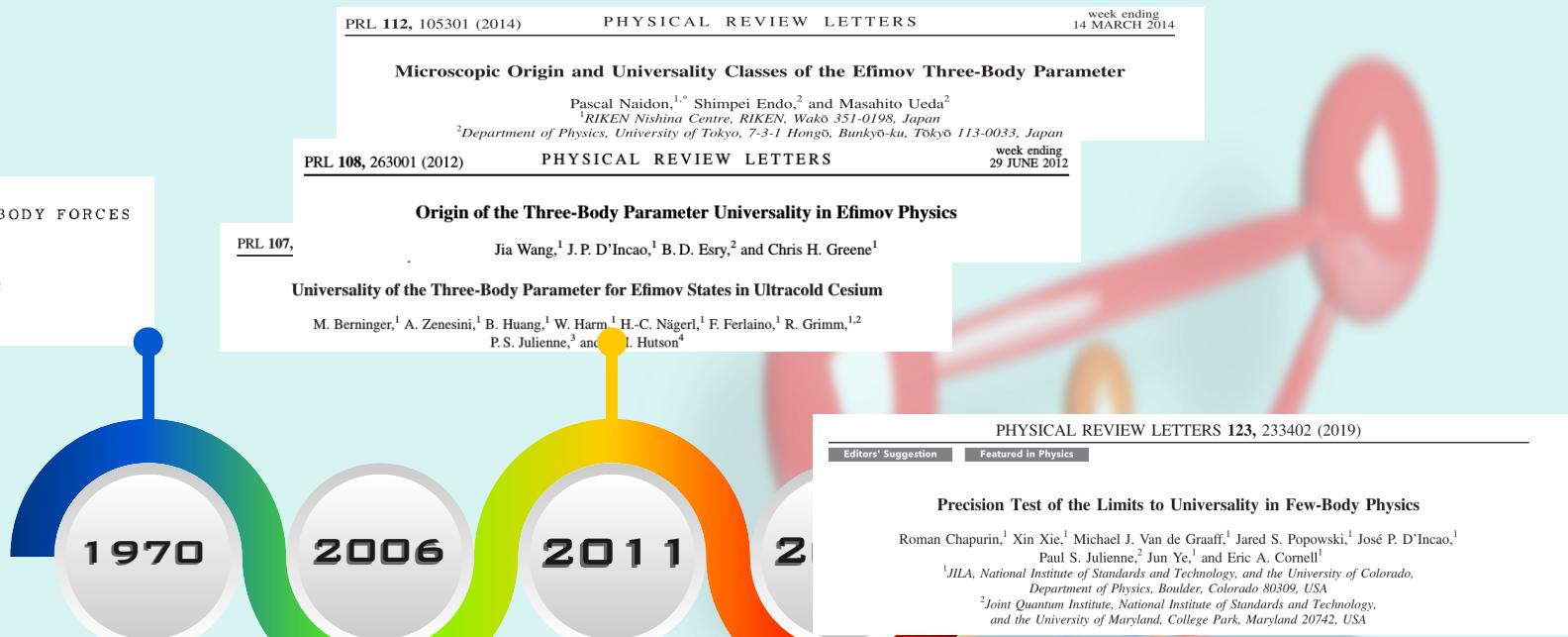
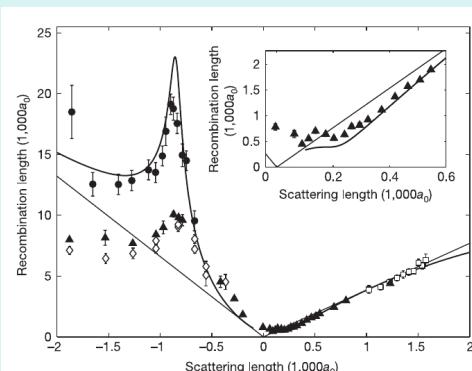
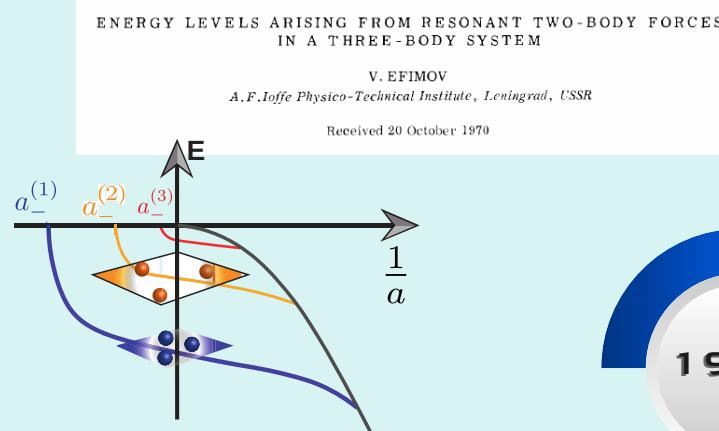
²Institut für Quantenoptik und Quanteninformation (IQOQI), Österreichische Akademie der Wissenschaften, 6020 Innsbruck, Austria

Jeremy M. Hutson

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(Received 26 February 2014; published 12 May 2014)

Efimov Physics in ultracold gases: A quick overview



Homo-**vs**-heteronuclear Efimov Physics

Motivation

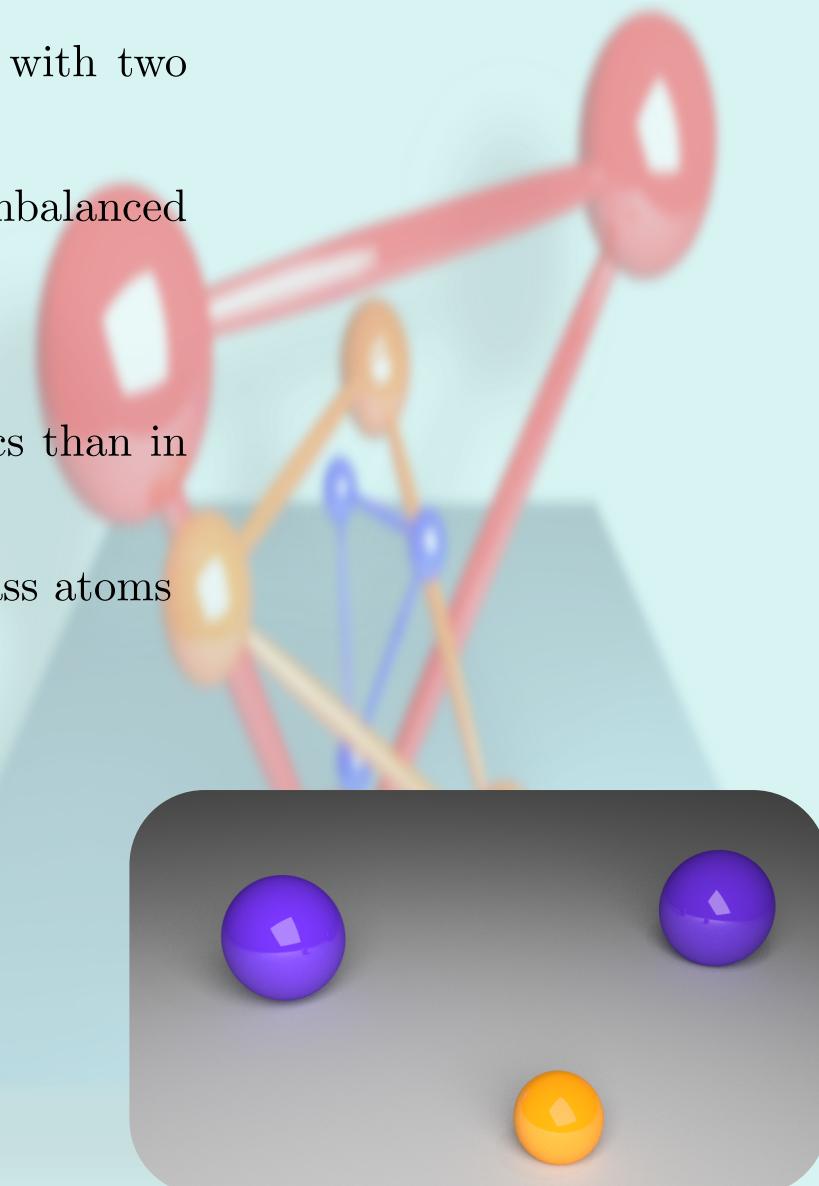
- Investigate the role of Efimov physics in collisions in systems with two heavy - one light particle
- Identify novel phenomena which govern the physics of a mass-imbalanced gas

Why mass-imbalanced systems?

- Three-body collisions in these systems possess far richer physics than in the case of equal mass particles
- Experimentally are more favorable than in the case of equal mass atoms
 - In the **homonuclear** case the Efimov states scale by ~ 22.7
 - In **heteronuclear** collisions the scaling factor is reduced

However...

- For **heteronuclear** systems the parameter space is **larger**
 - Intraspecies (**heavy-heavy**) scattering length, a_{HH}
 - Interspecies (**heavy-light**) scattering length, a_{HL}
- Both scattering lengths may vary in **sign**
- mass-ratio is an additional parameter



Homo-vs-heteronuclear Efimov Physics

- Recent experimental evidences suggest much richer Efimov physics
- Chin's group: $a_{\text{CsCs}} \gtrless 0$ & $a_{\text{LiCs}} \gtrless 0$



Geometric Scaling of Efimov States in a ${}^6\text{Li}-{}^{133}\text{Cs}$ Mixture

Shih-Kuang Tung, Karina Jiménez-García, Jacob Johansen, Colin V. Parker, and Cheng Chin*



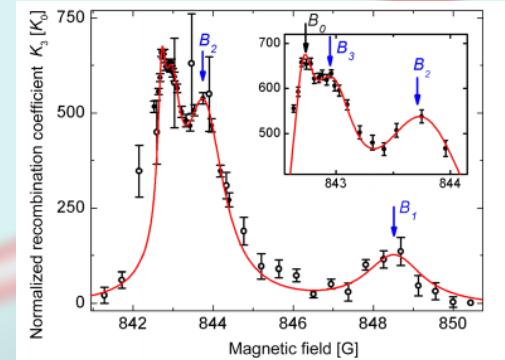
Testing universality of Efimov physics across broad and narrow Feshbach resonances

Jacob Johansen, B. J. DeSalvo, Krutik Patel and Cheng Chin*

Table 1 | Summary of Efimov resonances for the three Feshbach resonances in Li-Cs at 843 (ref. 12), 889, and 893 G.

B_0 (G)	s_{res}	$a_{\text{CsCs}}(a_0)$	$a_-^{(2)}(a_0)$	$a_{\text{th}}^{(2)}(a_0)$
888.577(10)(10)	0.66	200	-2,050(60)	-2,150
892.648(1)(10)	0.05	260	-3,330(240)	-2,200
842.750(1)(3)	0.66	-1,400	-1,635(60)	-1,680

Here, B_0 indicates the Feshbach resonance position, s_{res} the Feshbach resonance strength, a_{CsCs} the Cs-Cs scattering length, $a_-^{(2)}$ the resonance position associated with the second Efimov state, and $a_{\text{th}}^{(2)}$ the prediction from the universal theory using a single-channel model^{28,29}.

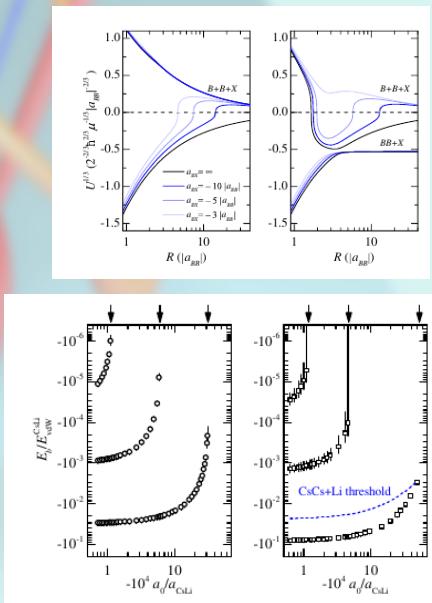
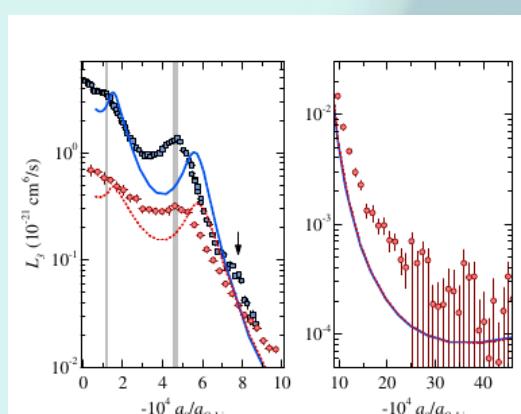


- Weidemüller's group: $a_{\text{CsCs}} > 0$ & $a_{\text{LiCs}} < 0$



Heteronuclear Efimov Scenario with Positive Intraspecies Scattering Length

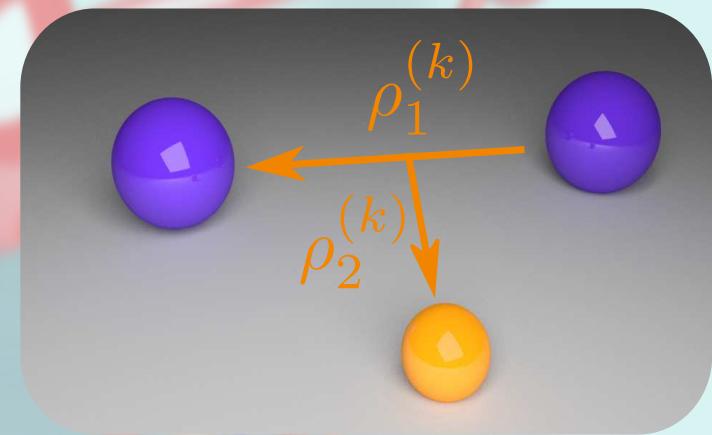
Juris Ulmanis,¹ Stephan Häfner,¹ Rico Pires,¹ Eva D. Kuhnle,¹ Yujun Wang,^{2,†} Chris H. Greene,^{3,*} and Matthias Weidemüller^{1,4,†}



A system of mass-imbalanced atoms

- Consider a system of two heavy and one light particle

$$H_{tot} = \sum_{i=1}^3 -\frac{\hbar^2}{2m_i} \nabla_i^2 + \sum_{i>j} V_{i,j}(r_{ij})$$



- The mutual two-body interactions are approximated via zero-range pseudopotentials
- Theoretical approach: The adiabatic hyperspherical representation

Adiabatic Hyperspherical Representation

- Hyperspherical coordinates:

$$\rho_1^{(k)} = R \sin \alpha^{(k)}, \quad \rho_2^{(k)} = R \cos \alpha^{(k)} \quad \& \quad \Omega^{(k)} = \{\omega_1^{(k)}, \omega_2^{(k)}, \alpha^{(k)}\}$$

- The total wavefunction reads:

$$\Psi(R, \Omega) = \sum_n R^{-5/2} F_n(R) \Phi_n(R; \Omega)$$

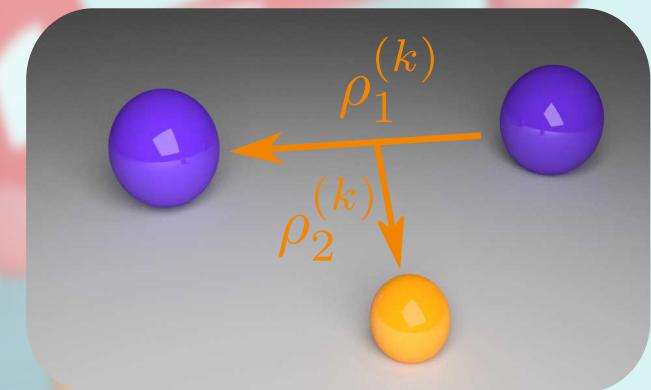
- The Hyperangular Equation for contact interactions:

$$H_{ad}(R; \Omega) \Phi_n(R; \Omega) = U_n(R) \Phi_n(R; \Omega)$$

- 1D coupled hyper-radial equations:

$$-\frac{\hbar^2}{2\mu} \frac{d^2}{dR^2} F_n(R) + (U_n(R) - E) F_n(R) = \frac{\hbar^2}{2\mu} \sum_m [2P_{nm} \frac{d}{dR} + Q_{nm}] F_m(R),$$

where $P_{nm} = \langle \Phi_n | \frac{\partial}{\partial R} | \Phi_m \rangle_\Omega$ and $Q_{nm} = \langle \Phi_n | \frac{\partial^2}{\partial R^2} | \Phi_m \rangle_\Omega$



E. Nielsen et al, Physics Reports 347, 373 (2001)

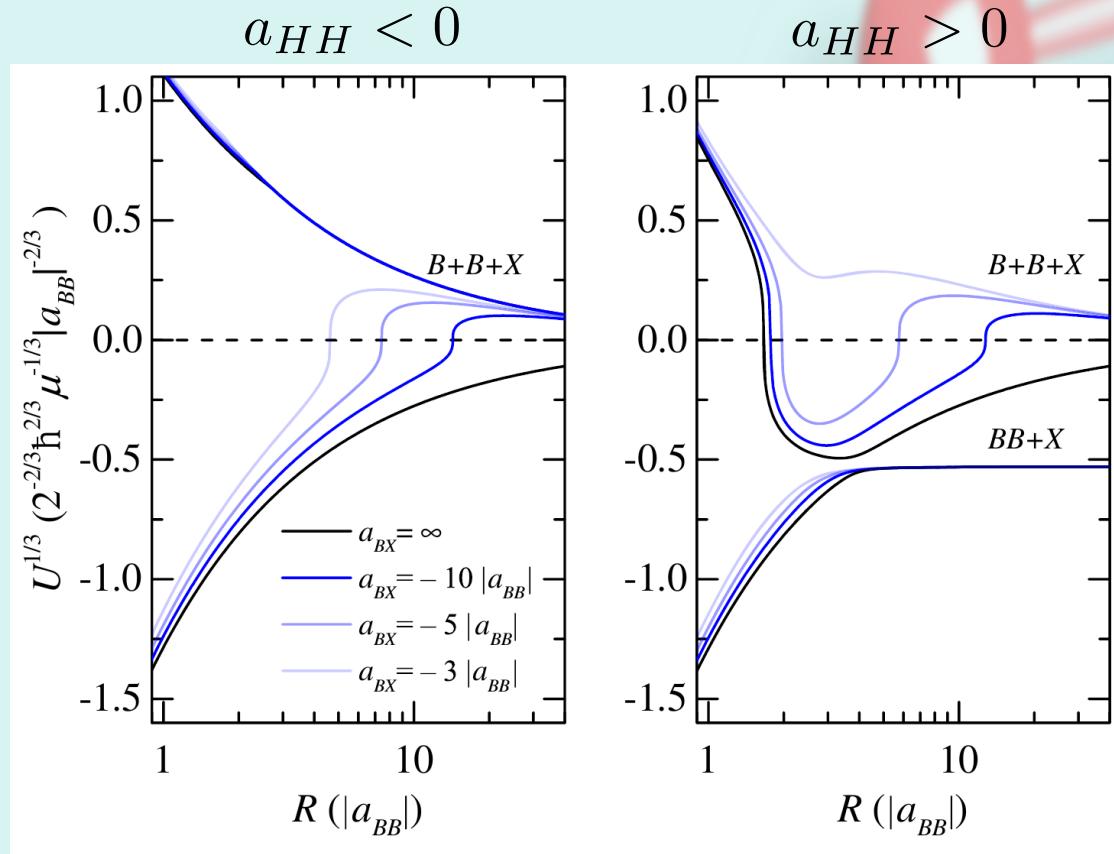
O. I. Kartavtsev and A. V. Malykh, JPB 40, 1429 (2007)

S.T. Rittenhouse et al, PRA 82, 022706 (2010)

Adiabatic Hyperspherical Representation

- Adiabatic potential curves

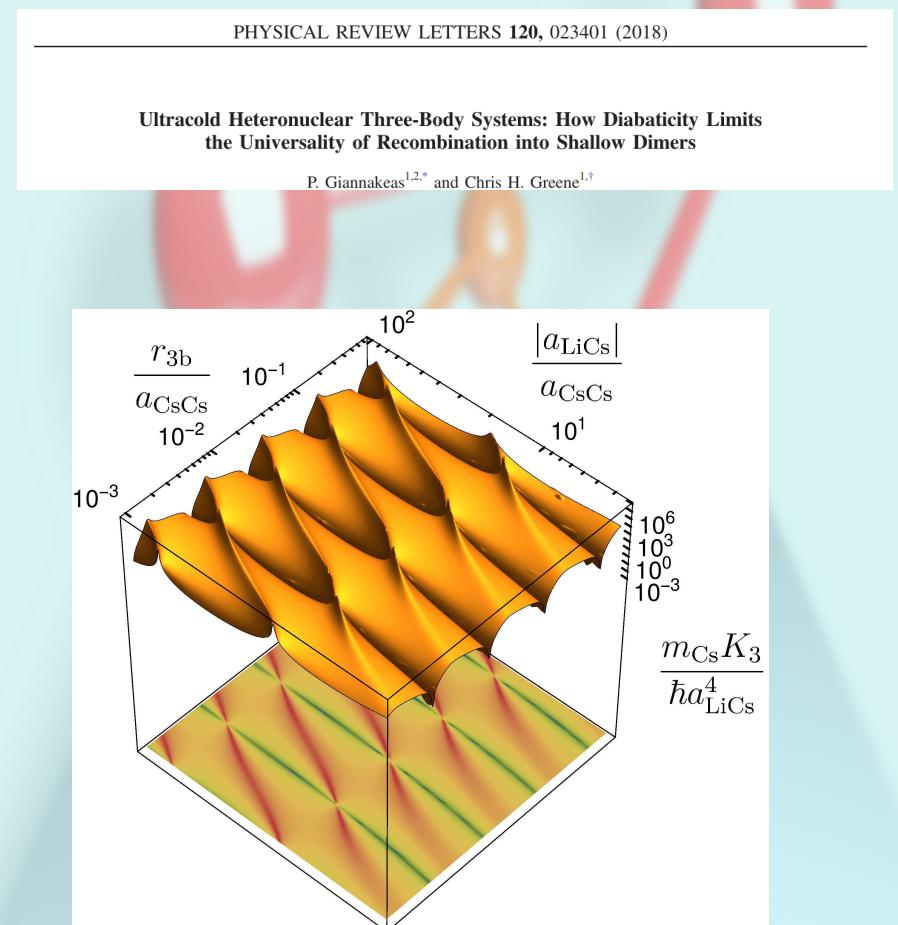
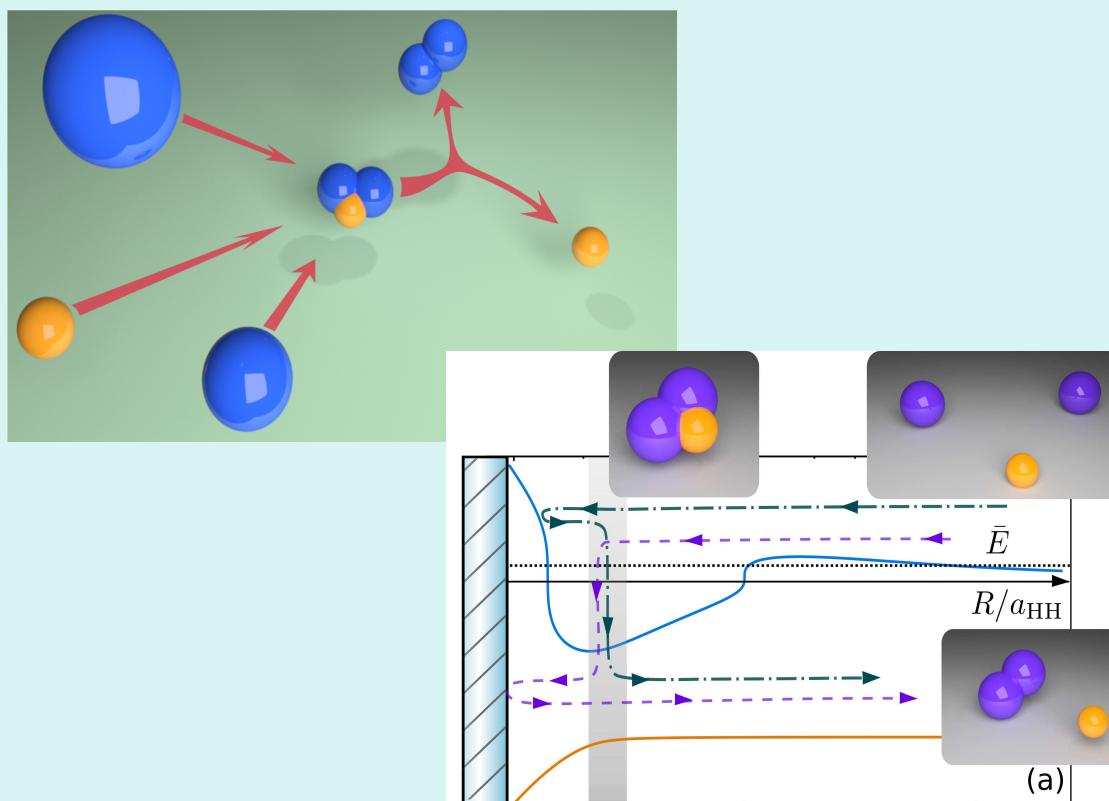
- For $a_{HL} < 0$ and $a_{HH} \gtrless 0$



Ulmanis et al, PRL 117, 153201 (2016)

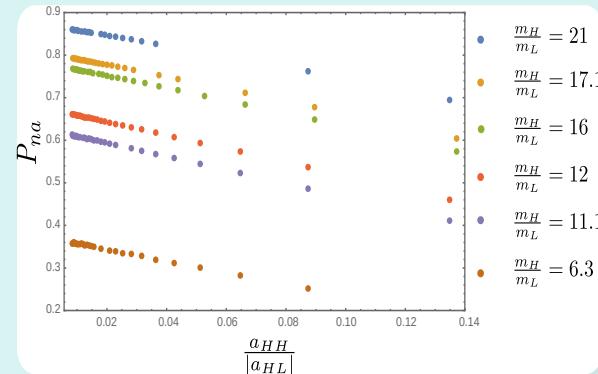
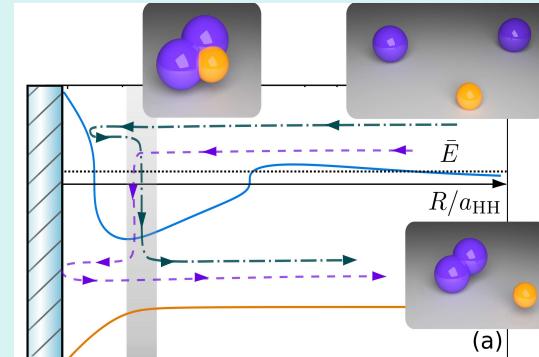
Three-body recombination into shallow dimers

- Rich topology: Efimov resonances + Stückelberg minima
- A unique property of HHL systems

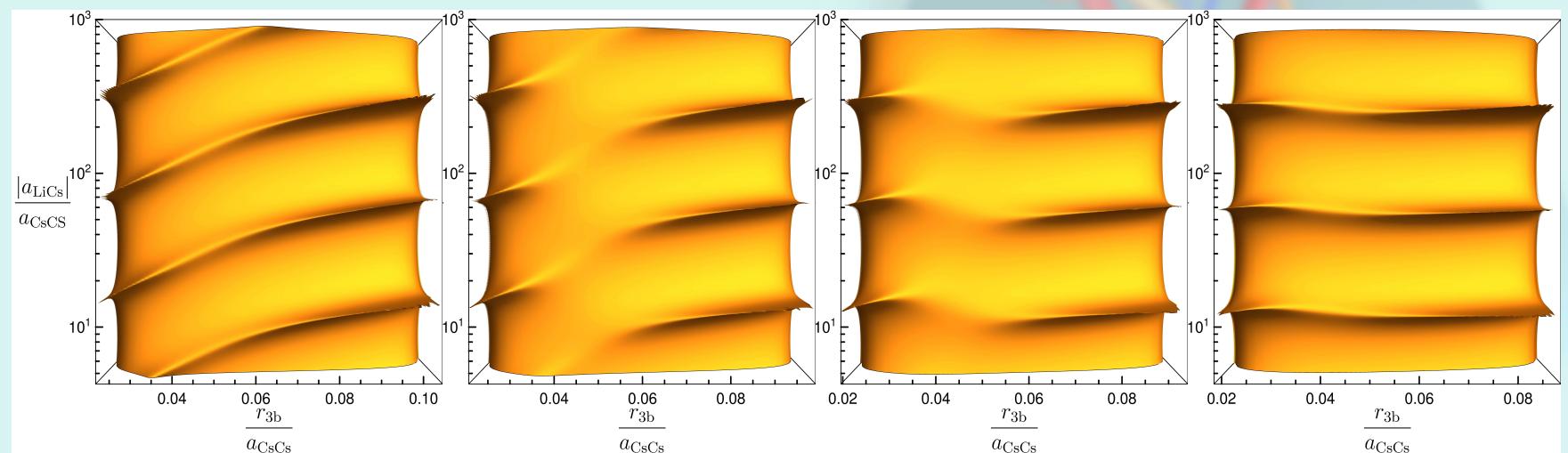


Three-body recombination into shallow dimers

- How the “diabaticity” affects the resonant structure?

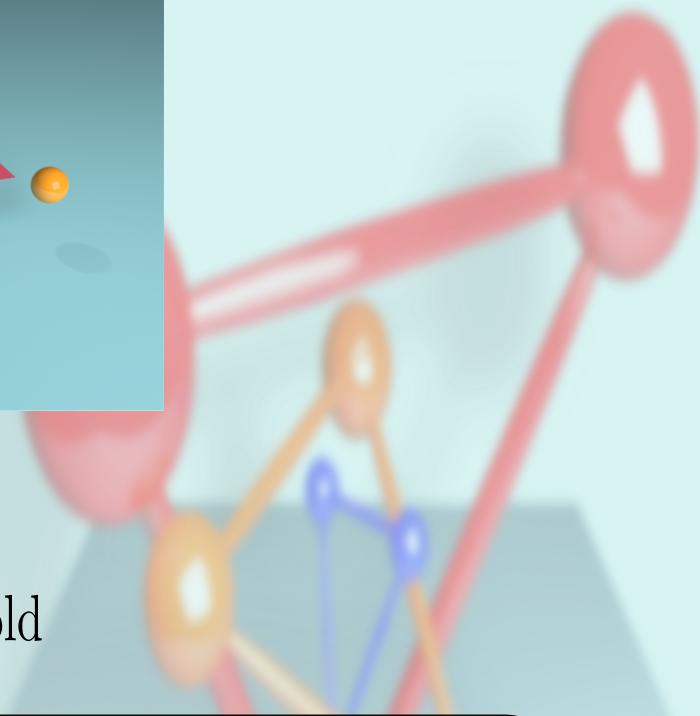
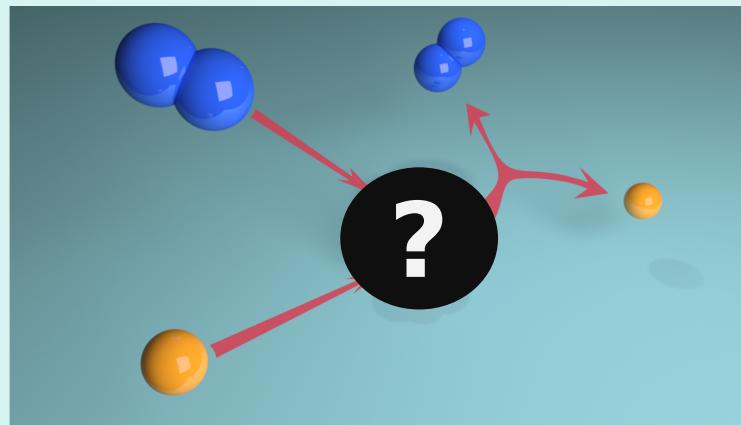


- Vary the Landau-Zener probability: Diabatic \rightarrow Adiabatic
- The less diabatic are the collisions the more universal are the Efimov resonances

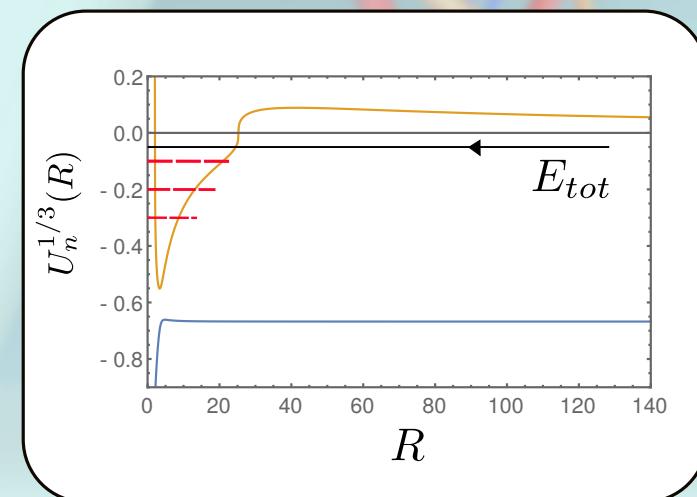
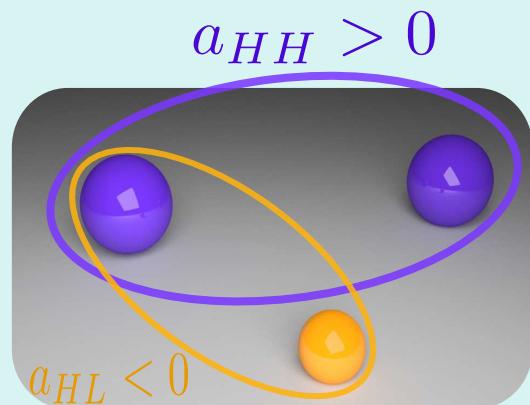


Atom-dimer collisions in mass-imbalanced gases

Physical system

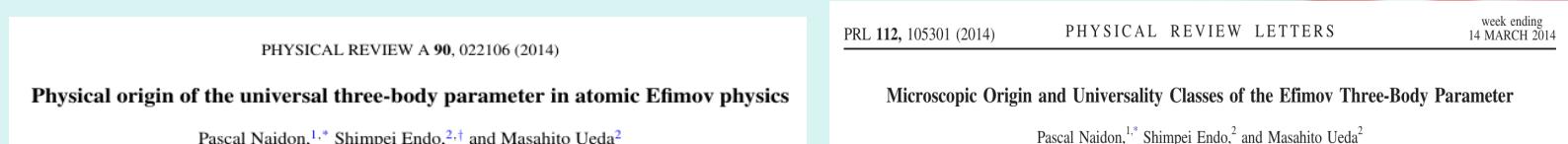


- Consider a heavy-heavy dimer colliding with a light atom
- The energy regime of interest lies below the break-up threshold

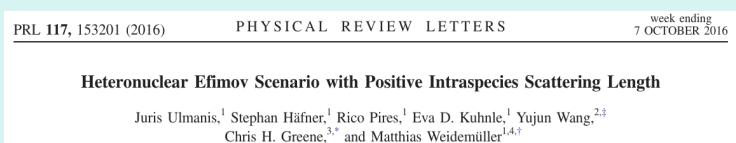


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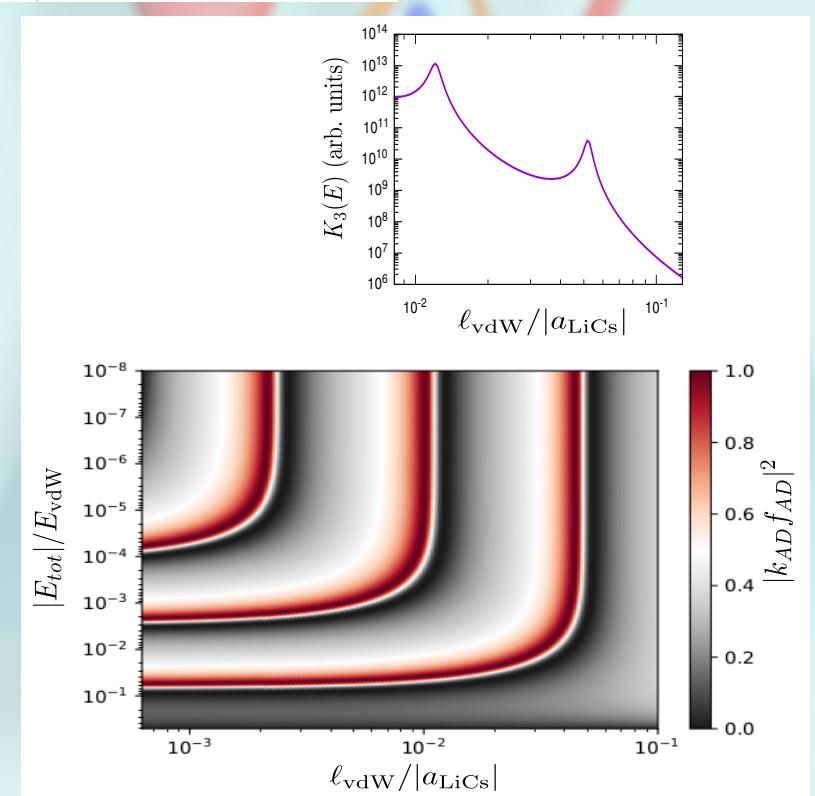
- Atom-dimer collisions are treated with Faddeev equations
- The pairwise interactions are modeled via Yamaguchi potentials
- Naidon's type of Yamaguchi potential → successfully captures the physics of Van der Waals interactions ($\sim 1/r^6$)



- Focus on ${}^6\text{Li}-{}^{133}\text{Cs}-{}^{133}\text{Cs}$
- Using the Li-Cs Feshbach resonance at $B = 889$ G, where $a_{\text{CsCs}} = 190 a_0$
- Parameters are relevant to the experiments:

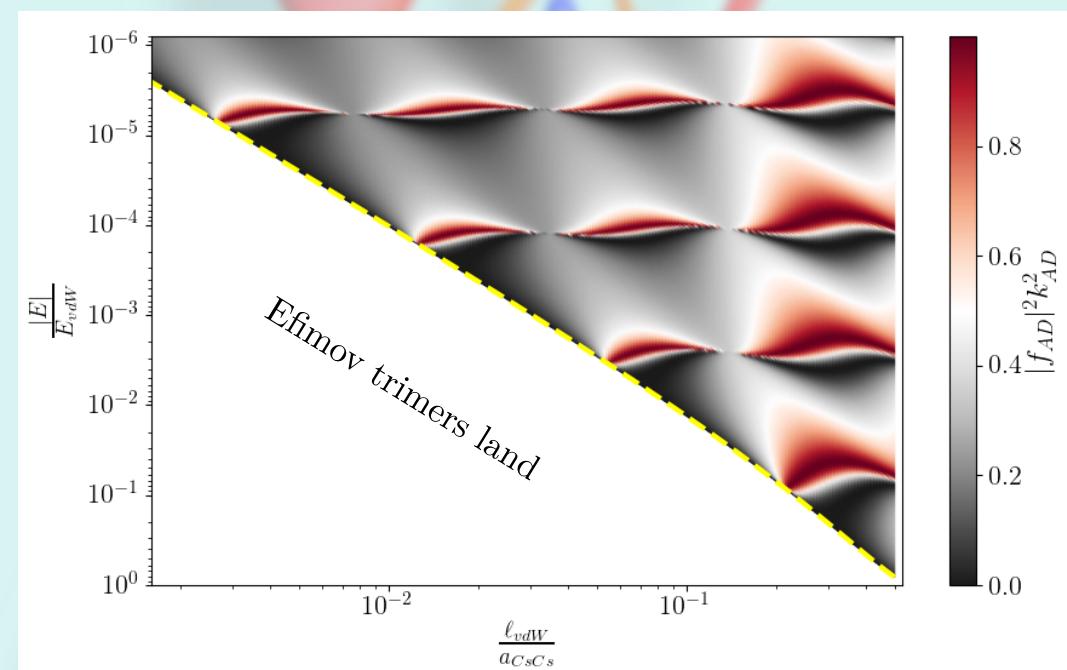


- K_3 and atom-dimer resonances near the break-up threshold are in agreement



Atom-dimer collisions in mass-imbalanced gases

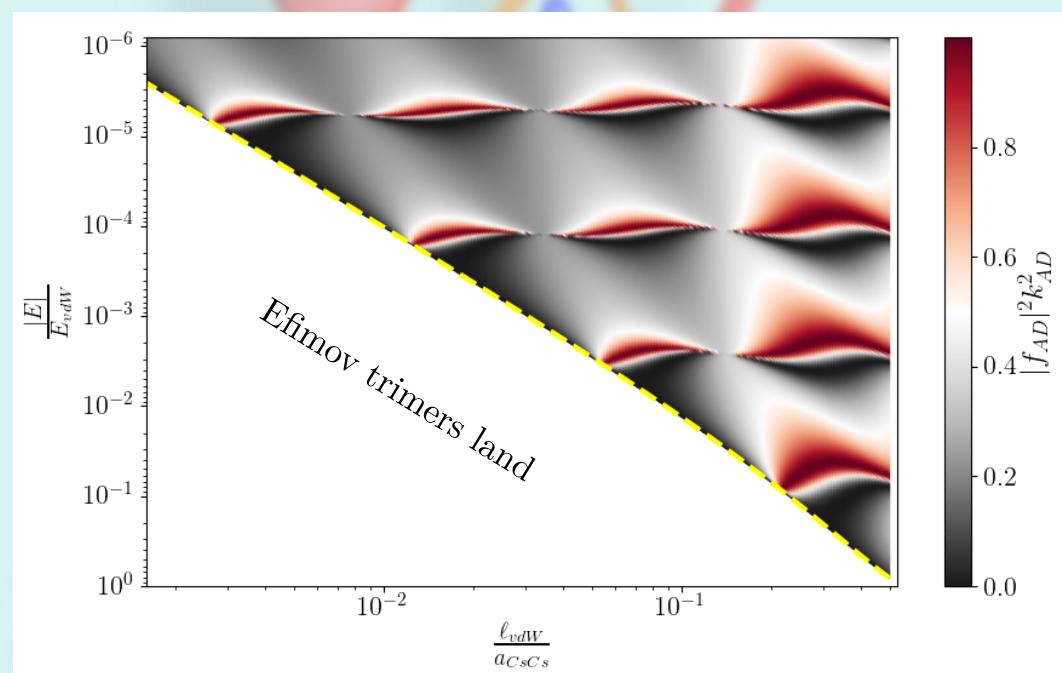
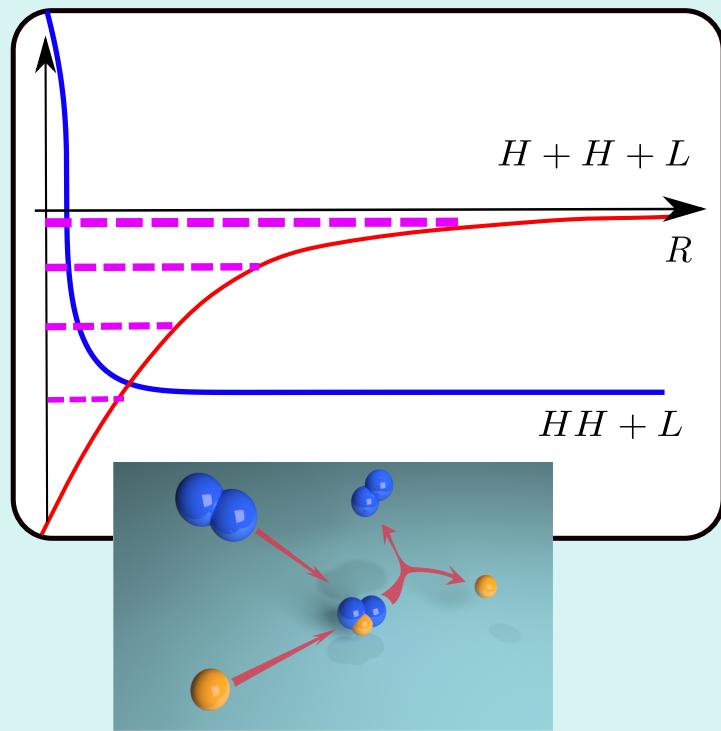
- Atom-dimer collisions near unitarity $|a_{HL}| \rightarrow \infty$
- Collisions are more diabatic close to the unitarity limit
- Emerging Stückelberg physics in the atom-dimer spectra



Atom-dimer collisions in mass-imbalanced gases

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- Collisions are more diabatic close to the unitarity limit
- Emerging Stückelberg physics in the atom-dimer spectra

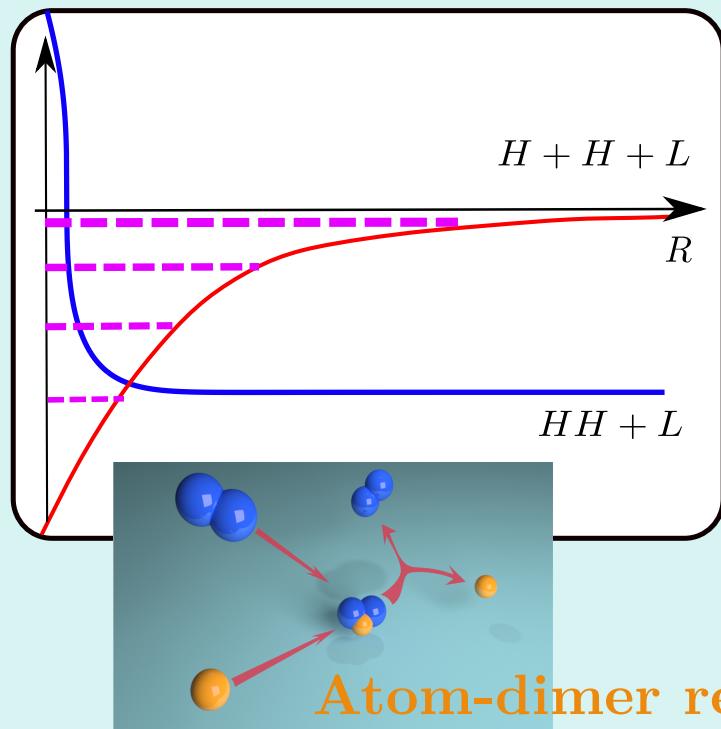
Intuitive Picture: **Diabatized**
Hyperspherical potential curves



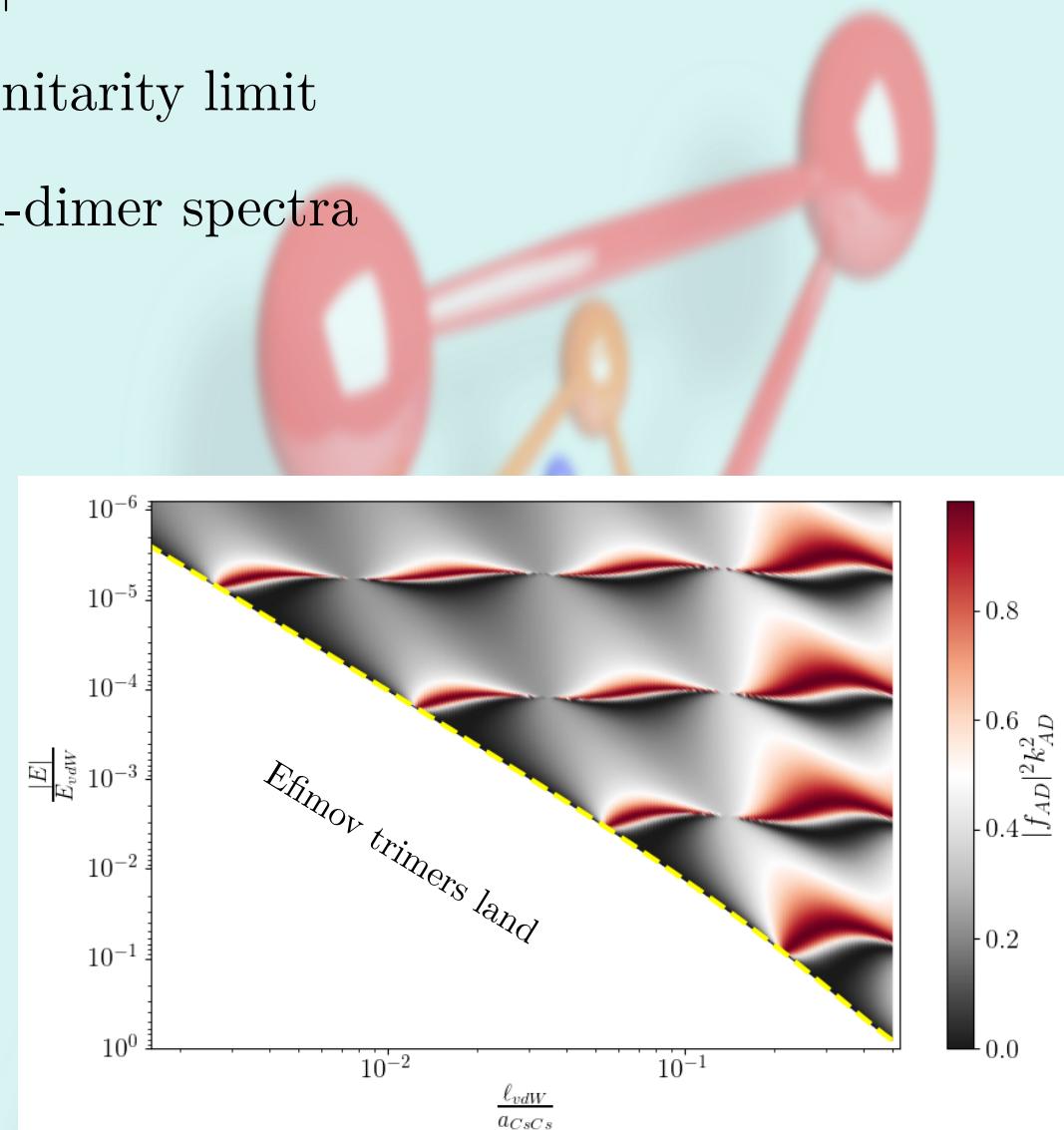
Atom-dimer collisions in mass-imbalanced gases

- Atom-dimer collisions near unitarity $|a_{HL}| \rightarrow \infty$
- Collisions are more diabatic close to the unitarity limit
- Emerging Stückelberg physics in the atom-dimer spectra

Intuitive Picture: **Diabatized**
Hyperspherical potential curves

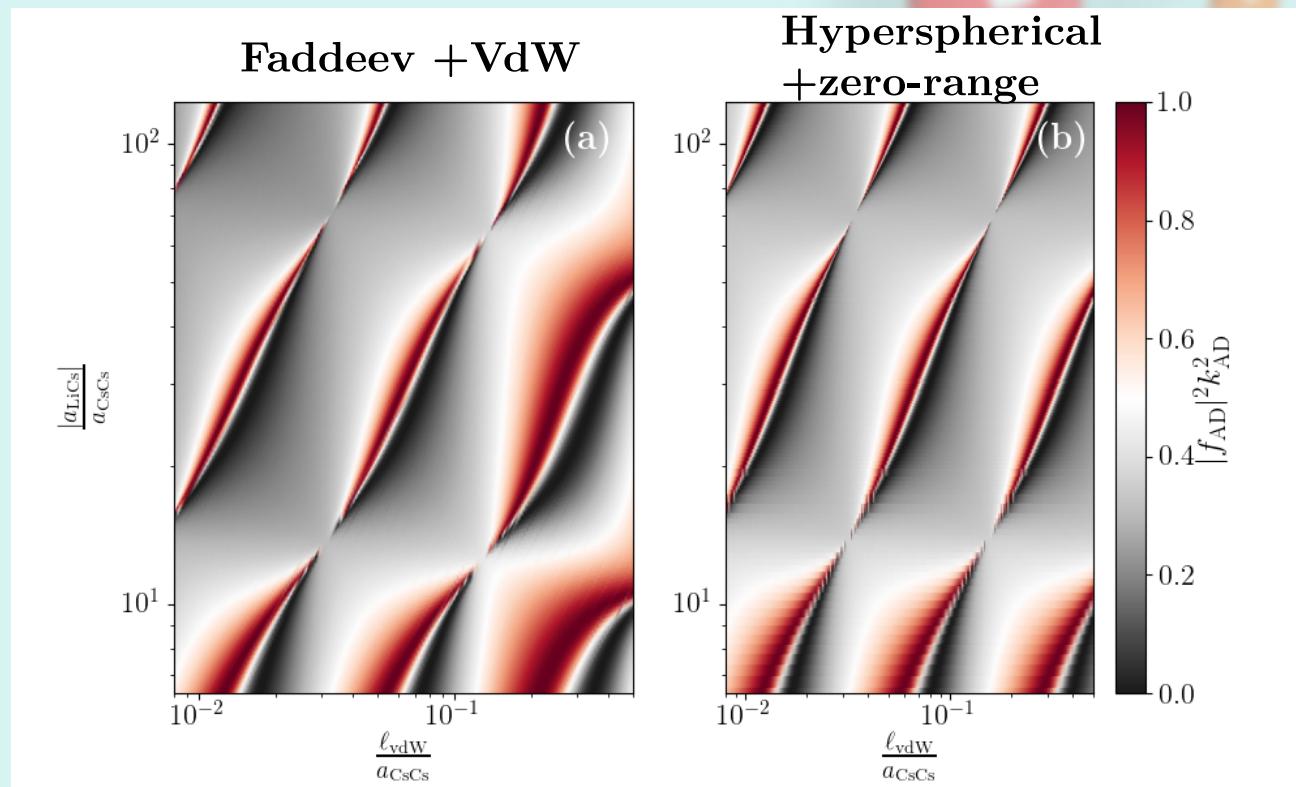


Atom-dimer resonances \rightarrow Fano-Feshbach mechanism



Atom-dimer collisions in mass-imbalanced gases

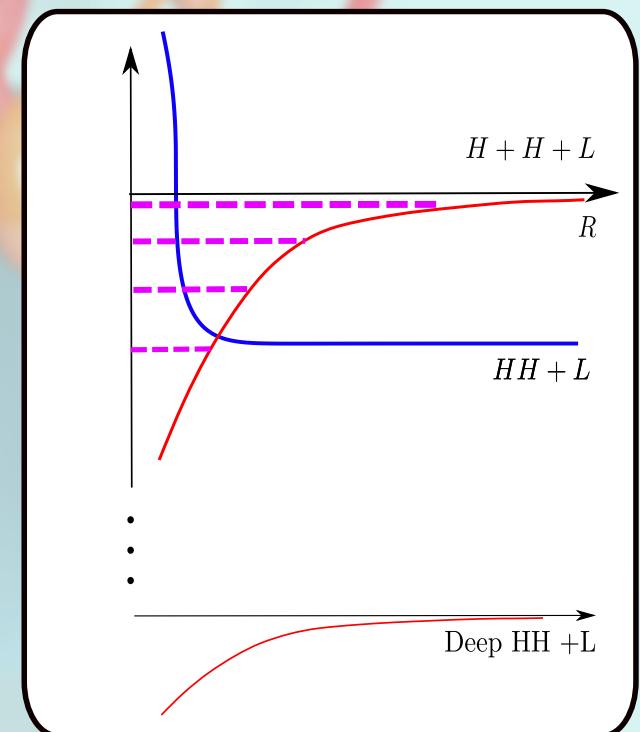
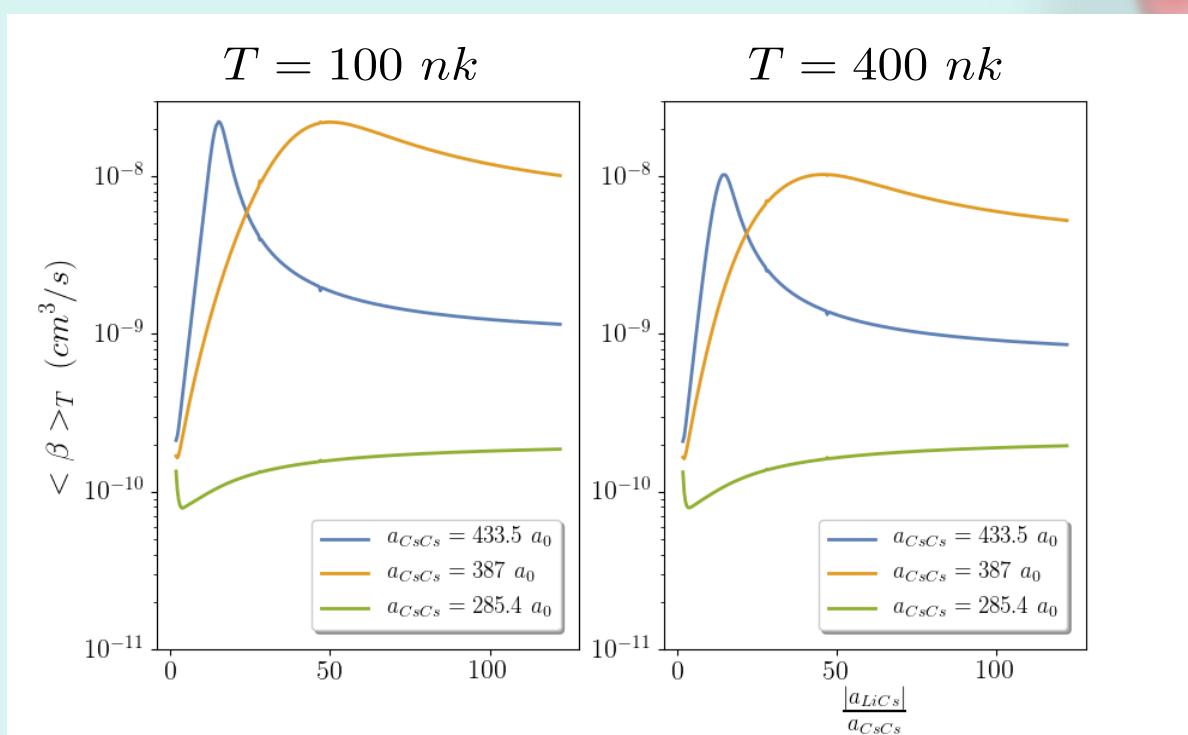
- Probing the regime of univerality at near break-up threshold energies
- Comparing zero-range Hyperspherical coordinates treatment with Faddeev approach
- Van der Waals physics is important for $a_{CsCs} < 10^3 a_0$



Atom-dimer collisions in mass-imbalanced gases

- Considering inelastic processes, i.e. **atom-dimer relaxation**
- Atom-dimer collisions can go to a deeply dimer+ a recoiling atom
- Quantity of interest: **Thermally averaged atom-dimer relaxation coefficient**

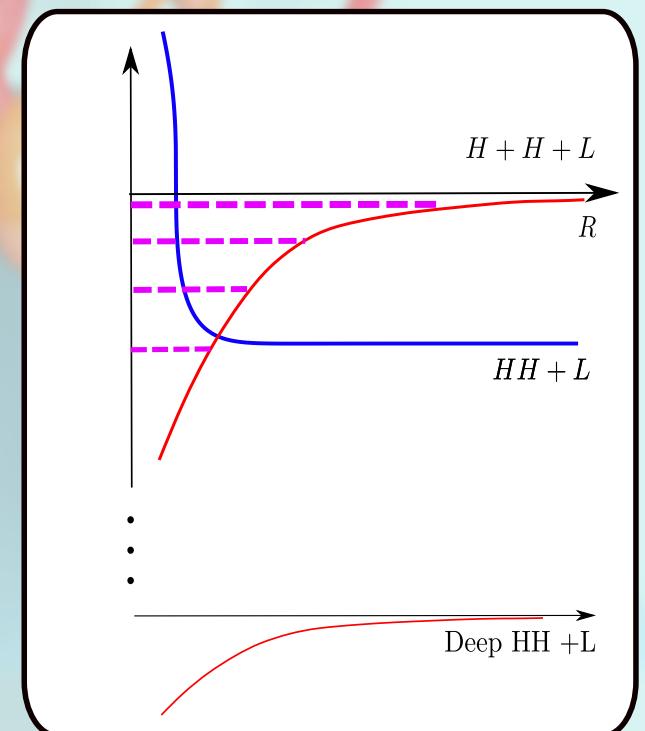
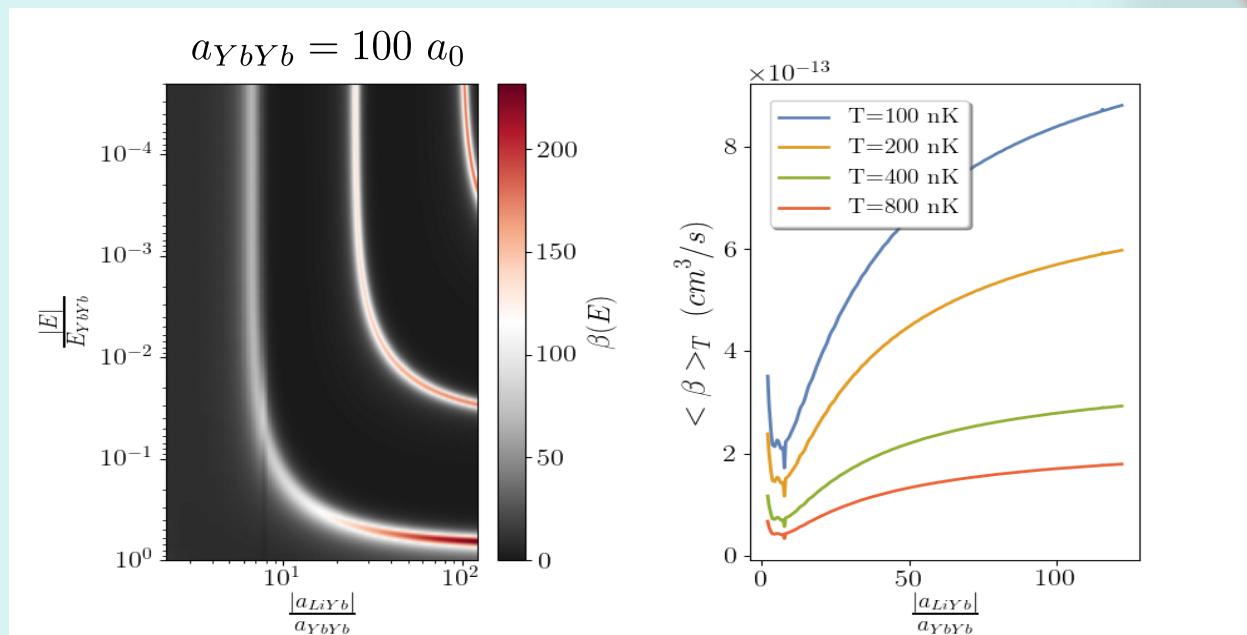
For ${}^6\text{Li}$ - ${}^{133}\text{Cs}$ - ${}^{133}\text{Cs}$:



Atom-dimer collisions in mass-imbalanced gases

- Large mass ratio are more favorable to observe the Fano-Feshbach atom-dimer resonances via deep dimer relaxation processes
- Available ranges of heavy-heavy scattering lengths is a necessity

For ${}^6\text{Li}$ - ${}^{174}\text{Yb}$ - ${}^{174}\text{Yb}$:



Conclusions

- Efimov physics possesses unique features in mass-imbalanced ultracold gases
- Three-body recombination processes to shallow dimers exhibit intertwined Efimov resonances + Stückelberg minima
- Atom-dimer resonances fulfill Fano-Feshbach scenario due to Efimov trimer states

