

# Study of $\bar{K}$ -cluster by using $(K^-, N)$ reaction

Reference

<https://doi.org/10.1093/ptep/ptaa139>

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2020/09/24, 25

第5回クラスター階層領域研究会

*(Introduction)*  
 *$\Lambda(1405)$  and  $K^-pp$*

# $\Lambda(1405)$

- $\Lambda(1405)$  is assigned as an excited three quark baryon (u, d, s) with  $I = 0$  and  $J^P = (1/2)^-$  in the constituent quark model.
- However, the observed mass is smaller about 80 MeV than the theoretical prediction.

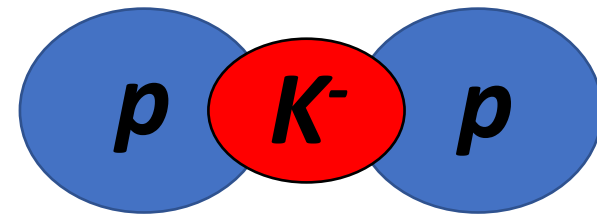


- $\bar{K}N$  bound state(?) two pole state(?)



- Many body system called as Kaonic nuclei is expected.  
Ex:  $K^-pp$ ,  $K^-K^-pp$ , etc...

# $K^-pp$ bound state

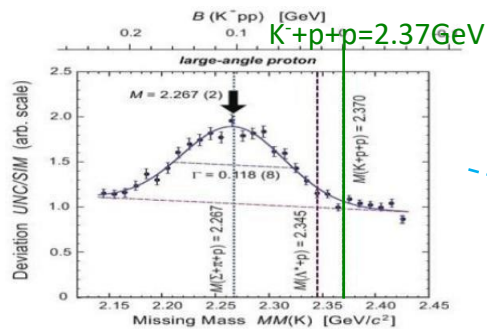


- It is expected to be the simplest kaonic nuclei.
- $\bar{K}NN$ , Total charge: +1,  $I = \frac{1}{2}$ ,  $J^P = 0^-$ .
- The bound state was expected due to the  $\bar{K}N$  strong interaction, which is strongly attractive in  $I = 0$ .
- It has a rich information such as the  $\bar{K}N$  strong interaction in sub-threshold region and behavior of  $\Lambda(1405)$  in many body system.
- It makes high density (?)

# $K^-pp$

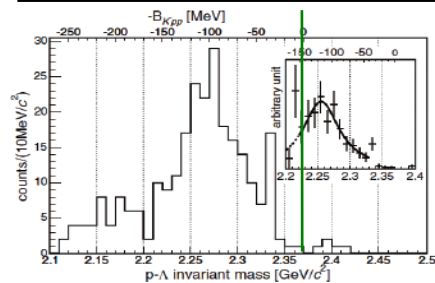
$p$   $K^-$   $p$

**DISTO:  $p(p, K^+)\Lambda p$**



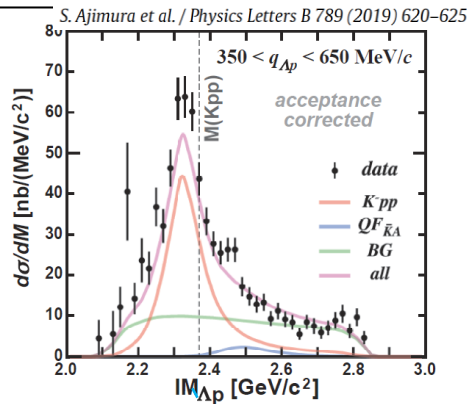
T.Yamazaki *et al.*, PRL 104, 132502 (2010)

**FINUDA: stopped  $K^-$**



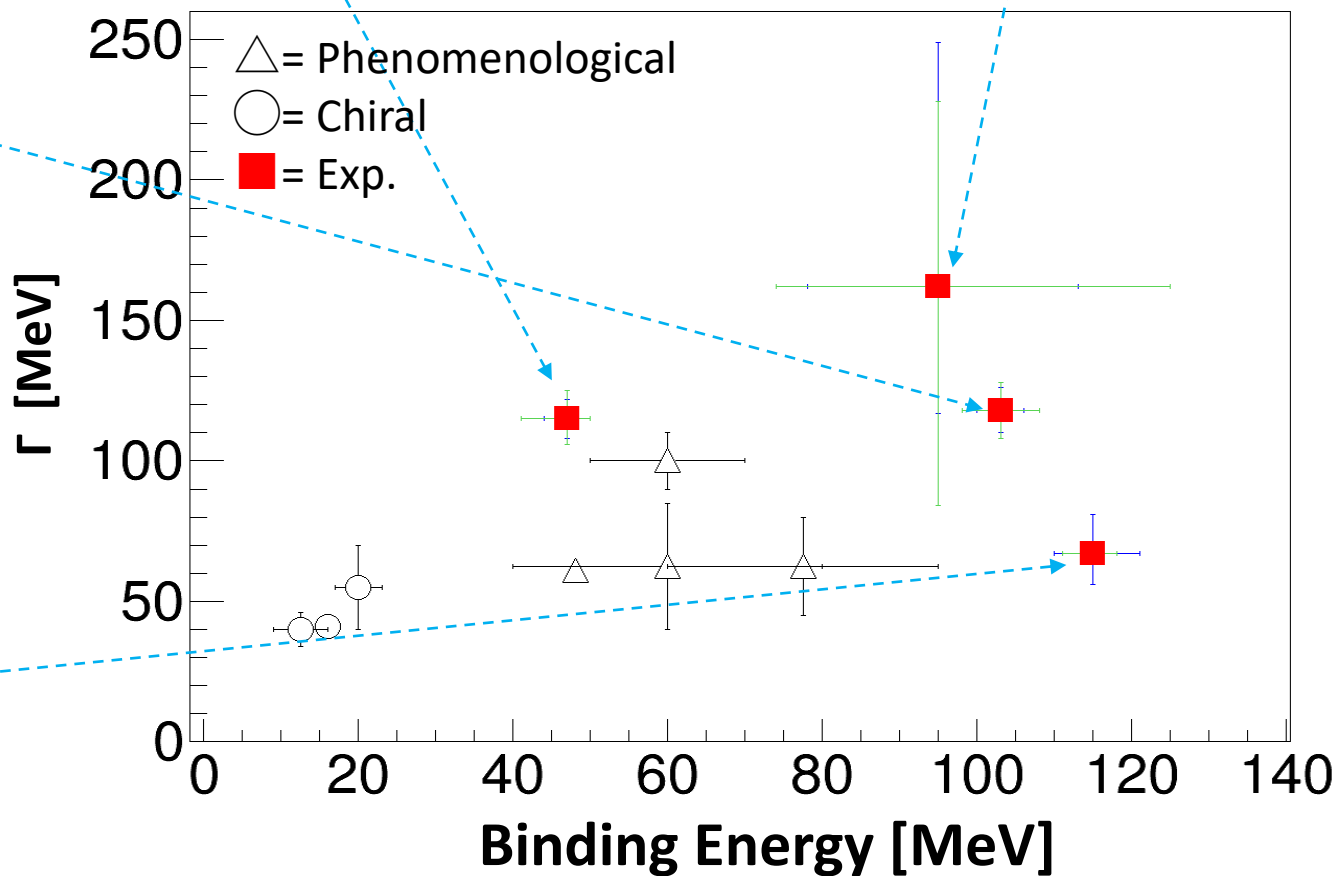
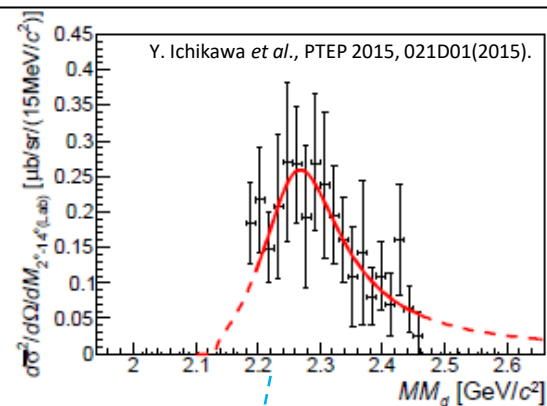
M.Agnello *et al.*, PRL 94, 212303 (2005)

**J-PARC E15:  $^3\text{He}(K^-, \Lambda p)n$**



S. Ajimura *et al.* / Physics Letters B 789 (2019) 620–625

**J-PARC E27:  $d(\pi^+, K^+)\Sigma^0 p$**



# Structure of $K^-pp$

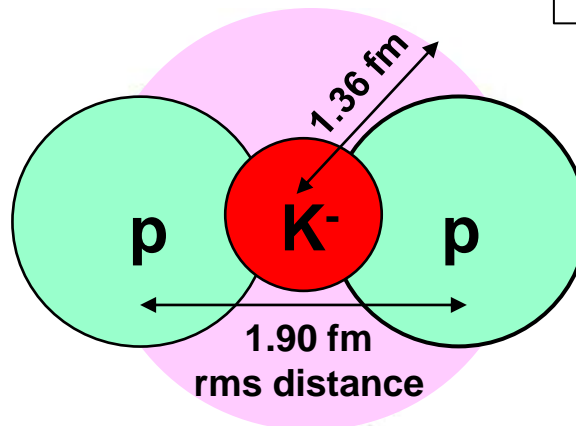
(Theoretical study)

赤石さんの  
スライドより

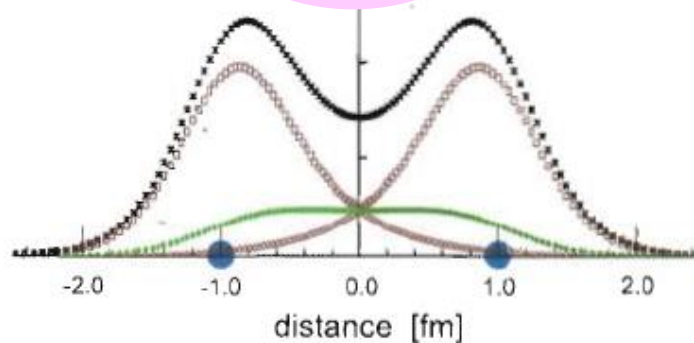
2002

Phys. Lett. B **535**  
(2002) 70

$K^-(pp)$



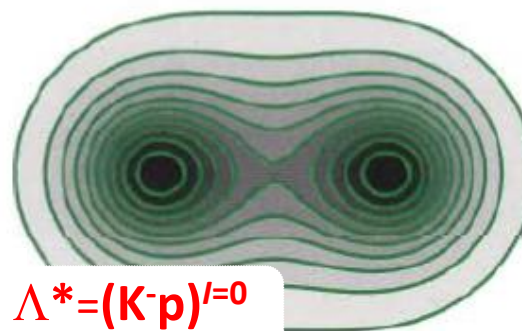
$(K^-p)-p$



2007

Phys. Rev. C **76**  
(2007) 045201

$\Lambda^*-p$  structure

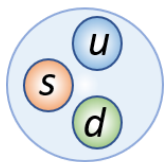


$\Lambda^* = (K^-p)^{I=0}$   
unit

with a few % covalent part

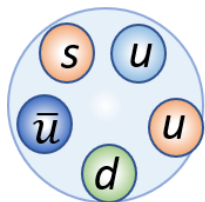
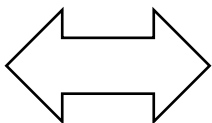
# Hierarchical structure

**$\Lambda(1405)$**

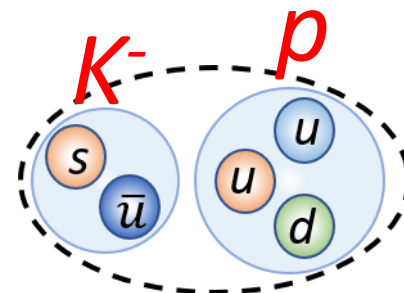
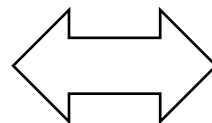


3 quarks

$$\Lambda(1405) = \Lambda^*$$



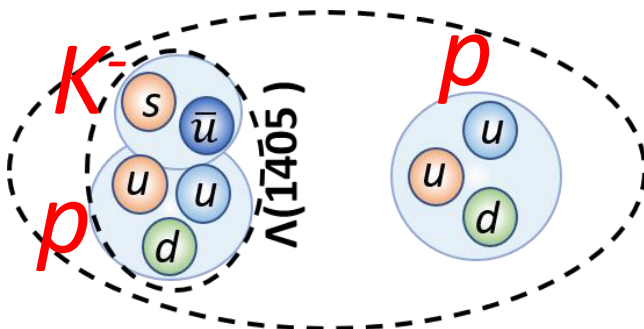
5 quarks



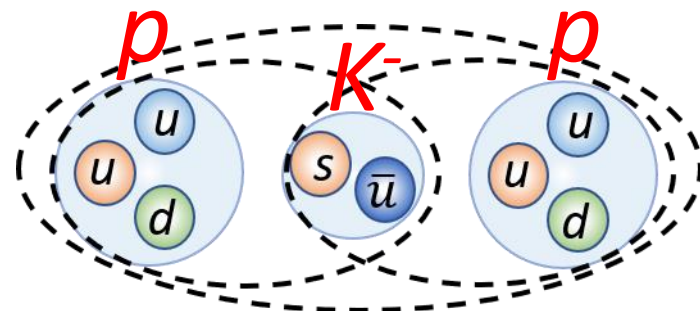
Meson – Baryon molecule

$$\Lambda(1405) = \bar{K} N + (\pi \Sigma + \dots)$$

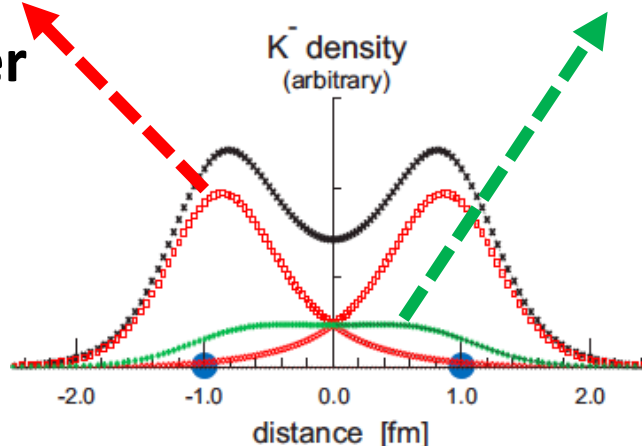
**$K^- pp$**



$\Lambda(1405)$ -Cluster



Field picture



# An event excess observed in the deeply bound region of $^{12}\text{C}(K^-, p)$ missing-mass spectrum

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# $\bar{K}$ nuclei in many body system

We have measured, for the first time, the inclusive missing-mass spectrum of the  $^{12}\text{C}(K^-, p)$  reaction at the incident kaon momentum of 1.8 GeV/c at the J-PARC K1.8 beamline. We observed a prominent quasi-elastic peak ( $K^-p \rightarrow K^-p$ ) in this spectrum. In the quasi-elastic peak region, the effect of secondary interaction is apparently observed as a peak shift, and the peak exhibits a tail in the bound region. We compared the spectrum with a theoretical calculation based on the Green's function method by assuming different values of parameters for the  $K$ -nucleus optical potential. We found

<https://doi.org/10.1093/ptep/ptaa139>

should mainly contribute. The enhancement is well fitted by a Breit-Wigner function with a kaon-binding energy of 90 MeV and width of 100 MeV. A possible interpretation is a deeply bound state of a  $Y^*$ -nucleus system.



# $\bar{K}$ -A interaction

An important tool is **kaonic atoms**.

- Simple tp approach

$$[\Delta - 2\mu(B + V_{opt} + V_c) + (V_c + B)^2]\Psi = 0,$$

$$2\mu V_{opt}(r) = -4\pi \left(1 + \frac{\mu}{m} \frac{A-1}{A}\right) b_0 \rho(r)$$

$$b_0 \rightarrow b_0 + B_0[\rho(r)/\rho_0]$$

$$\text{Re}(V_0) \sim -80 \text{ MeV}$$

- Chiral motivated model

$$\text{Re}(V_0) \leq -60 \text{ MeV}$$

- DD(Density dependent) potential

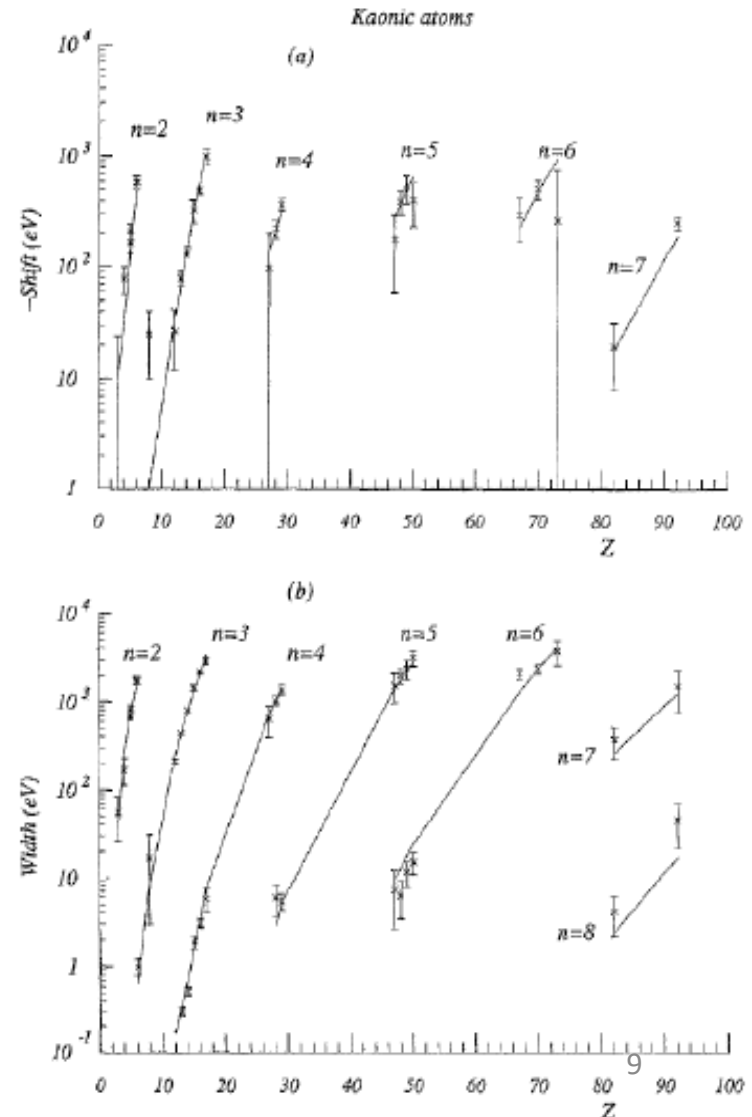
$$\text{Re}(V_0) = -(150-200) \text{ MeV}$$

- Fourier-Bessel method

$$\text{Re}(V_0) \sim -(170) \text{ MeV}$$

- IHW  $K^{\text{bar}}$ N interaction+phenomenological multi-nucleon absorption

$$\text{Re}(V_0) \sim -(170) \text{ MeV}$$



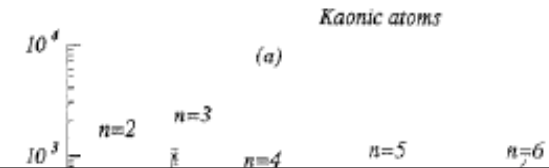
# $\bar{K}$ -A interaction

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$$2\mu V_{opt}(r) = -4\pi \left(1 + \frac{\mu}{m} \frac{A-1}{A}\right) b_0 \rho(r)$$



The depth of  $\bar{K}$ -nucleus potential **strongly depends** on the **model setting**. It is **not conclusive** whether  $\bar{K}$ -nucleus potential is “**deep**” or “**shallow**”!! Both type of potential can reproduce the kaonic atoms data.

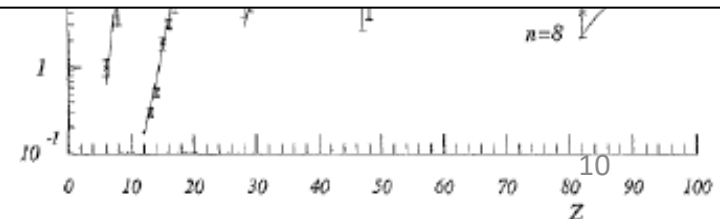


To solve this problem,

**a new experimental constraint is necessary!**

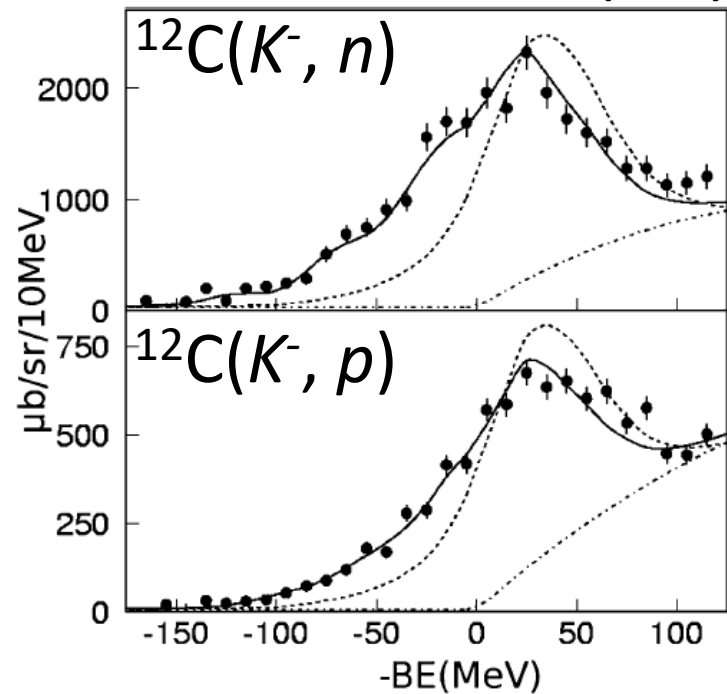
- IHW  $K^{\text{bar}}N$  interaction+phenomenological multi-nucleon absorption

$$\text{Re}(V_0) \sim -(170) \text{ MeV}$$



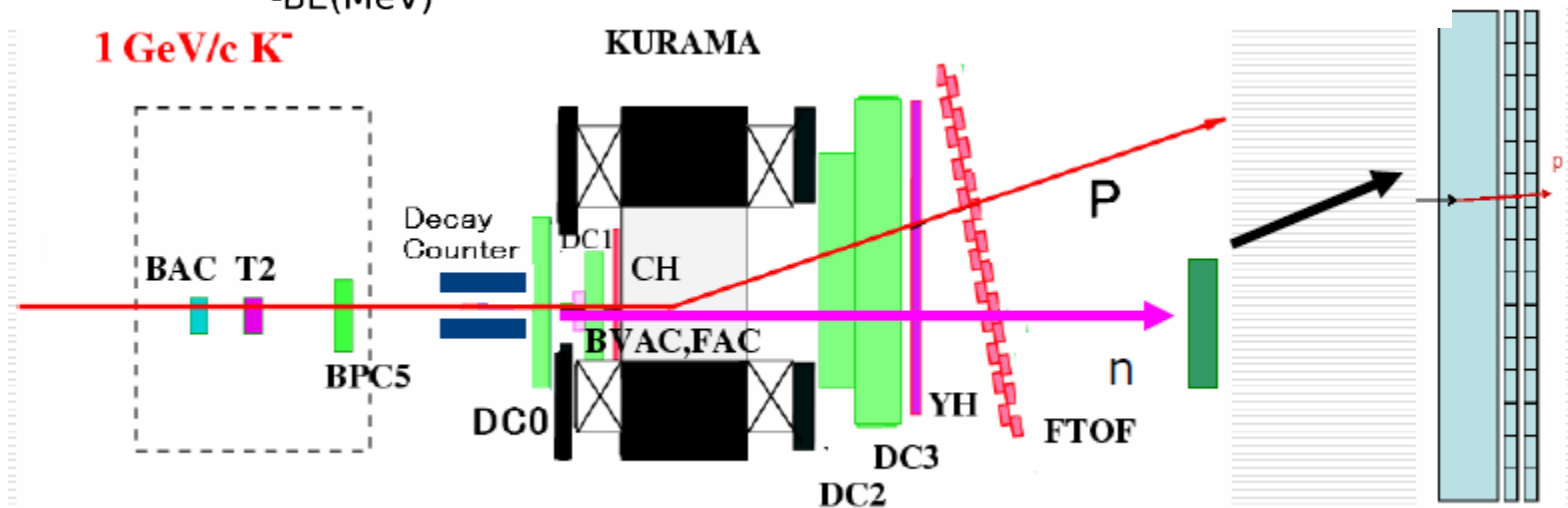
# Past experiment: KEK E548 [ $^{12}\text{C}(K^-, N)$ ]

T. Kishimoto et al., PTP 118, 1 (2007).



- $^{12}\text{C}(K^-, n)$ ,  $^{12}\text{C}(K^-, p)$  at 1 GeV/c
  - $K^-$  beam:  $10^4/\text{spill}$
  - KEK-PS K2 beamline + KURAMA
  - MM resolution  $\sim 10 \text{ MeV } (\sigma)$
  - $\theta_{sc} < 4.1^\circ$  was chosen
- $V_{\text{opt}}$  was studied comparing DWIA
  - $C(K^-, n)$ :  $V_{\text{opt}} = (V_0: -190, W_0: -40) \text{ MeV}$
  - $C(K^-, p)$ :  $V_{\text{opt}} = (V_0: -160, W_0: -50) \text{ MeV}$

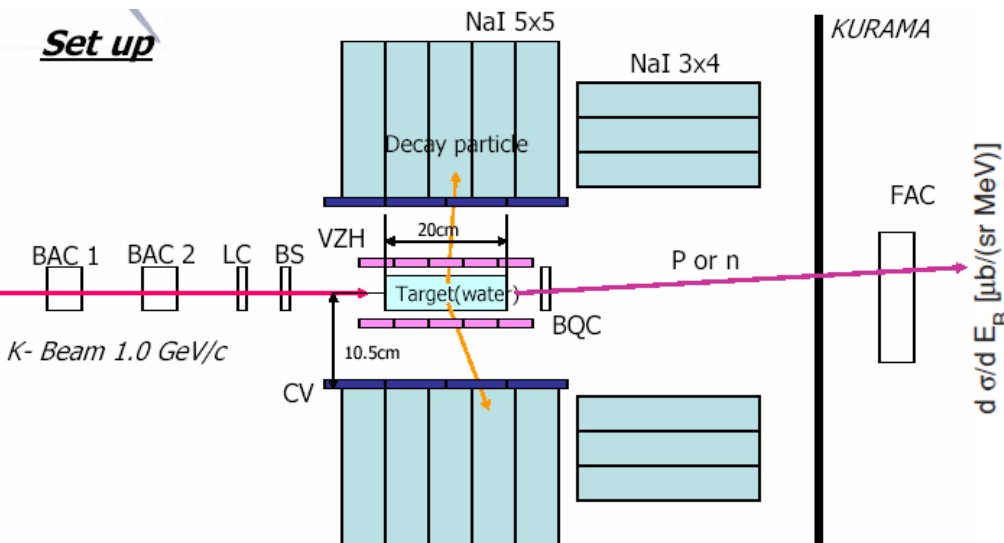
(dotted line:  $V_{\text{opt}} = (V_0: -60, W_0: -60) \text{ MeV}$ )



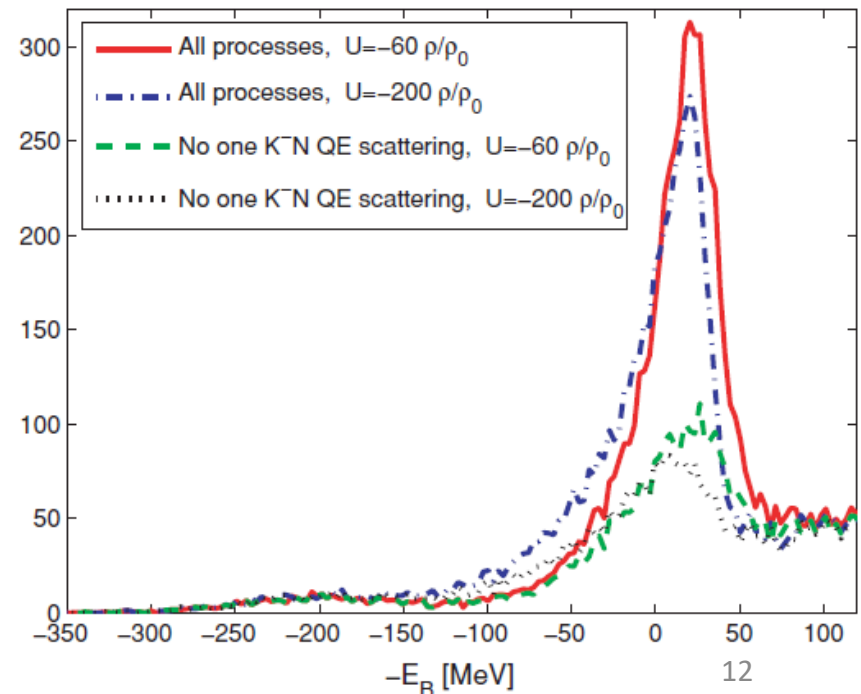
# Discussion for KEK E548

- V. K. Magas *et al.*, pointed out a serious drawback in this experimental setup.
  - In E548, at least one charged particle detected by their decay counter was required (**semi-inclusive spectrum**).

**Semi-inclusive spectra doesn't have enough sensitivity !!**



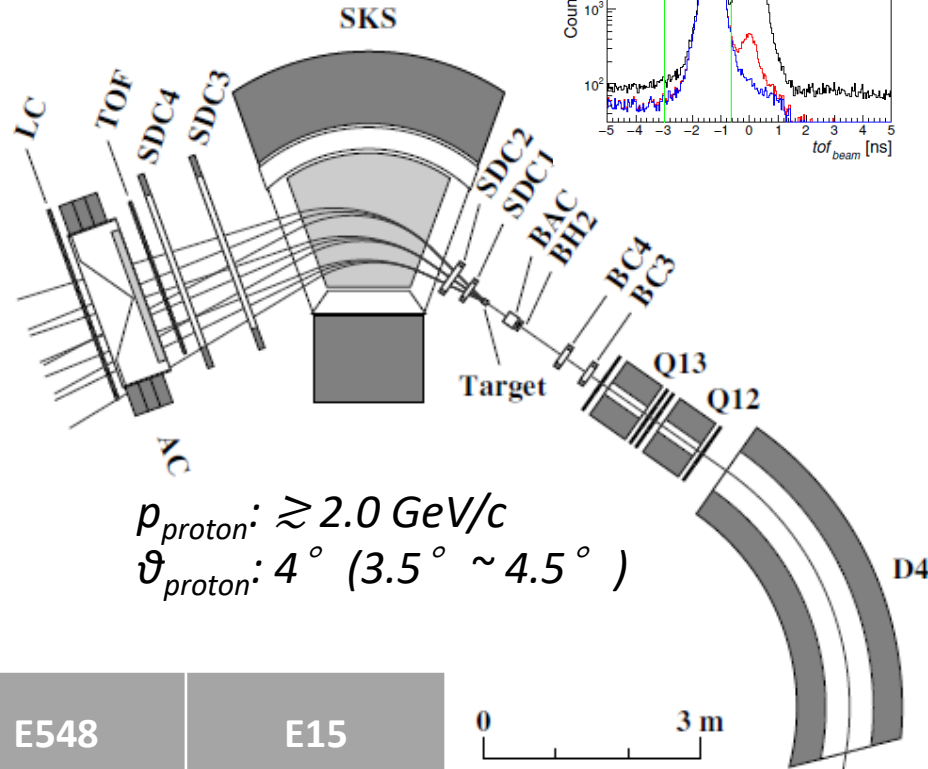
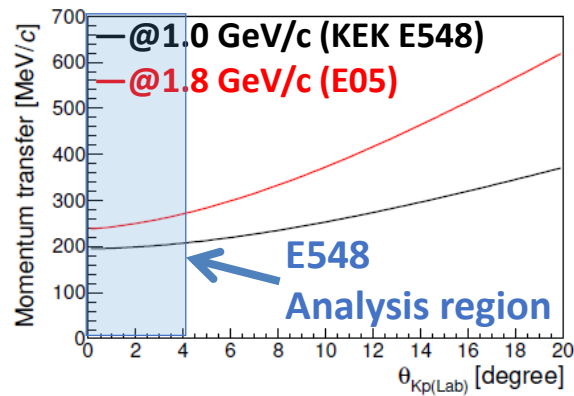
V. K. Magas *et al.*, PRC 81, 024609 (2010).



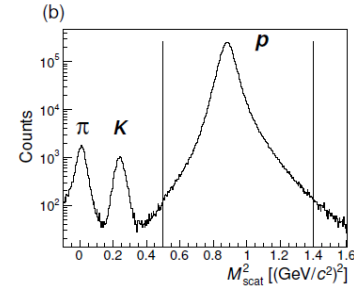
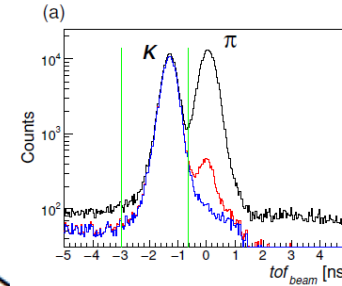
# J-PARC E05 [ $^{12}\text{C}(\text{K}^-, \text{p})$ @1.8 GeV/c]

## *Inclusive measurement*

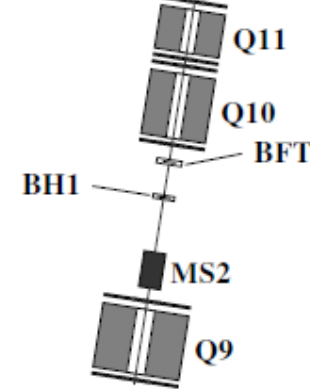
Momentum transfer  
for  $Kp$  elastic scattering



$p_{\text{proton}}: \gtrsim 2.0 \text{ GeV/c}$   
 $\vartheta_{\text{proton}}: 4^\circ (3.5^\circ \sim 4.5^\circ)$

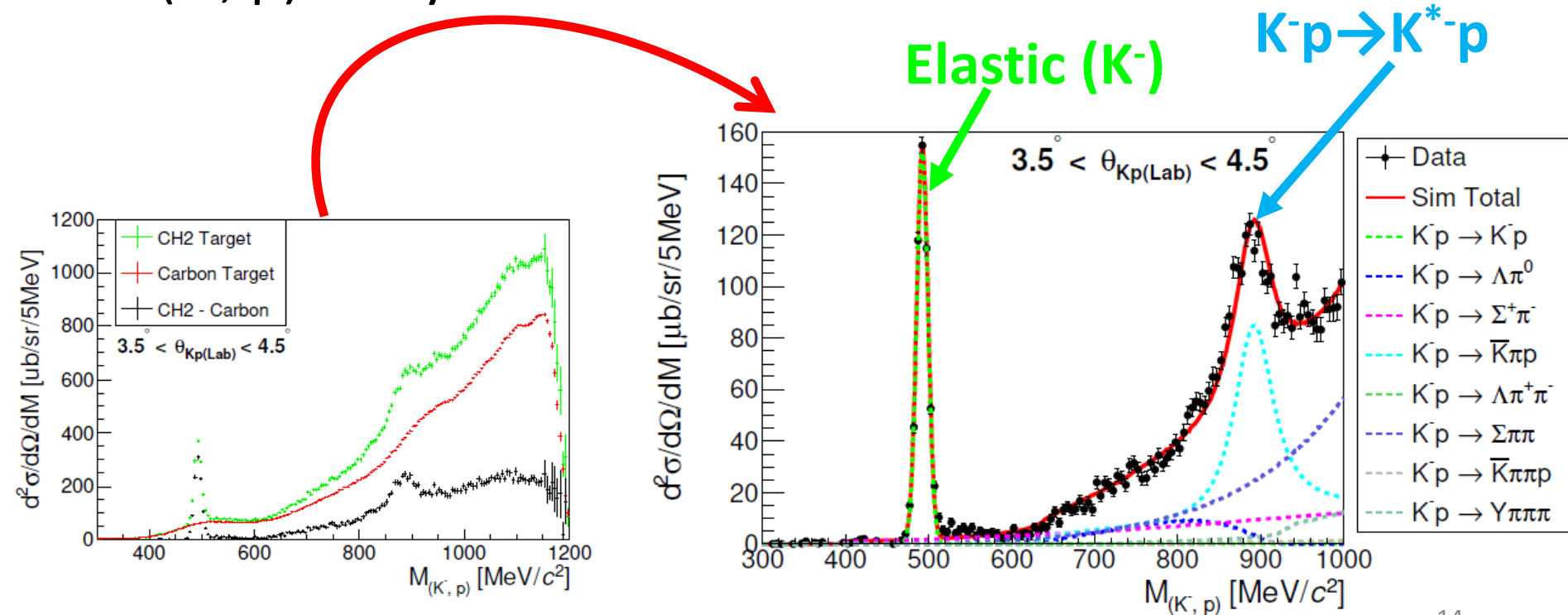


( $\text{K}^-$ , N) data	E05	E548	E15
$p_{\text{K}^-}$ [GeV/c]	1.8	1.0	1.0
Reaction	$^{12}\text{C}(\text{K}^-, \text{p})$	$^{12}\text{C}(\text{K}^-, \text{p/n})\text{x}$	$^3\text{He}(\text{K}^-, \text{n})\text{x}$
$\sigma_{\text{M}}$ [MeV]	4.2	10	10



# Calibration: $p(K^-, p)$ @1.8 GeV/c

- We obtained the reasonable solution by the template fit.
  - Each yield was free parameter
  - Resonance productions via  $K^*(K^-p \rightarrow K^{*-}p)$ ,  $\Delta$ ,  $Y^*$  are included.
- We fixed the “p”-target component in  $^{12}\text{C}$  for the  $^{12}\text{C}(K^-, p)$  analysis.



# $^{12}\text{C}(\text{K}^-, p)$ spectrum ( $V_0, W_0 = (0, 0)$ )

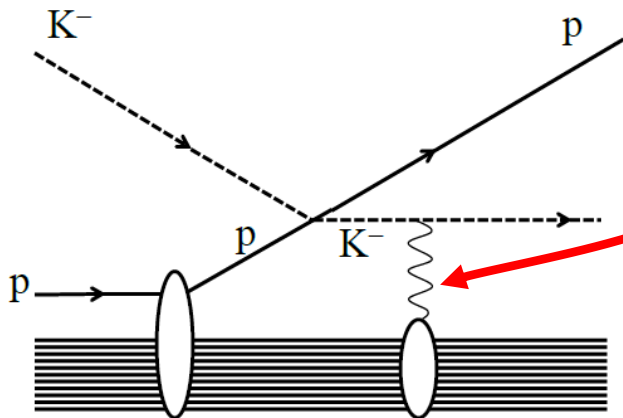
- Interesting component
  - ---  $\text{K}^-p$  (QF-Elastic): Calculated by DWIA( $V_0, W_0 = (0, 0)$ )
- Background
  - ---  $\text{K}^-p$  (QF-InElastic): Monte-Carlo simulation based on  $p(\text{K}^-, p)$  analysis
  - $\text{K}^-n \rightarrow X$  (QF) : Monte-Carlo simulation, Yield: free parameters

$$\left( \frac{d^2\sigma}{d\Omega dE} \right)_A^{\text{lab}} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{ele}}^{\text{lab}} \times S(E) \quad .$$

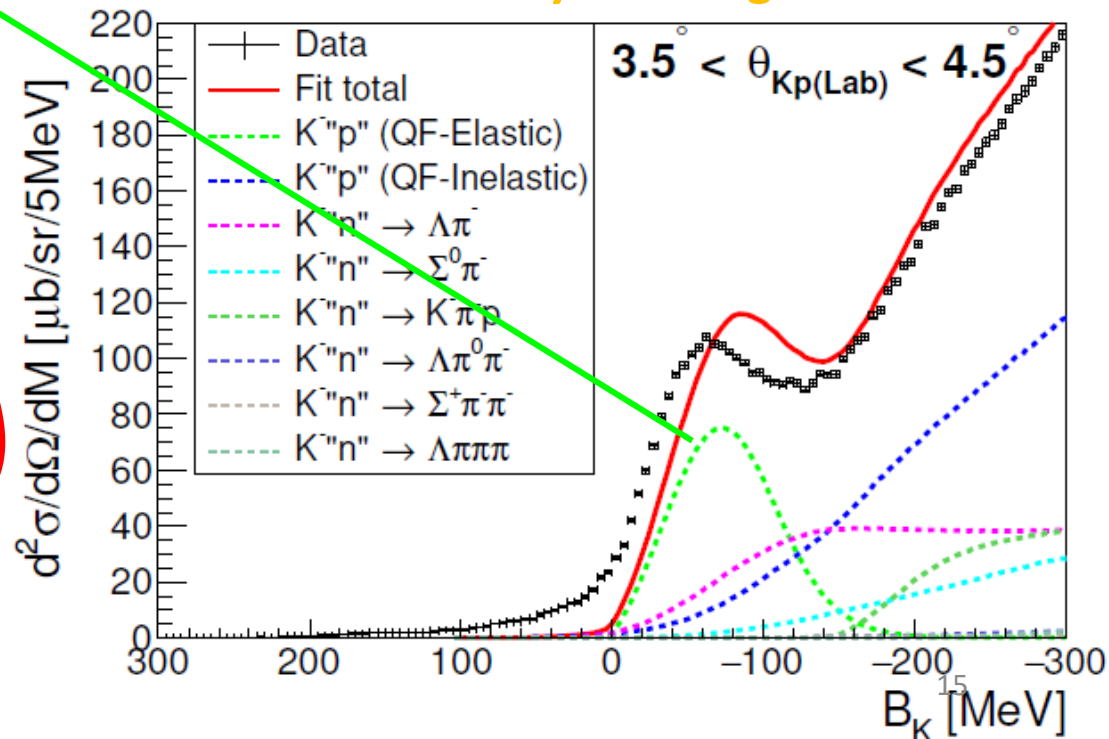
$$S(E) = -\frac{1}{\pi} \text{Im} \sum_f K \int dr dr' \tau_f^\dagger(r) G(E; r, r') \tau_f(r'),$$

$$G(E, r, r') = \left\langle p^{-1} \left| \phi_K(r) \frac{1}{E - H_K + i\epsilon} \phi^\dagger(r') \right| p^{-1} \right\rangle ,$$

$$U(r, E) = (V_0 + iW_0 f_{\text{phase}}(E)) \frac{\rho(r)}{\rho(0)} ,$$

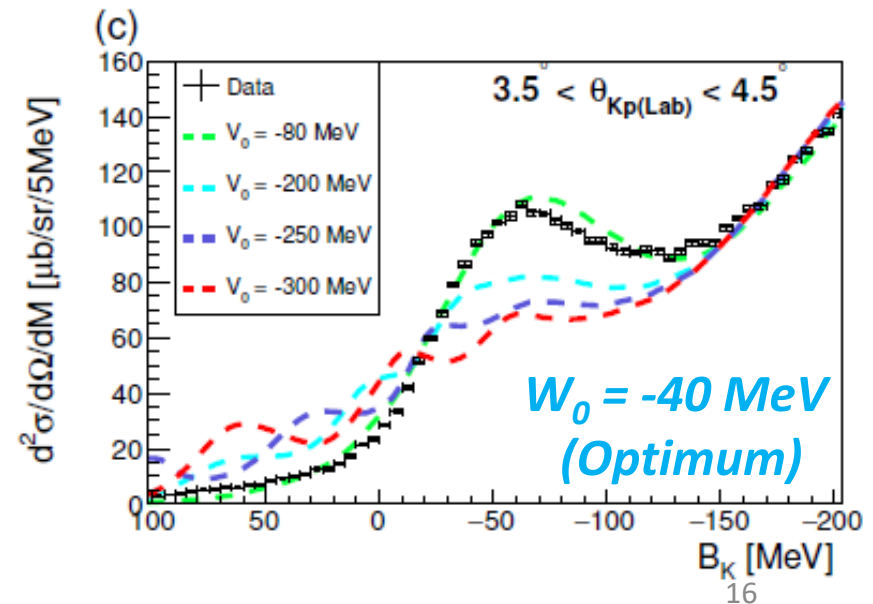
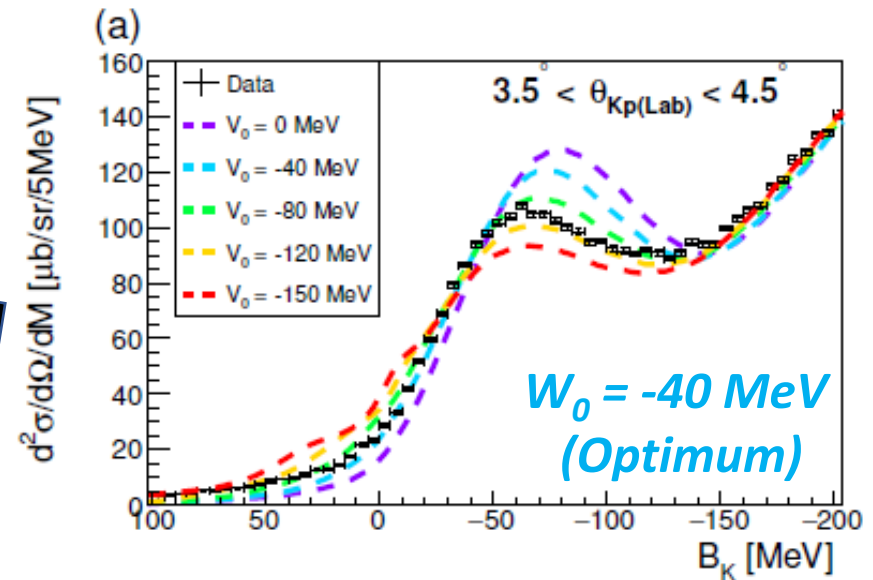
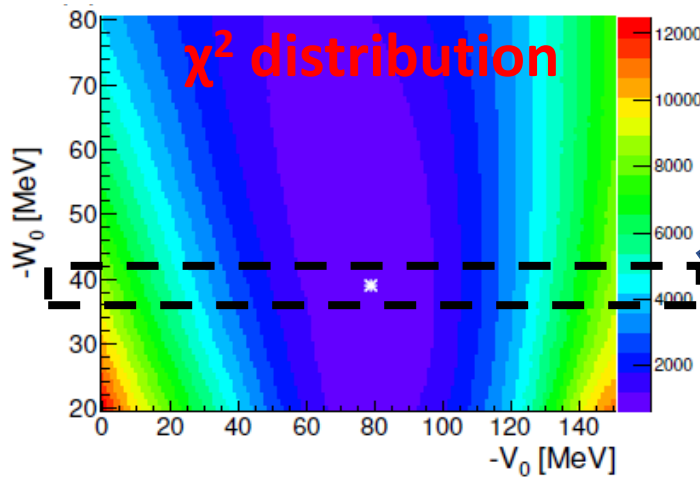


DWIA: Calculated by J. Yamagata-Sekihara.

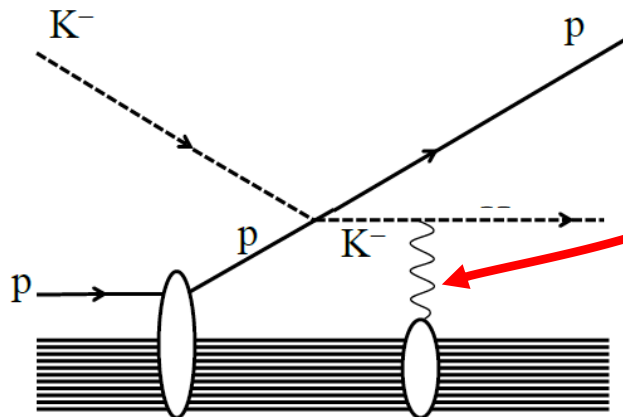


# Comparison by change ( $V_0$ , $W_0$ )

**Optimum:  $(V_0, W_0) = (-80, -40)$  MeV!**  
**Corresponding to shallow potential**



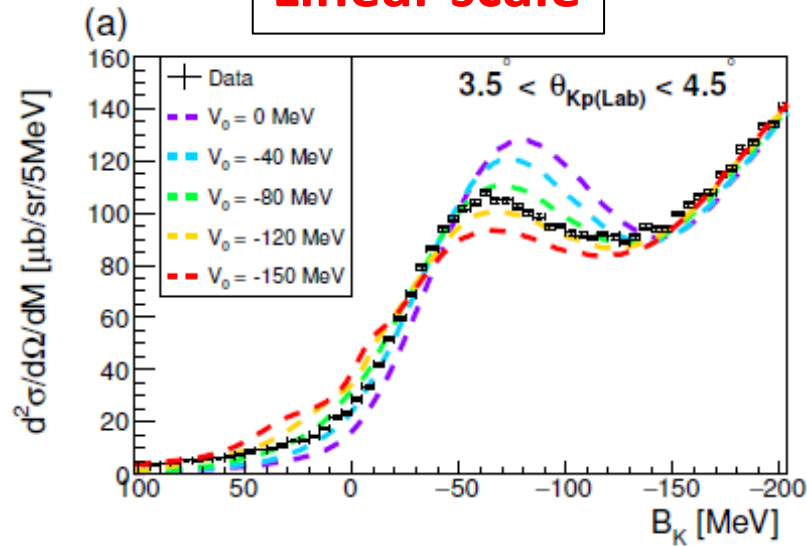
$$U(r, E) = (V_0 + iW_0 f_{\text{phase}}(E)) \frac{\rho(r)}{\rho(0)},$$



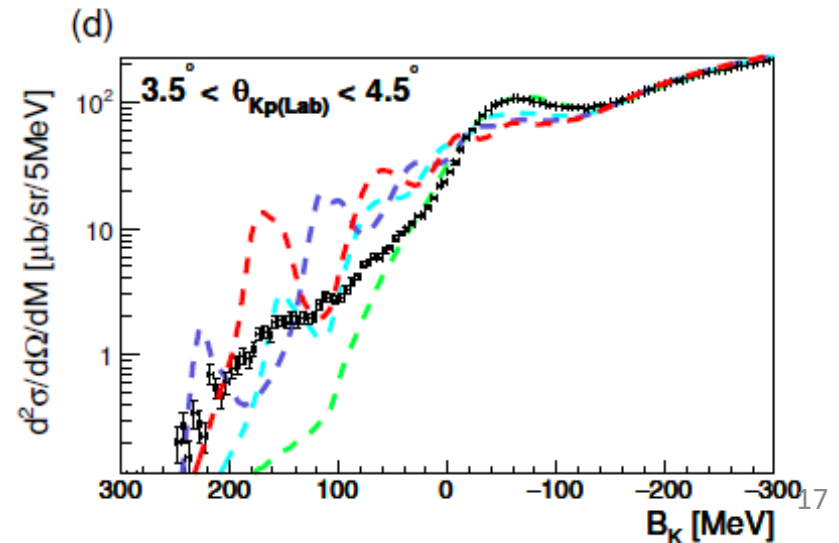
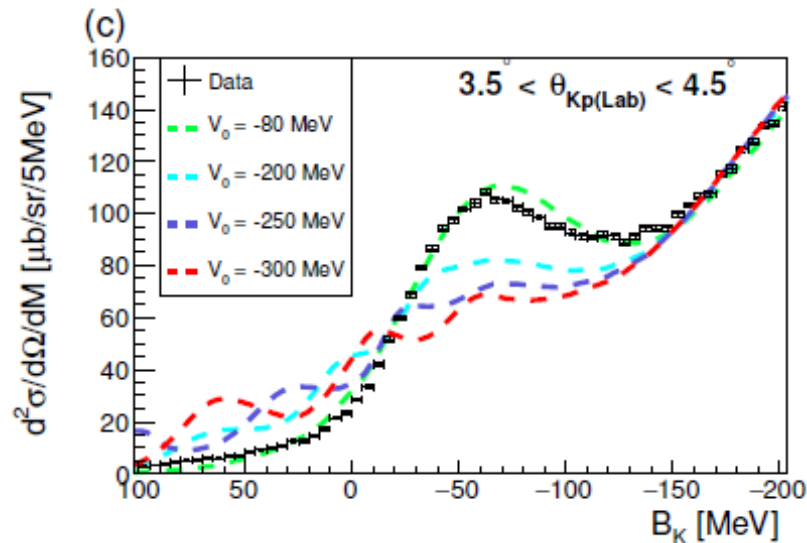
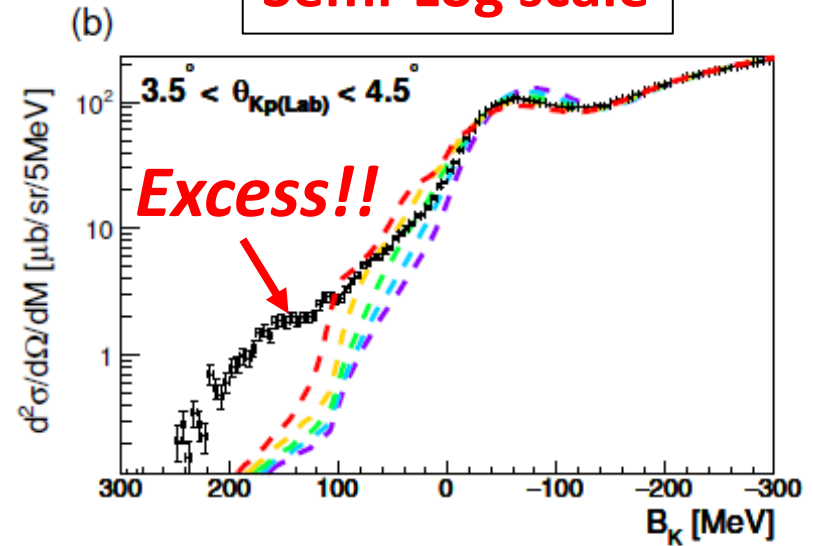


# Event Excess

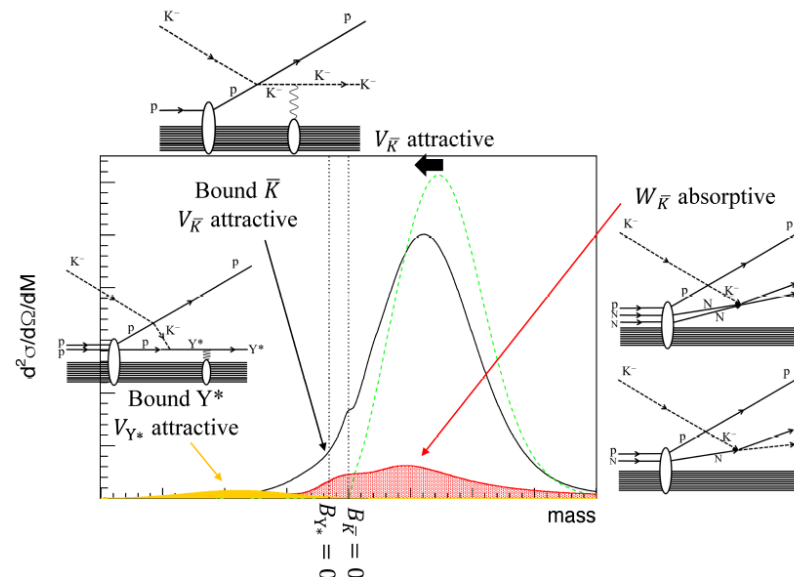
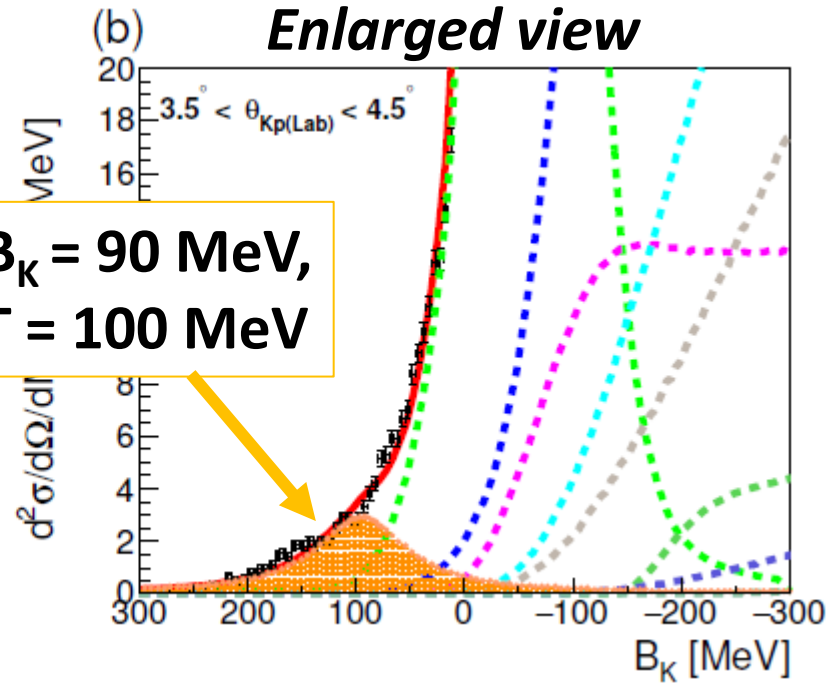
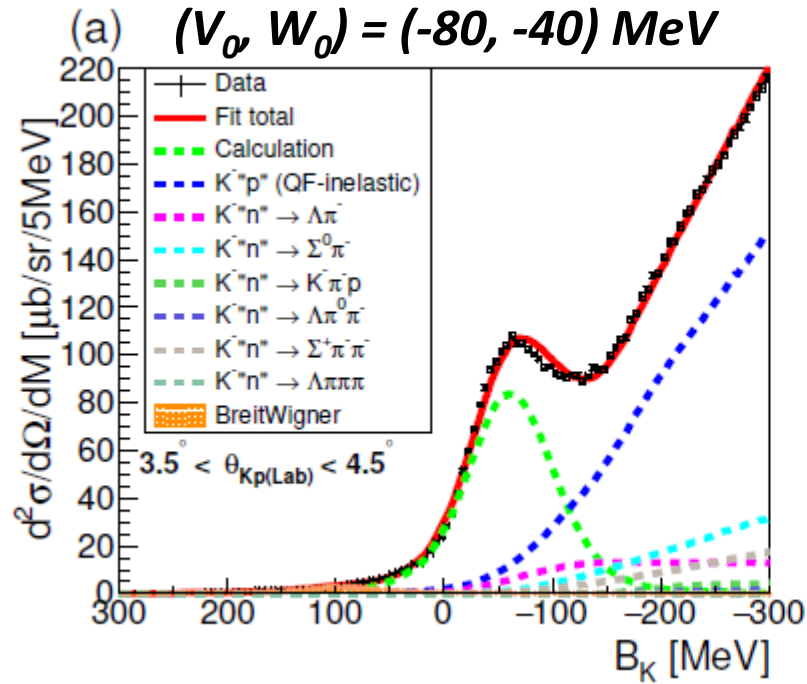
Linear scale



Semi-Log scale

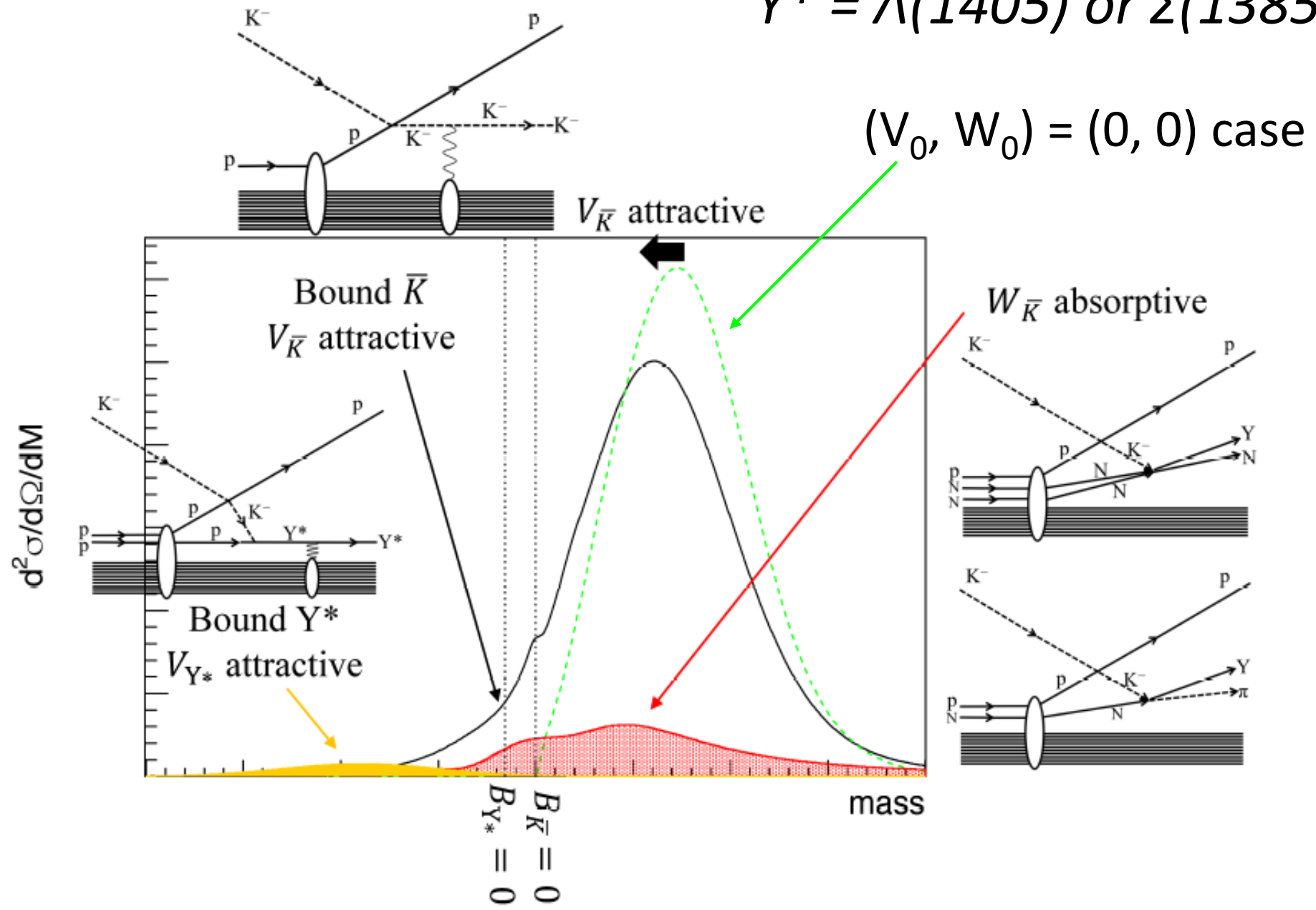


# Event Excess: Fitted by BW ( $Y^*$ -nucleus?)



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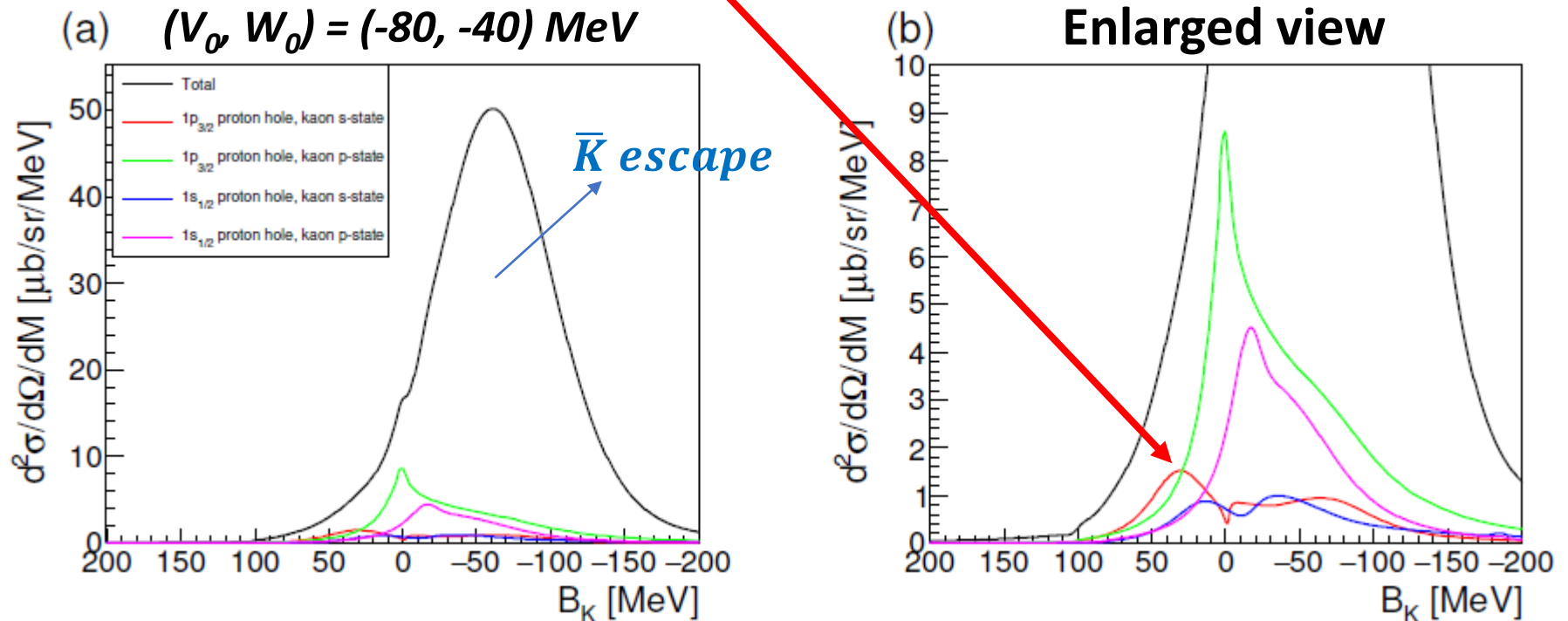
$Y^* = \Lambda(1405) \text{ or } \Sigma(1385)$



# Kaonic nuclear state (Decomposed theoretical spectrum)

*proton-hole:  $1p_{3/2}$ ,  $\bar{K}$  : s-state*

*Kaonic nuclear state:  $B_K = 31 \text{ MeV}$ ,  $\Gamma = 53 \text{ MeV}$*



# Discussion: Relationship with kaonic-atom X-rays

*E. Friedman, A. Gal / Nuclear Physics A 899 (2013) 60–75*

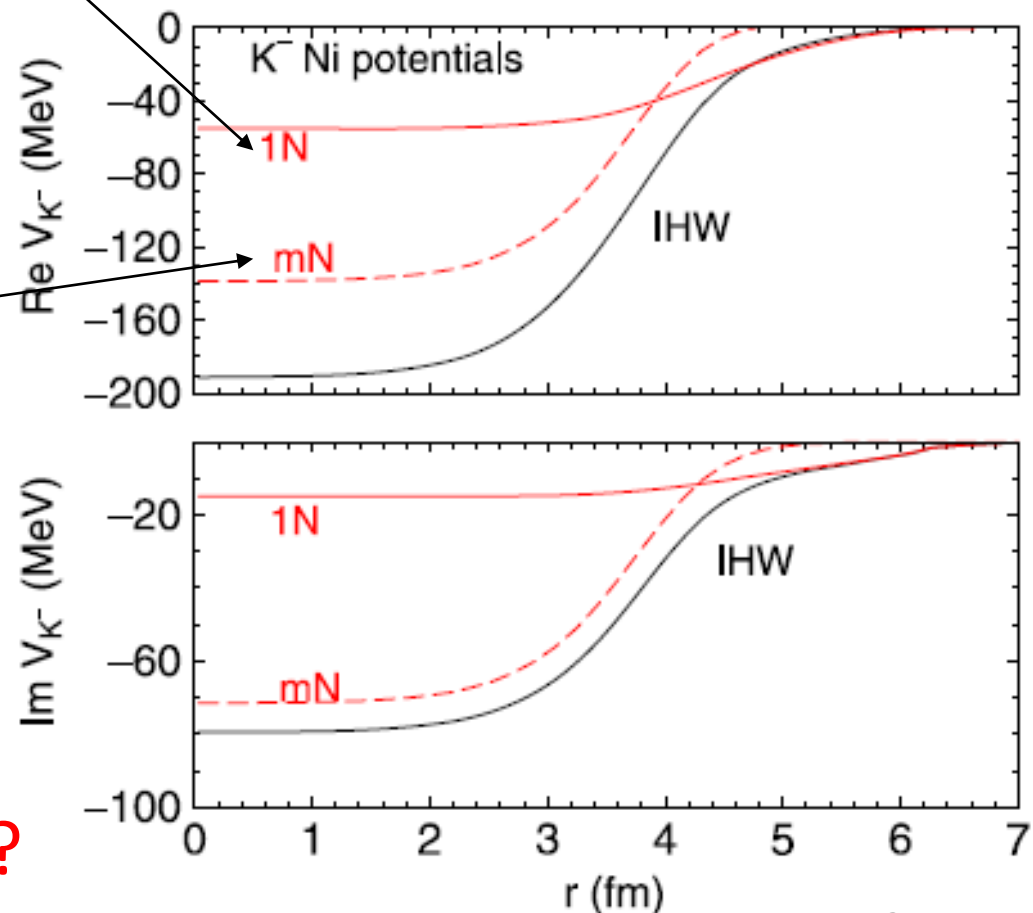
$$V_{K^-} = V_{K^-}^{(1)} + V_{K^-}^{(2)}$$

$V_K^{(1)}$ : 1N absorption term  
derived by IHW NLO  
chiral K-N scattering amplitude

$V_K^{(2)}$ : mN absorption term  
Phenomenological potential  
(fitted by X-ray data)

For the deep  $V_K^{(2)}$  potential,  
Y\* doorway process as  
 $K^-p \rightarrow Y^*$ ,  $Y^*n \rightarrow \Lambda n$   
should play an important role!!

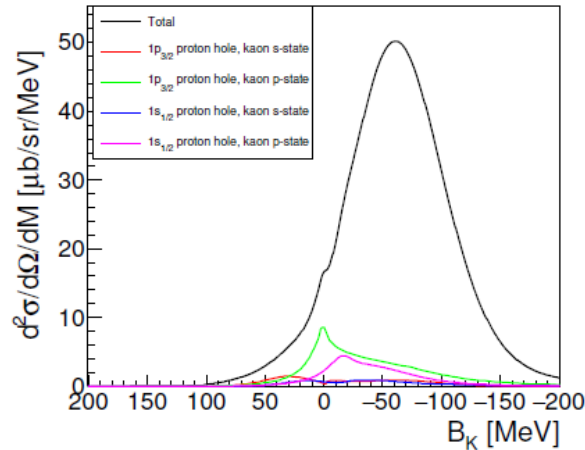
$V_K^{(2)}$  corresponding to  $V_{Y^*}$ ?



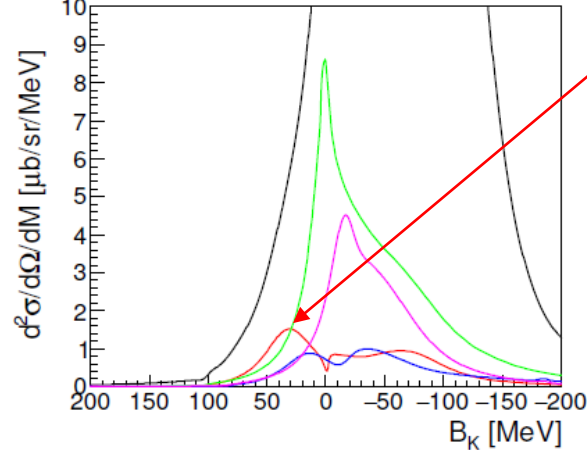
# Outlook

# Exclusive measurement (Motivation)

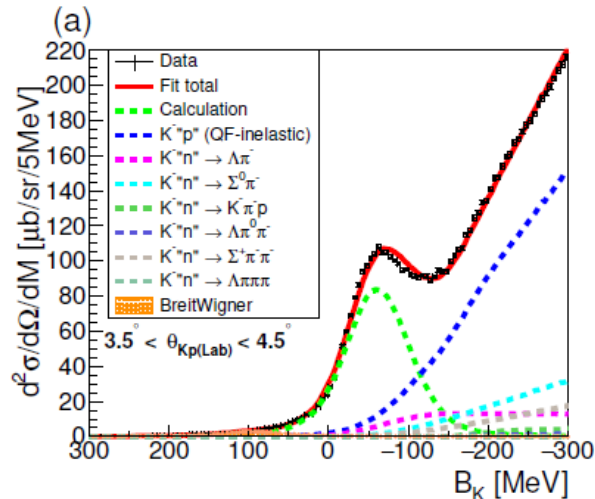
(a)  $(V_0, W_0) = (-80, -40) \text{ MeV}$



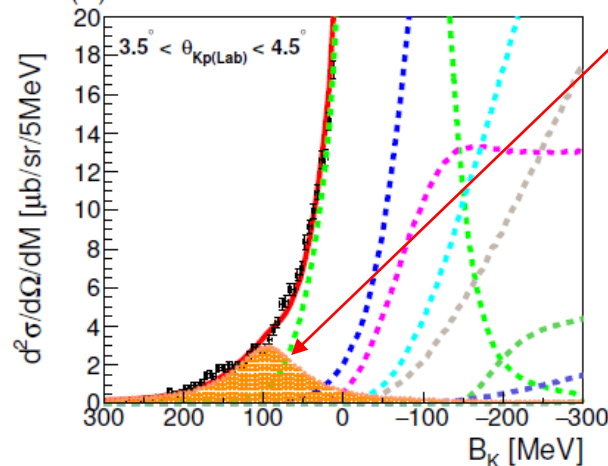
(b) Enlarged view



Motivation:  
To observe the 1s state  
as a distinct peak!  
Method:  
 $^{12}\text{C}(\text{K}^-, \text{p})\Sigma\pi\text{p}$   
measurement(?)



(b) Enlarged view



Motivation:  
To observe the excess  
as a distinct peak!  
Method:  
 $^{12}\text{C}(\text{K}^-, \text{p})\Lambda\text{p}$   
measurement(?)

# Conversion spectrum

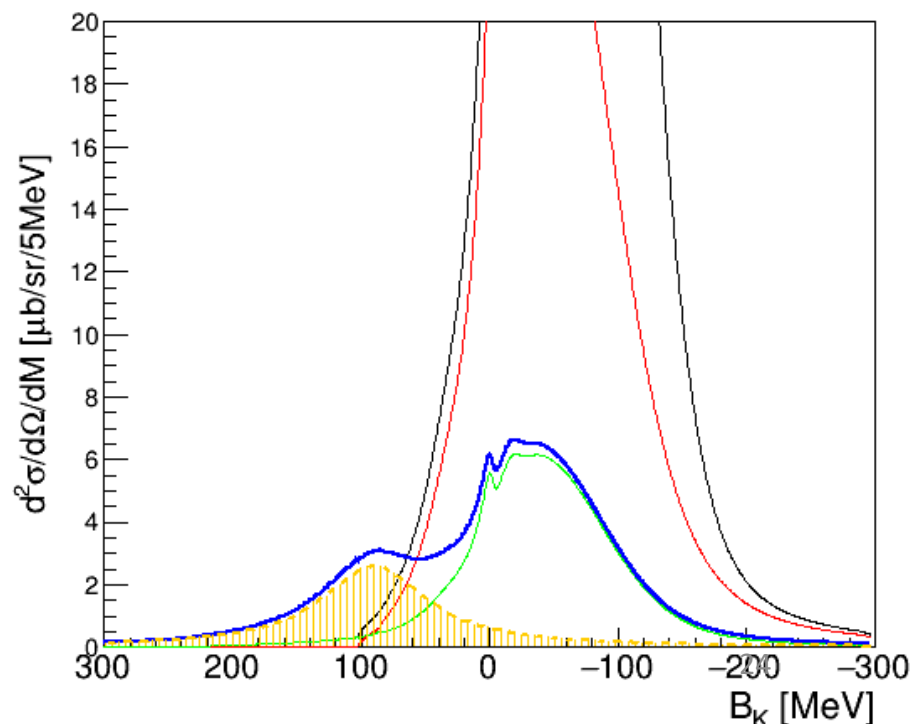
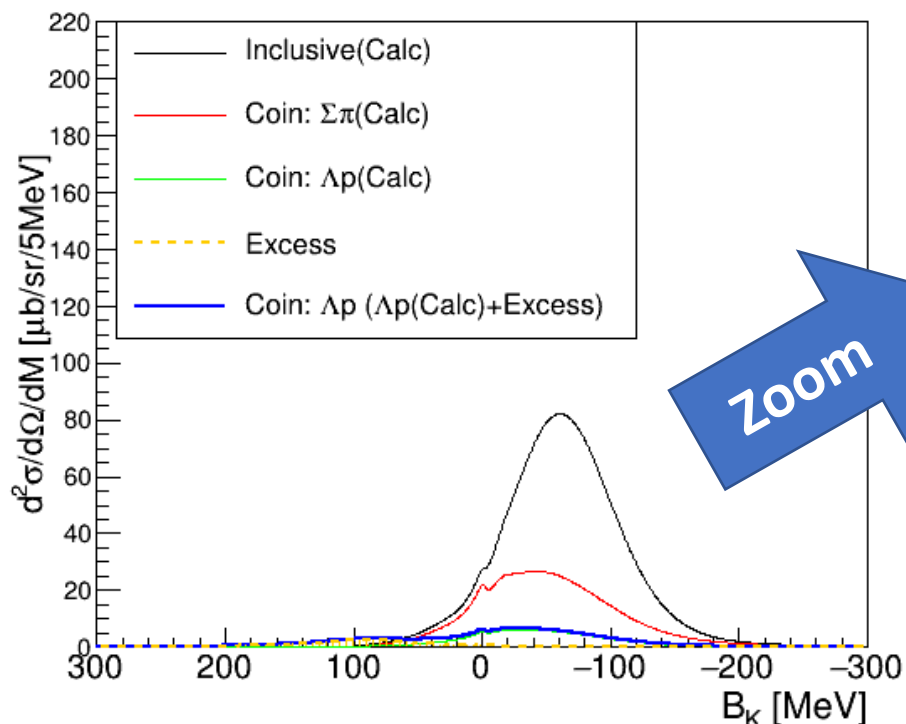
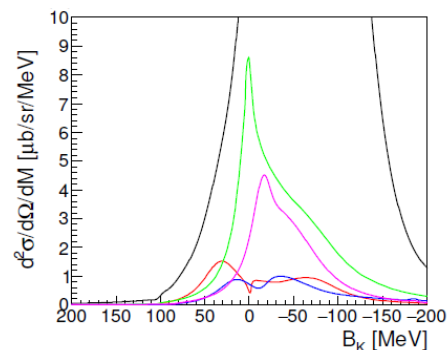
Difficult to see the 1s peak by One body abs. ( $^{12}\text{C}(\text{K}^-, \text{p})\Sigma\pi$ ).  
The one of the possible channel is  $^{12}\text{C}(\text{K}^-, \text{p})\Sigma\pi\text{p}$ .

$^{12}\text{C}(\text{K}^-, \text{p})\Lambda\text{p}$  probability is low.

→ Possibility to see the  $\text{Y}^*$ -nucleus state.

$$(V_0, W_0) = (-80, -40) \text{ MeV}$$

*Calculated by J. Yamagata-Sekihara.*





# Beyond E05 = E42 (H-dibaryon search)

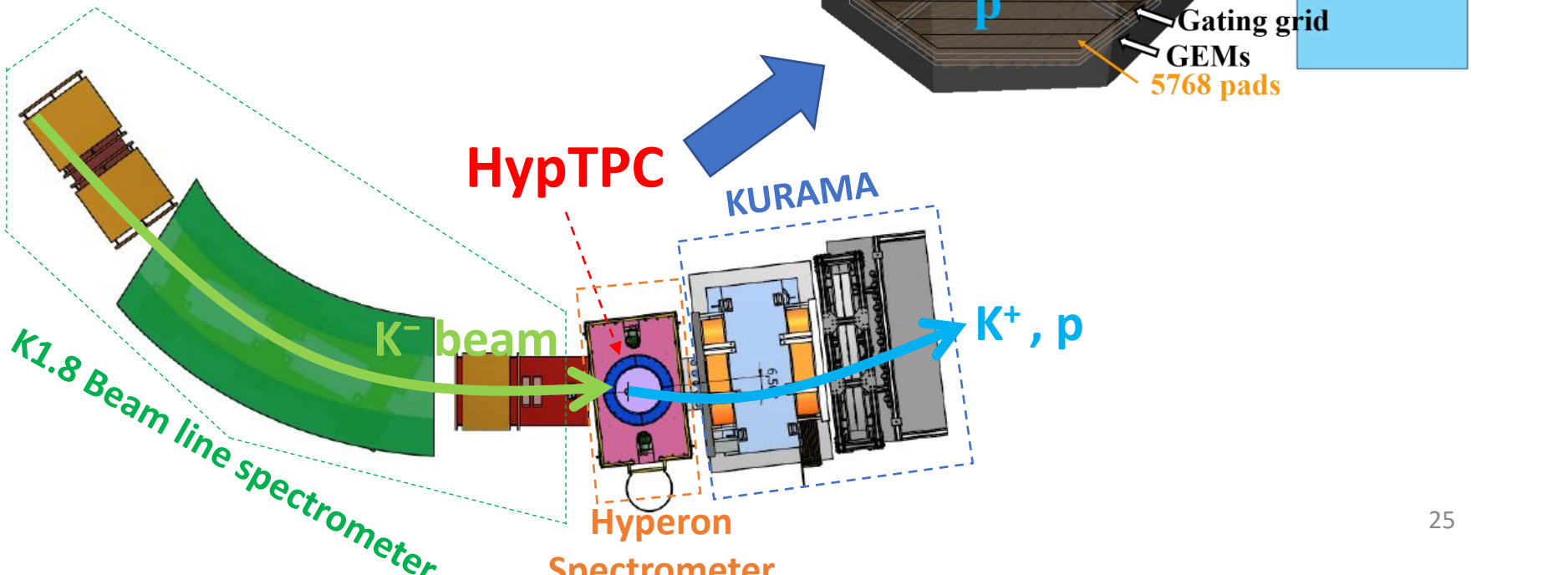
Outgoing proton: KURAMA

Decay particle: **HypTPC**

$\Lambda p$ : measured by  $p, \pi^-, p$

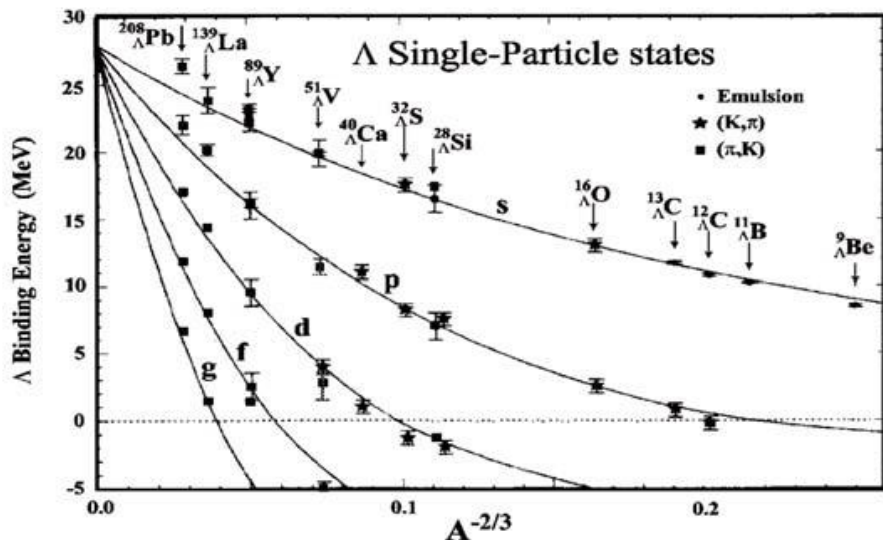
$\Sigma \pi p$ : identified by  $\pi^\pm \pi^\pm p$

E42 experiment: *Spring of 2021*



# Further ( $K^-$ , p) study: A-dependence

In case of  $\Lambda$  hypernucleus,  
we can see the clear single-particle states.  
(Described by single-particle potential)



**Measurement  
of the ( $K^-$ , p)  
A-dependence**

How about the Kaonic ( $Y^*$ ) nucleus?  
Can we see the shell structures?

→ Key points

- Hierarchical structures
- $\bar{K}N$  sigma term

# Summary

- We have measured the inclusive  $^{12}\text{C}(\text{K}^-, \text{p})$  spectrum at J-PARC (J-PARC E05 byproduct).
- $(V_0, W_0) = (-80, -40)$  MeV, corresponding to shallow potential, well reproduced the measured spectrum.
  - This potential contains the  $B_K \sim 30$  MeV Kaonic bound state.
- We also have found the significant event excess, which can be interpret as a  $Y^*$ -nucleus state, around  $B_K \sim 100$  MeV.
- Outlook
  - Coincidence measurement: E42
    - Decay charged particles will be measured by using the HypTPC.
    - $^{12}\text{C}(\text{K}^-, \text{p})\Lambda\text{p}$  reaction is promising to confirm the event excess.
  - Systematic study (A-dependence) will tell us the exotic property of the K-nucleus.