



2022/11/03

International Symposium on Clustering as a Window on the Hierarchical  
Structure of Quantum Systems (CLUSHIQ2022)



# Study of three nucleon force via proton- ${}^3\text{He}$ scattering

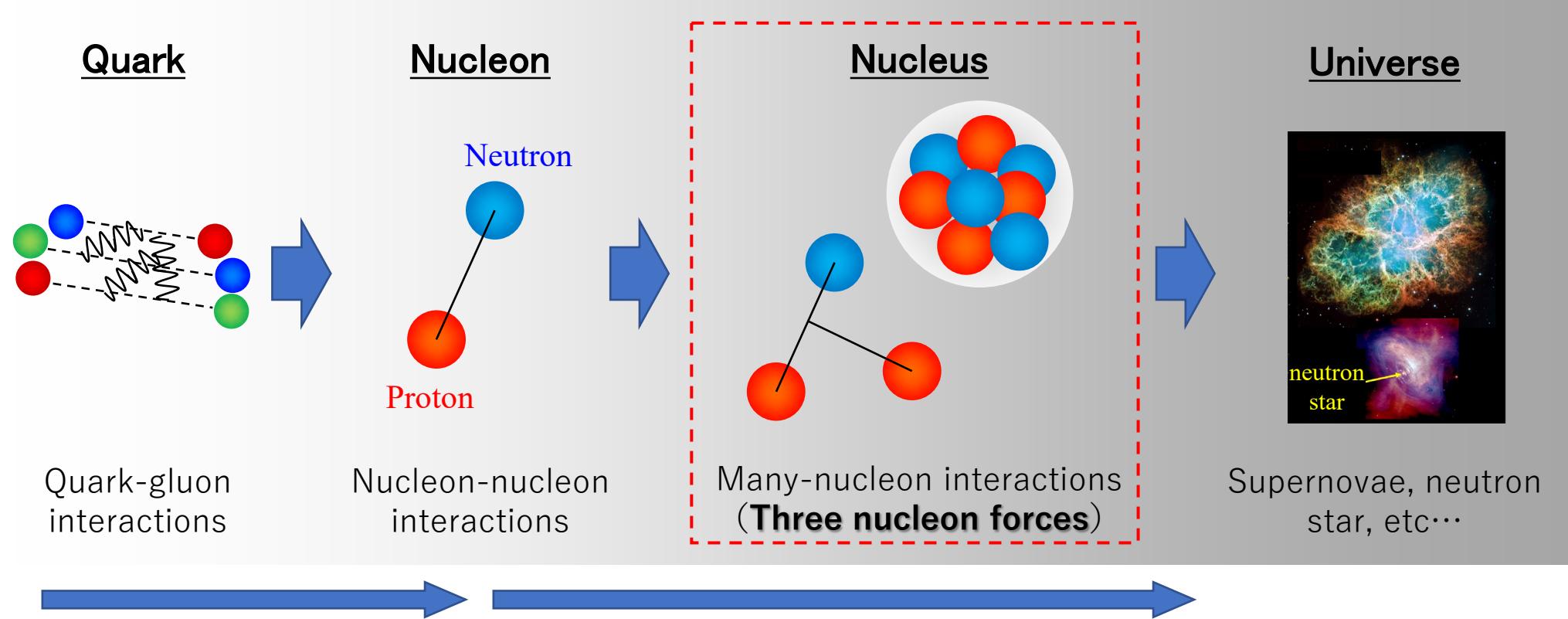
- 
- 1. Introduction
  - 2. Measurement of  $p-{}^3\text{He}$  Scattering
  - 3. Experimental Results
  - 4. Future Plan
  - 5. Summary

Tokyo Institute of Technology,

Department of physics

**Atomu Watanabe**

# Study of Nuclear Forces –*from quark to universe*–



*Consistent understanding from quarks to the universe*

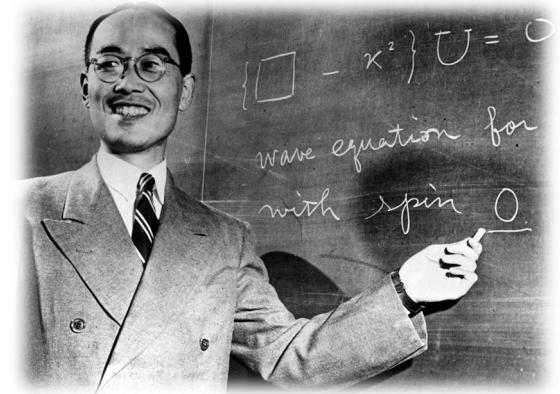
# 2 & 3 Nucleon Force

## Theoretical Description of Nucleon-Nucleon (NN) Force

1935 **Meson exchange picture** by H. Yukawa Proc. Phys. Math. Soc. Jpn **17**, 48.

1990's **Realistic NN potentials**

→ precisely reproduce 3000–4000 NN scattering data ( $\chi^2/\text{datum} \sim 1$ )



Hideki Yukawa

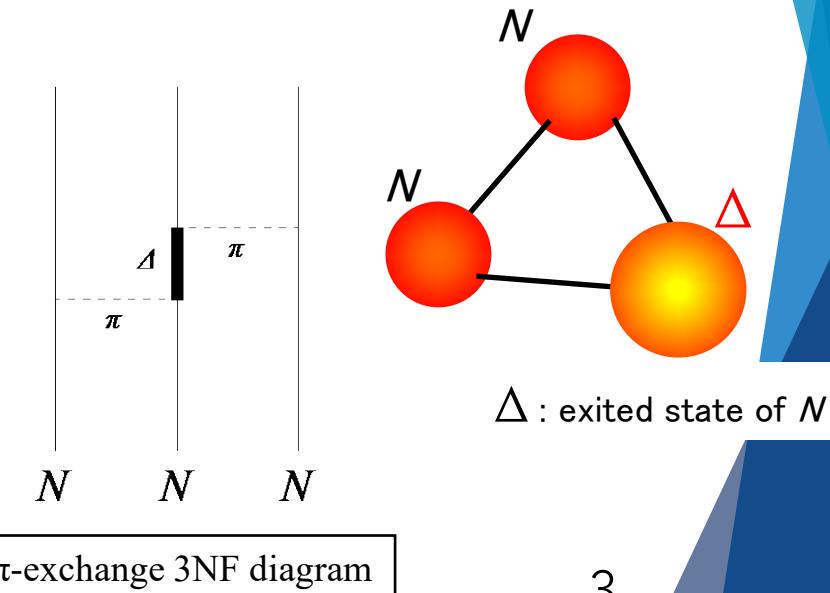
## Three-Nucleon Force (3NF)

First theoretical insight by Fujita & Miyazawa →  **$2\pi$ -exchange 3NF**

Prog. Theor. Phys. **17**, 360 (1957).

- ✓  $\Delta$ -isobar excitation in the intermediate state.
- ✓ 3NFs play important roles in various nuclear properties (e.g., few-nucleon scattering, B.E. of light nuclei, and nuclear matter).

*3NF is a key to understand nuclear phenomena*



# Few-Nucleon Scattering

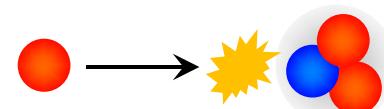
A **good probe** to study the dynamical aspects of 3NFs.

- ✓ Momentum dependence
- ✓ Spin & Iso-spin dependence



↳ **Theory** : Faddeev (-Yakubovsky) eq., etc...

Rigorous numerical calc. for 3, 4N system  
with 2NF, 3NF inputs



↳ **Exp.** : Precise Data

Cross section, Spin observables ( $A_i$ ,  $C_{ij}$ ,  $K_{ij}$ )

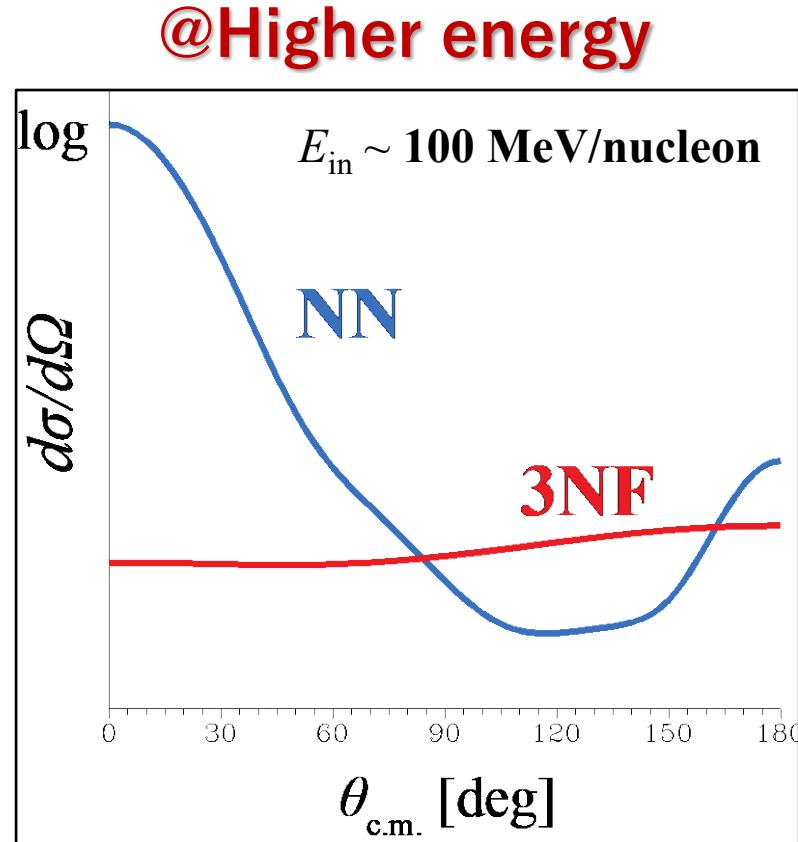
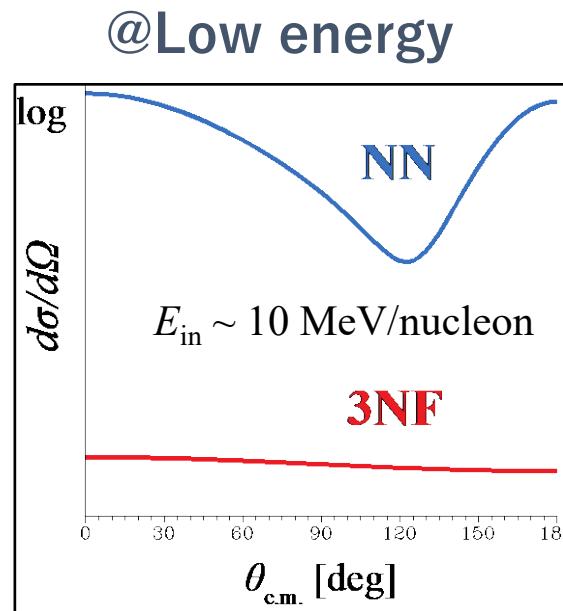
We can extract fundamental information of Nuclear Forces !

# Where can we find 3NFs?

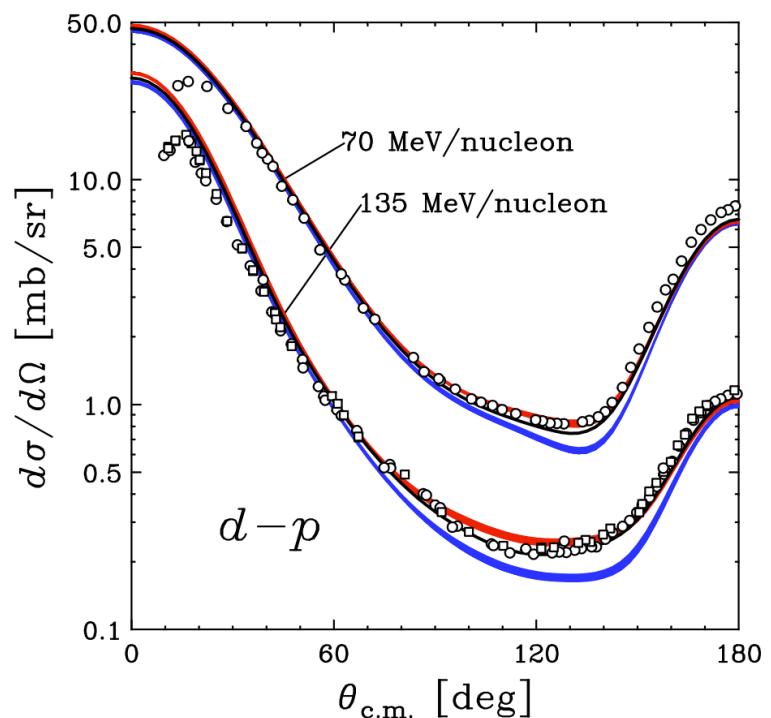
## Nucleon-Deuteron Scattering

H. Witala *et al.*, Phys. Rev. Lett. **81**, 1183 (1998).

- H. Witala *et al.* predicted that 3NF effects are seen in the cross section minimum at around **100 MeV/nucleon**.

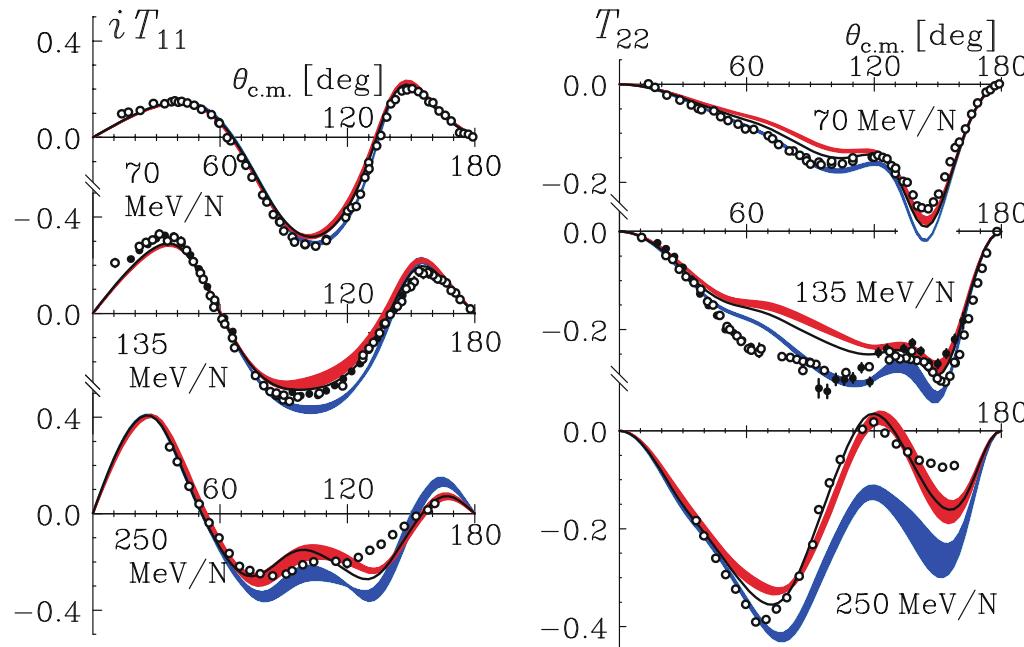


# 3NF Study via $d+p$ Elastic Scattering at 70–300 MeV/u



K. Sekiguchi *et al.*, PRC **65**, 034003 (2002).

- 2NF (AV18, CDB, Nijm I,II)
- 2NF + 3NF (TM'99)
- Urbana IX + AV18

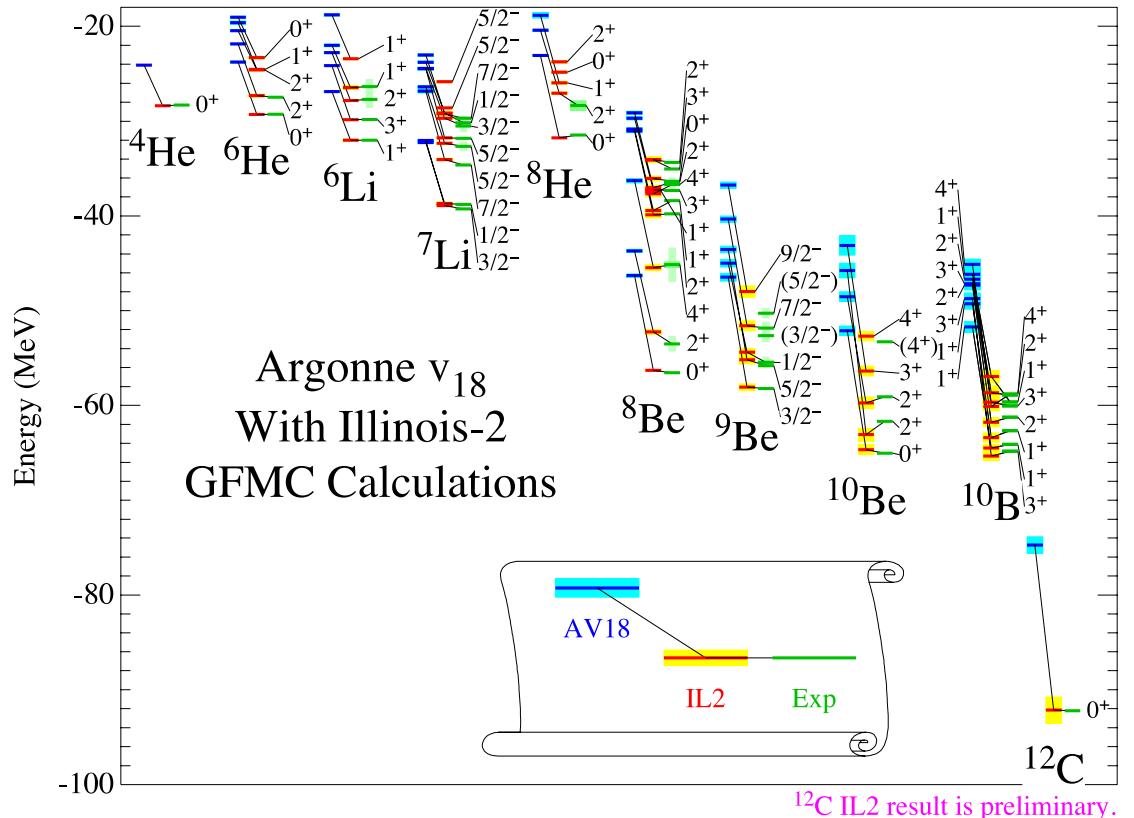


- Differential Cross Section  $d\sigma/d\Omega$ 
  - 3NFs are clearly needed.
- Spin Observables ( $iT_{11}, T_{20}, T_{21}, T_{22}, K_{ij}^{l'}$ )
  - The data are partially reproduced by including 3NFs.

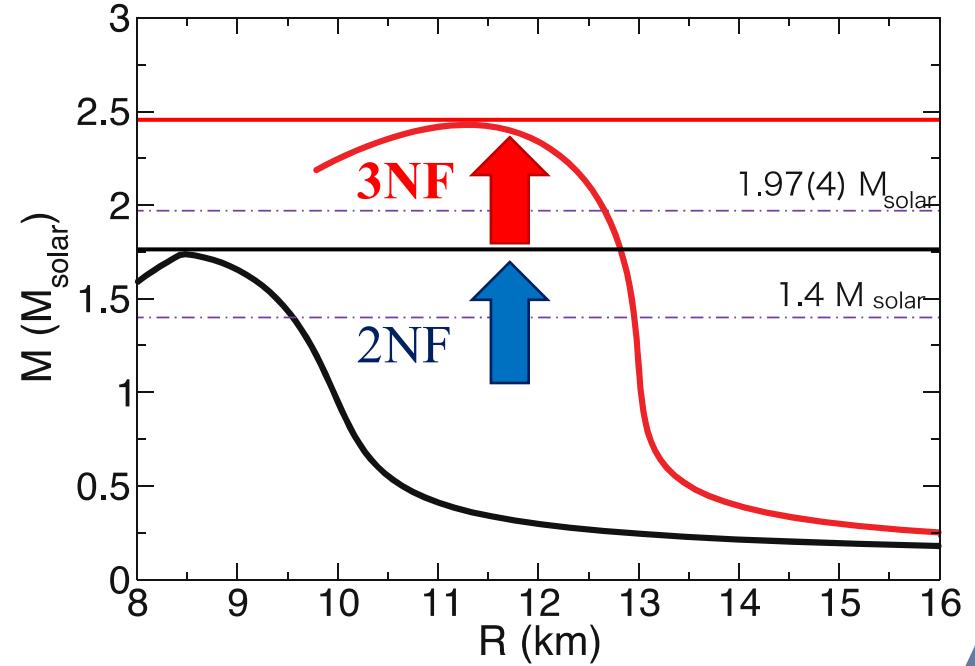
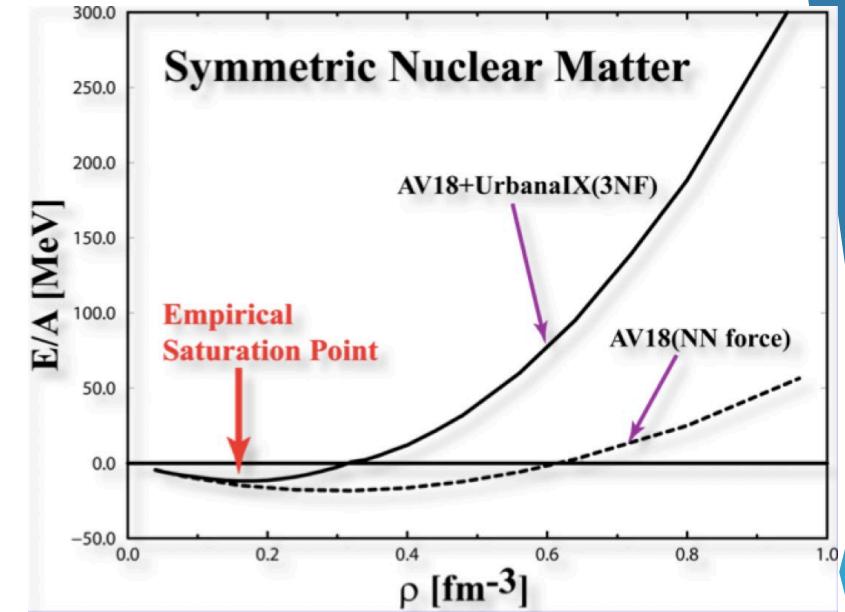
→ Solid basis to explore the 3NF properties

# $T = 3/2$ channel of 3NFs

- Important roles for Neutron-rich nuclei, Neutron matter, etc. ...
- Total isospin channel of 3NFs is limited to  $T = 1/2$  for  $d + p$ .



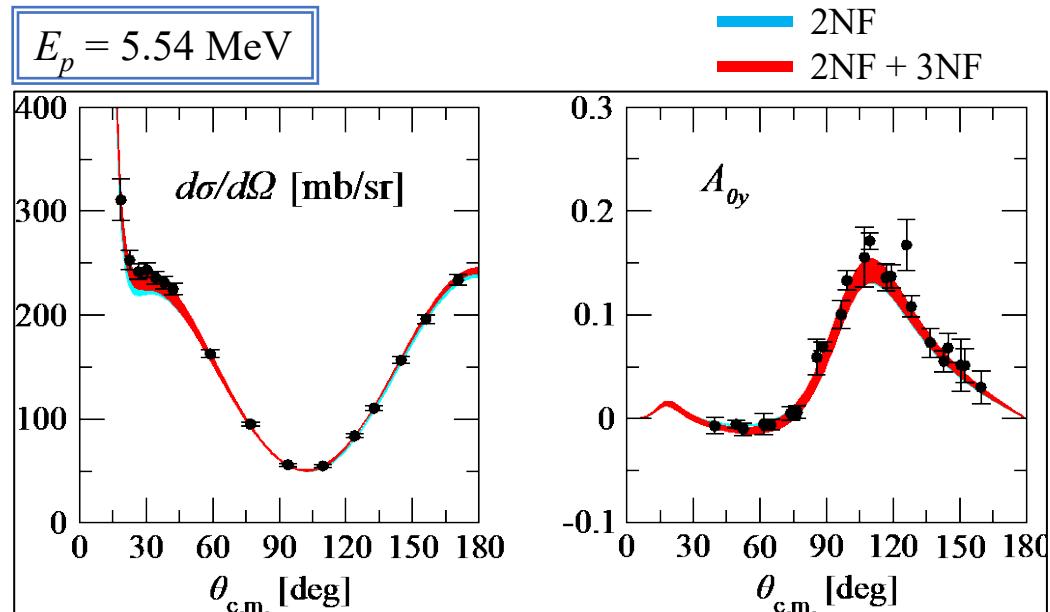
S. C. Pieper *et al.*, NPA 751, 516 (2005).



# 3NF Study via $p$ - $^3\text{He}$ Scattering

## Measurement of $p+^3\text{He}$ system ( $E_p \geq 65$ MeV)

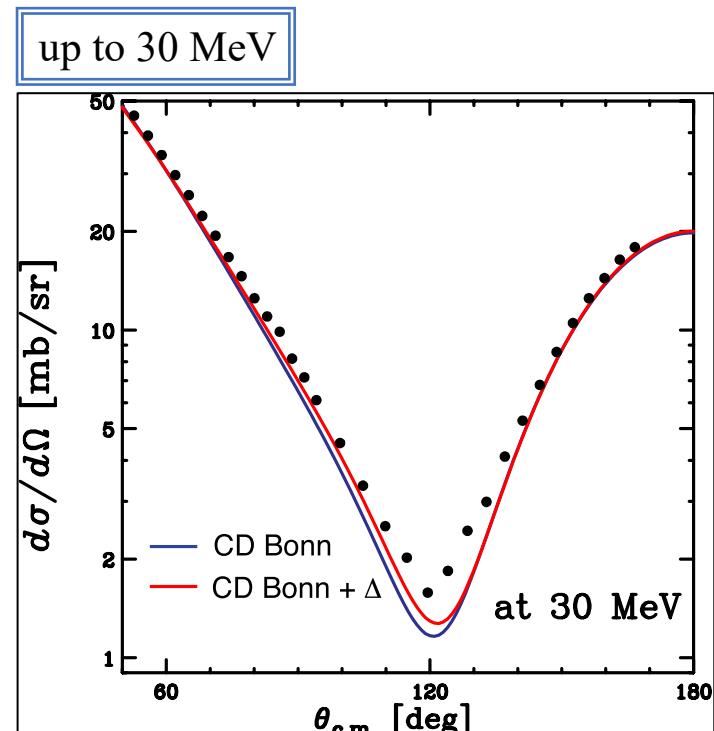
- First Step from few to many nucleon systems
- Approach to iso-spin dependence of 3NFs ( $T = 3/2$  3NFs)
- Theory in progress...



M. Viviani *et al.*, PRL 111, 172302 (2013).

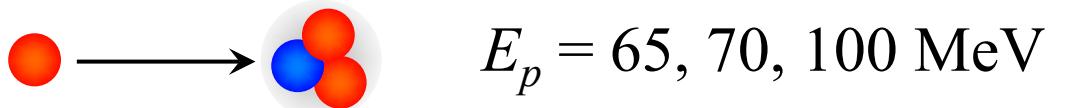
## Observables

Cross section,  
Analyzing powers,  
Spin correlation coefficients.



A. Deltuva and A. C. Fonseca, PRC 87, 054002 (2013).

# Measurements of proton- ${}^3\text{He}$ Scattering



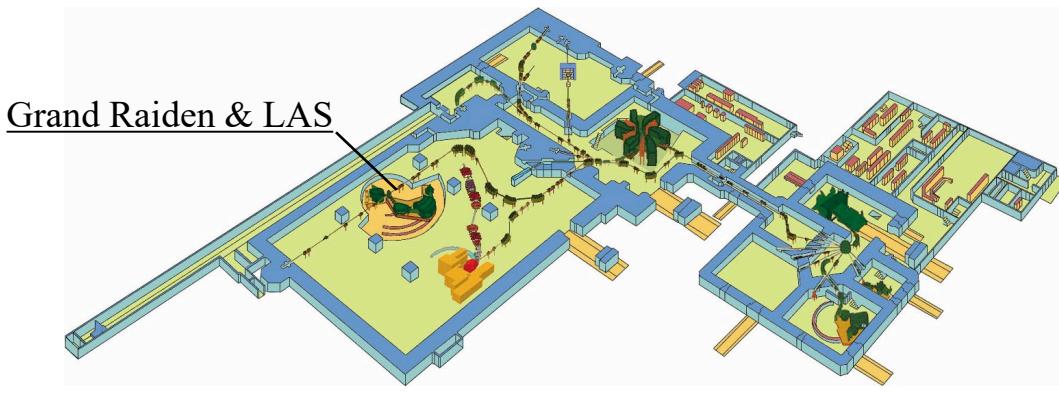
Reported in “AW *et al.*, Phys. Rev. C **103**, 044001 (2021)” for 65, 70 MeV.  
Paper of the measurement at 100 MeV has been accepted to PRC.

# Summary of Measurement for $p+^3\text{He}$

Incident Energy	70 MeV	65 MeV	65 MeV	100 MeV
Beam	$p$	pol. $p$	pol. $p$	pol. $p$
Observables	$A_y(^3\text{He})$	$d\sigma/dQ, A_y(p)$	$A_y(p), A_y(^3\text{He}), C_{y,y}$	$A_y(p), A_y(^3\text{He}), C_{y,y}$
Measured Angles ( $\theta_{\text{c.m.}}$ )	$46^\circ - 141^\circ$	$27^\circ - 170^\circ$	$46^\circ - 133^\circ$	$47^\circ - 149^\circ$
Facility	<b>CYRIC,</b> Tohoku Univ.	<b>RCNP,</b> Osaka Univ.	<b>RCNP,</b> Osaka Univ.	<b>RCNP,</b> Osaka Univ.
Exp. Course	41 course	WS course	ENN course	ENN course

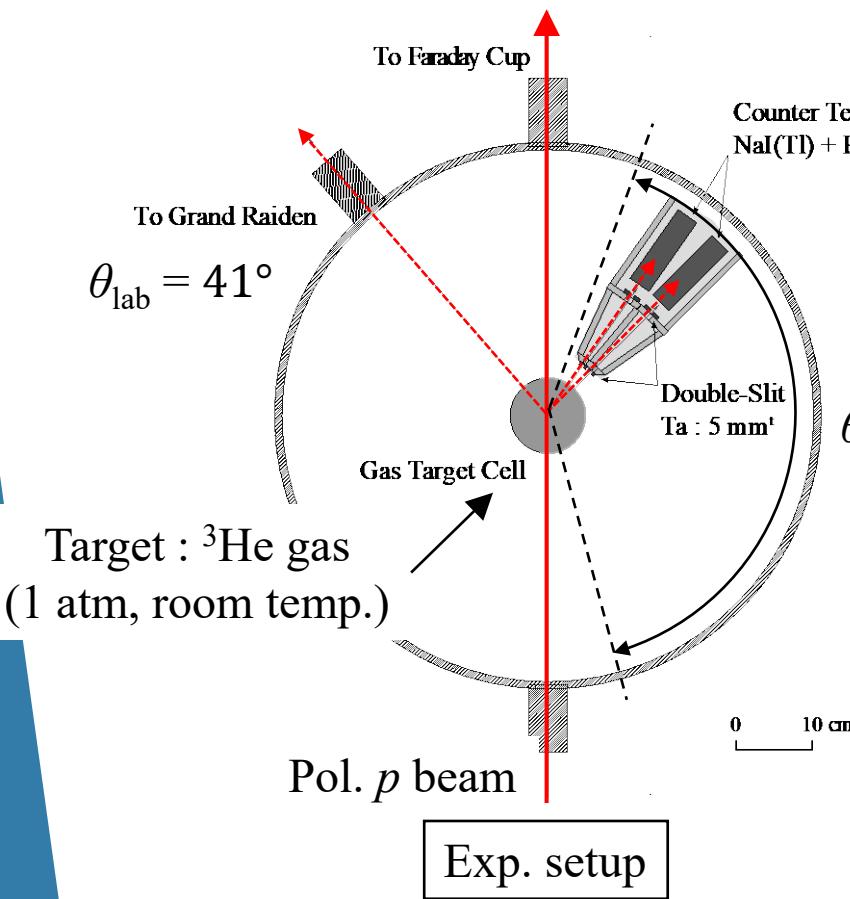


**CYRIC** (AVF cyclotron)



**RCNP**

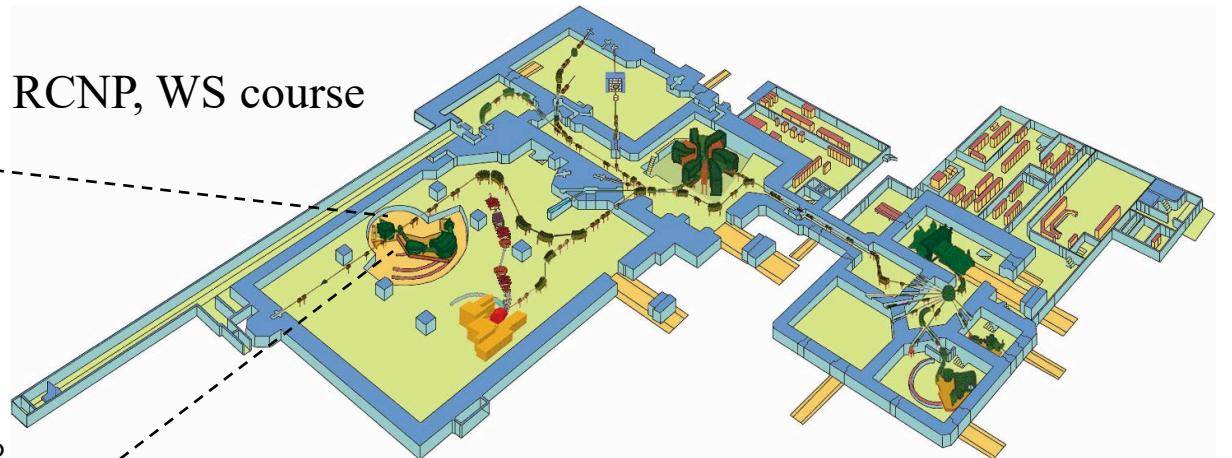
# Measurement of Differential Cross Section



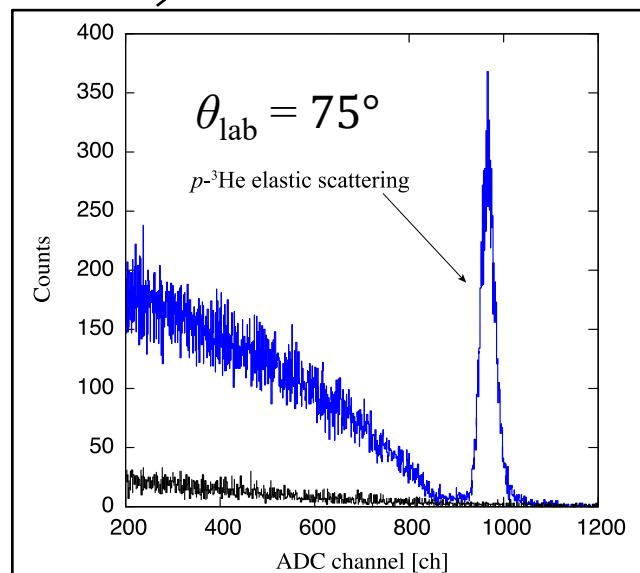
Target :  ${}^3\text{He}$  gas  
(1 atm, room temp.)

Pol.  $p$  beam

Exp. setup

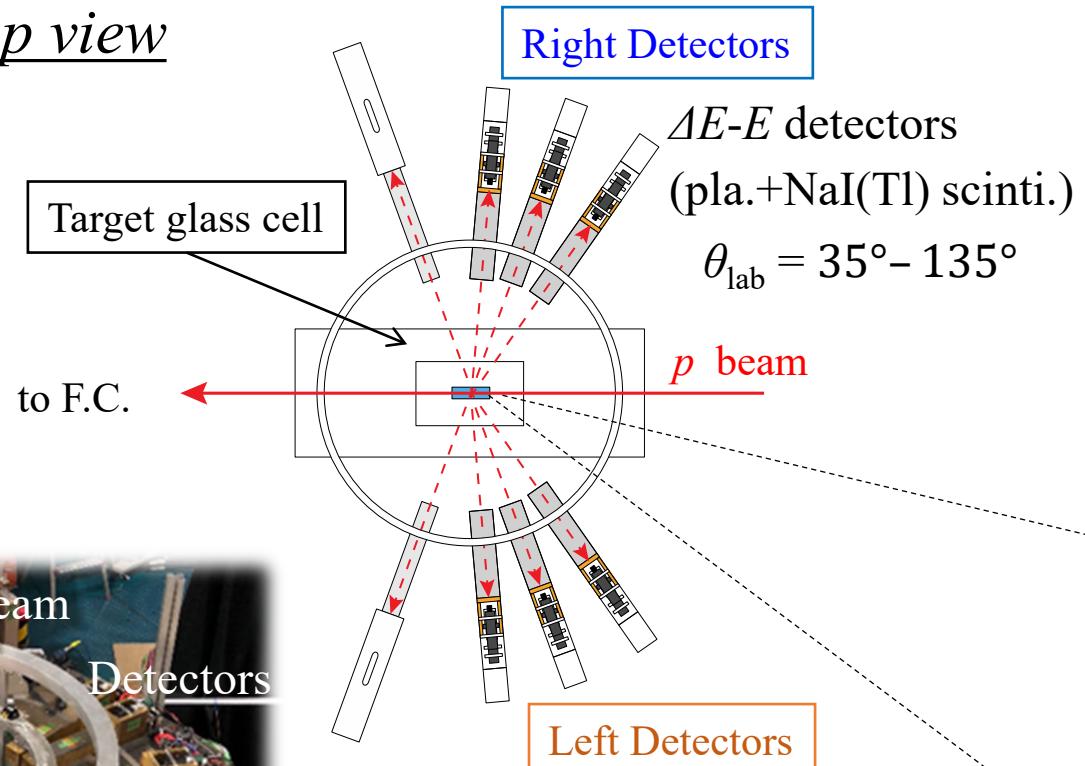
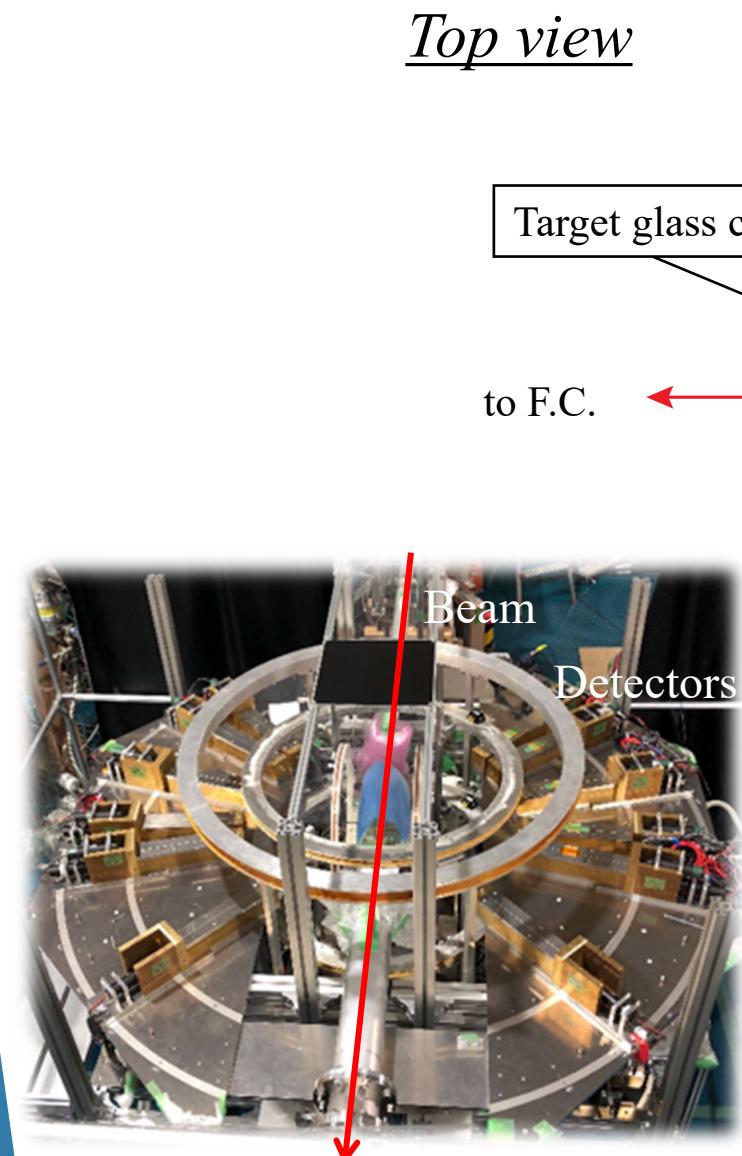


$\theta_{\text{lab}} = 20^\circ - 165^\circ$



Grand Raiden & LAS

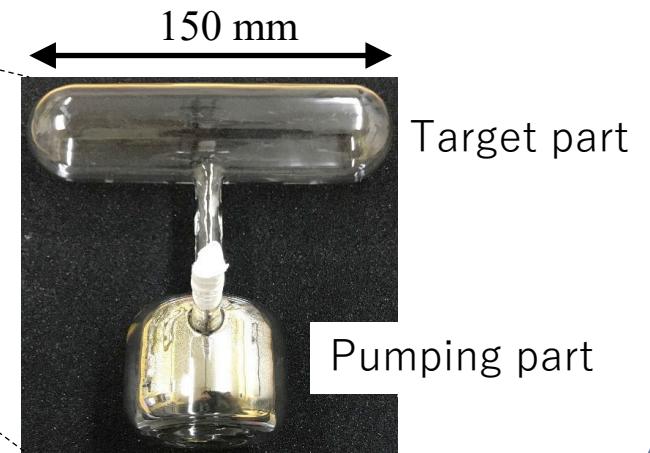
# Experimental Setup with Pol. ${}^3\text{He}$ Target @CYRIC, RCNP



- ${}^3\text{He}$  gas : 3 atm,  $\sim 2 \text{ mg/cm}^2$
- $\text{N}_2$  gas :  $\sim 0.1 \text{ atm}$
- A small amount of Rb, K

Pol.  ${}^3\text{He}$  Target

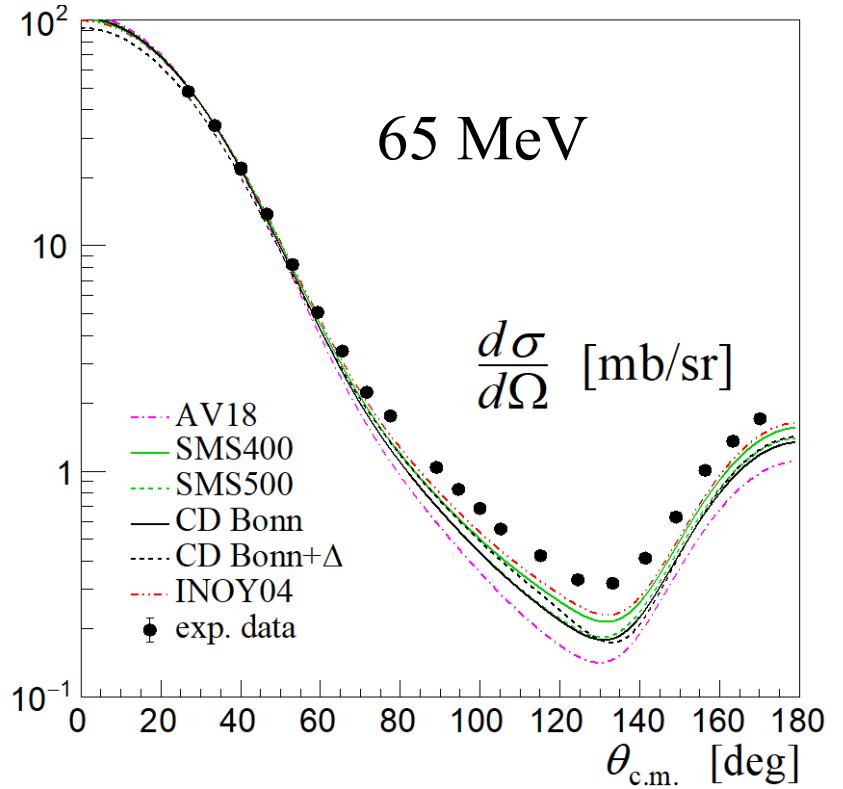
Method: AH-SEOP  
Target cell: GE180 glass  
Typical pol.:  $\sim 40\%$



**Target glass cell**

# Experimental Results for $p+{}^3\text{He}$

\*Calculations : A. Deltuva, private communications



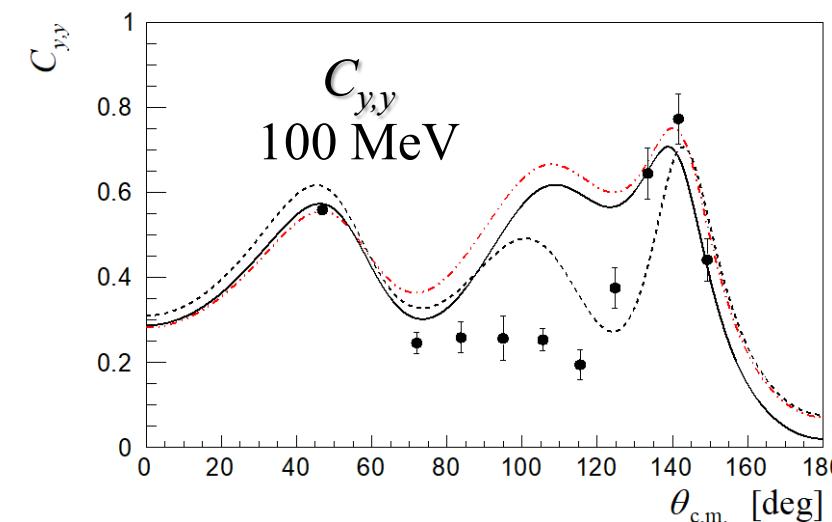
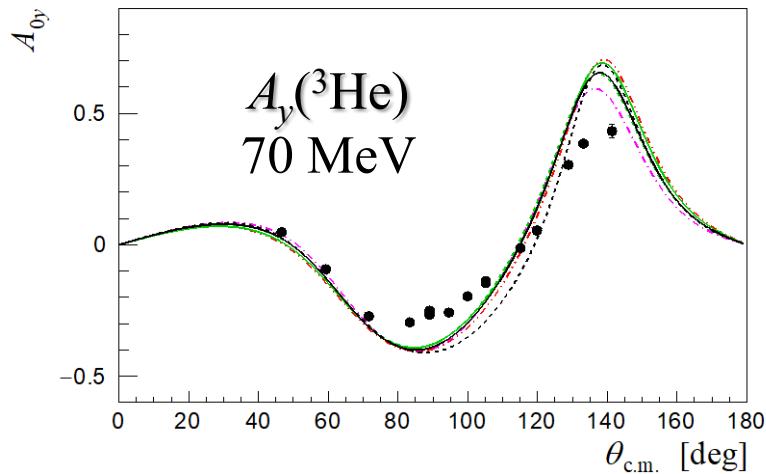
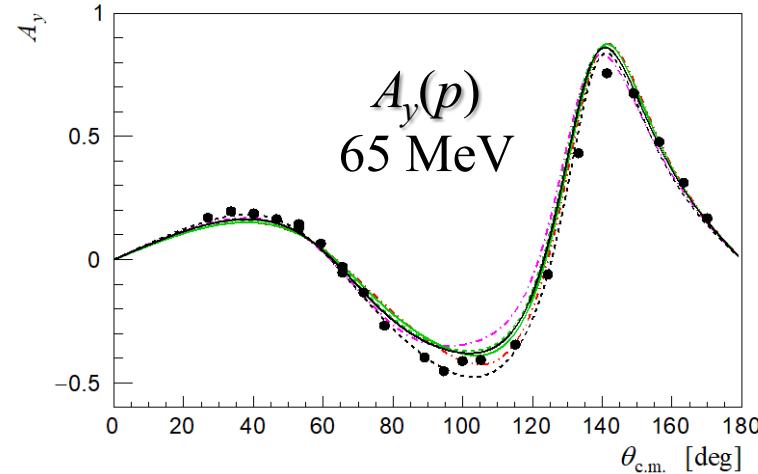
AV18, CD-Bonn : Realistic NN potential

INOY04 : reproducing  ${}^3\text{H}$ ,  ${}^3\text{He}$  B.E. w/o 3NFs

SMS : Chiral EFT (2NF, N<sup>4</sup>LO+)

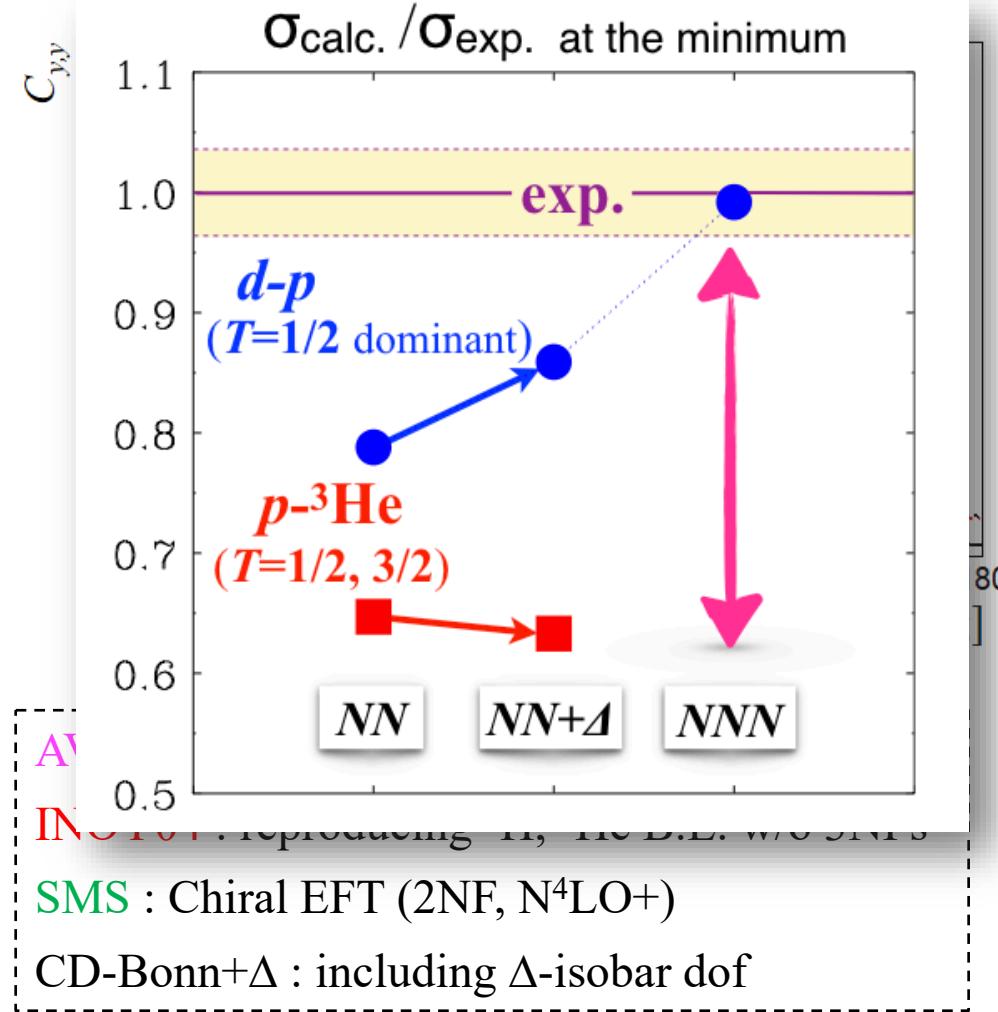
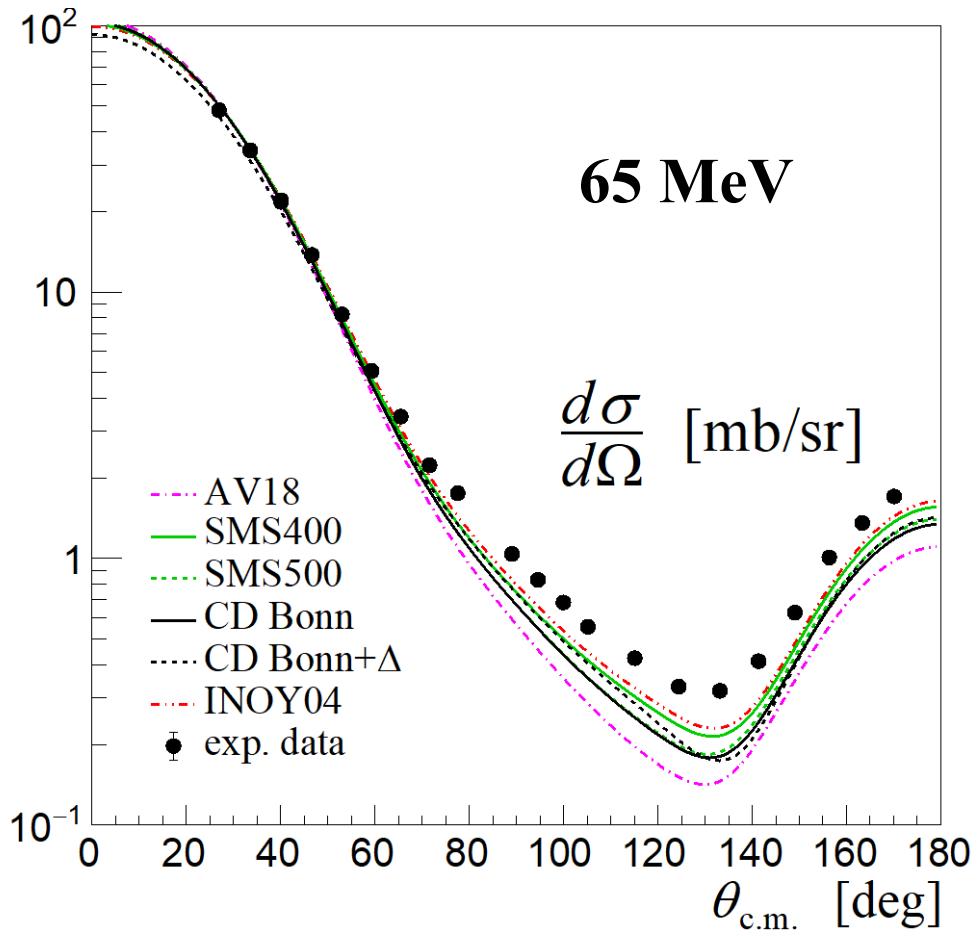
CD-Bonn+Δ : including Δ-isobar dof

\*Coulomb force is omitted.



# Experimental Results for $p+{}^3\text{He}$

\*Calculations : A. Deltuva, private communications



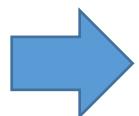
\*Coulomb force is omitted.

# Conclusions

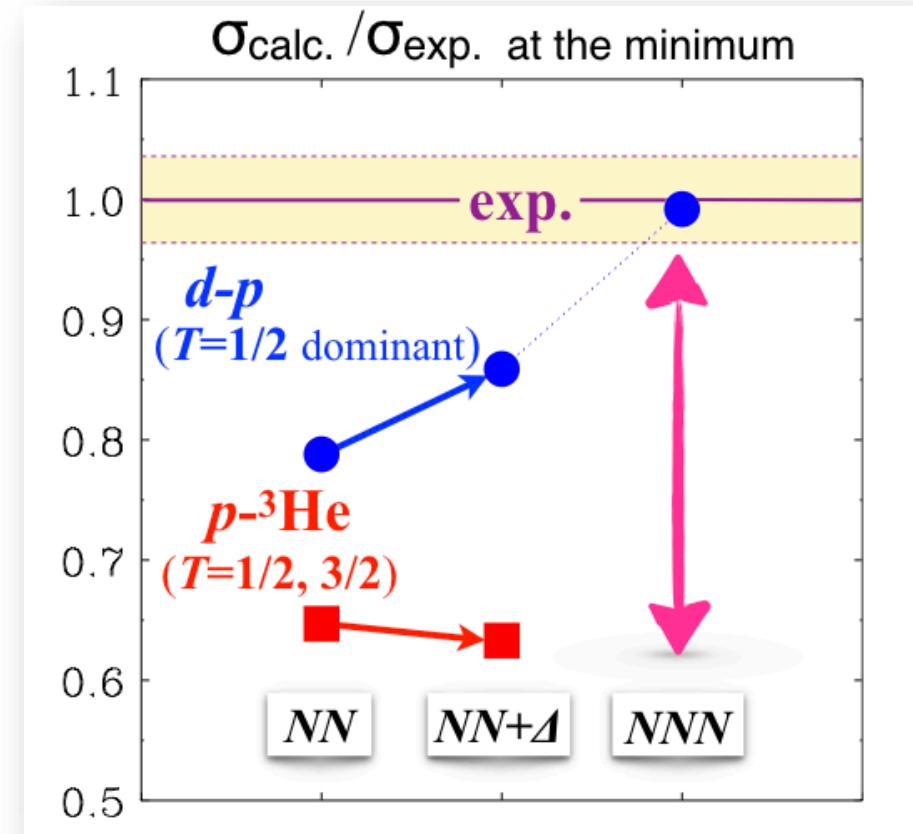
*From comparison between the data and calculations...*

- Clear discrepancies are found at  $d\sigma/d\Omega$  minimum.  
→ larger than *d-p* scattering
- $\Delta$ -isobar effects do **NOT** always remedy that situation.
- Spin correlation coefficient  $C_{y,y}$  shows sizable effects of  $\Delta$ -isobar.

***p-<sup>3</sup>He elastic scattering at intermediate energies***



*An excellent tool to explore the 3NFs which could not be accessible in 3N scattering.*



Further study in view of analysis of scattering amplitude is in progress...

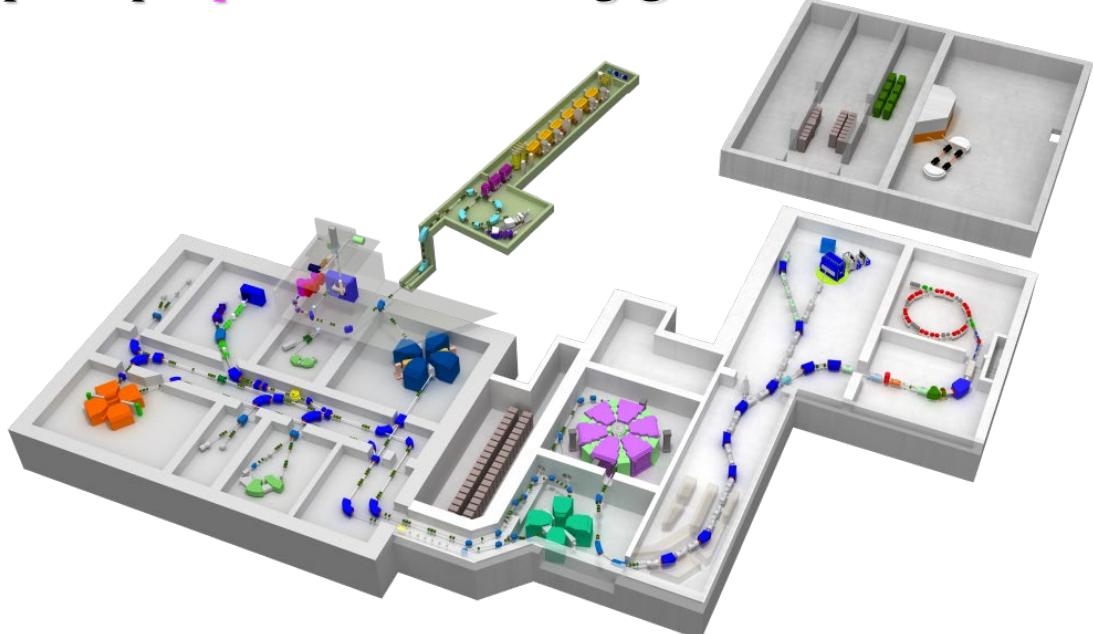
# Future Plan for 3NF Study

## Determination of $\chi$ EFT 3NFs from $d$ - $p$ elastic scattering

Experiment:

Measurement of spin correlation coefficients  
for  $d+p$

pol.  $d$ -pol.  $p$  Elastic Scattering @RIBF



Theory:

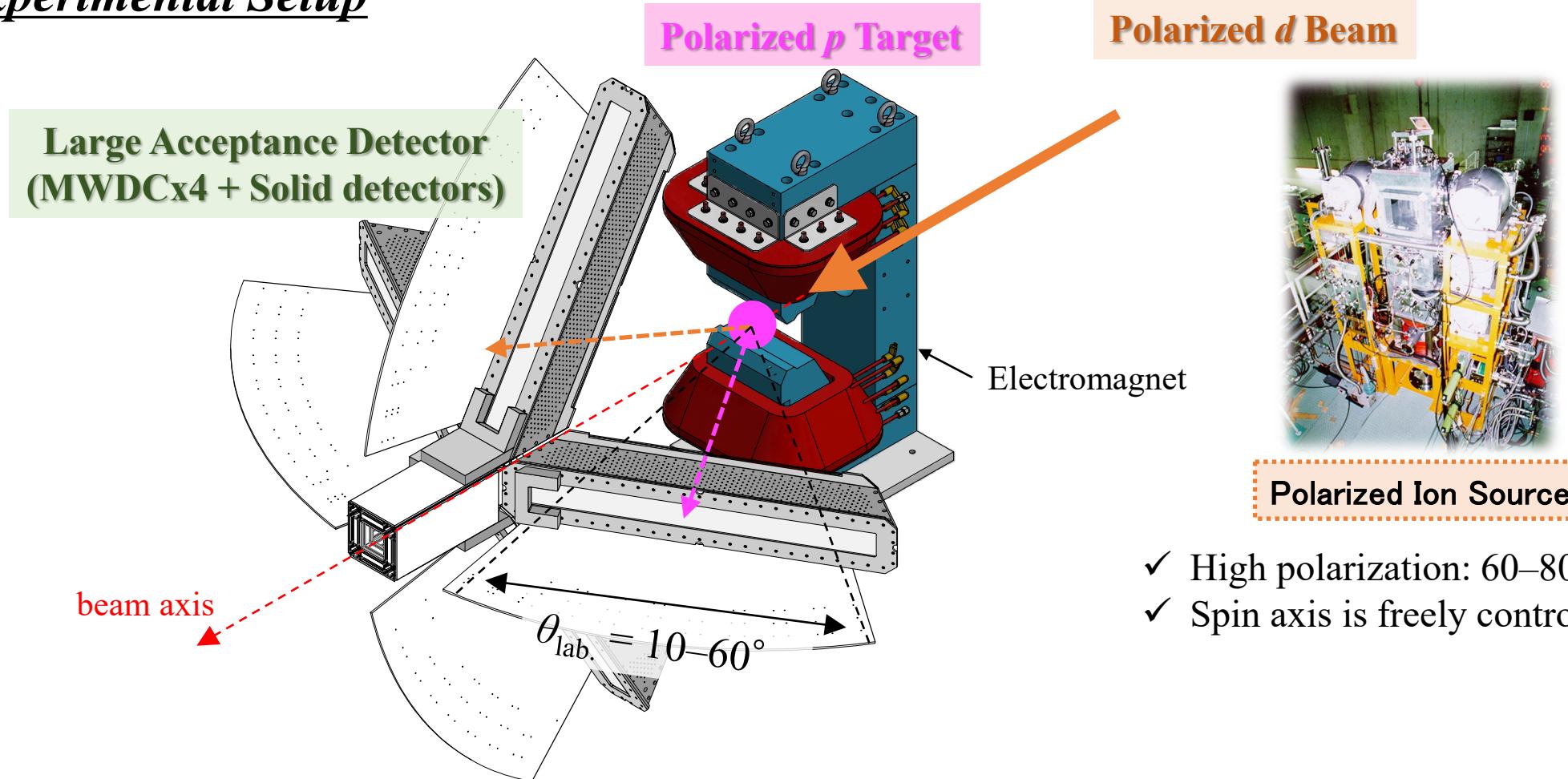
Chiral Effective Field Theory (EFT)

	2N Force	3N Force
LO $(Q/A_\chi)^0$		
NLO $(Q/A_\chi)^2$		
$N^2LO$ $(Q/A_\chi)^3$		
$N^3LO$ $(Q/A_\chi)^4$		
$N^4LO$ $(Q/A_\chi)^5$		

$C_D$   $C_E$   
13 LECs

# Measurement of Spin Correlation Coefficients for $d+p$

## Experimental Setup



*Beam test will be performed at HIMAC next month.* 17

### Polarized $d$ Beam



### Polarized Ion Source

- ✓ High polarization: 60–80%
- ✓ Spin axis is freely controlled.

# Summary

Study of 3NFs for  $p\text{-}{}^3\text{He}$  elastic scattering at intermediate energies ( $E/A \geq 65$  MeV)

- ❖ First step from few-nucleons to many body
- ❖ Approach to total iso-spin  $T = 3/2$  channel of 3NFs

Measurement of  $p\text{-}{}^3\text{He}$  elastic scattering for 65, 70 and 100 MeV @CYRIC, RCNP

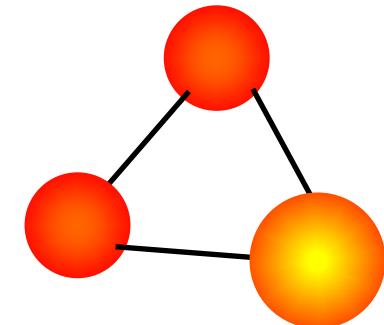
- ❖ Precise data of  $d\sigma/dQ$ ,  $A_y(p)$ ,  $A_{0y}({}^3\text{He})$ ,  $C_{y,y}$
- ❖ Comparison the data with the predictions based on NN potential
  - ✓ Calculation (with  $\Delta$ -dof.) **do NOT reproduce the data**
  - ✓ **Different properties from  $d\text{-}p$  scattering system**
  - ✓  $C_{y,y}$  shows sizable  $\Delta$ -isobar effects

Excellent tool for  
3NF study

## Future Plan

$d\text{-}p$  scattering : Complete set of spin correlation coefficients

→ **Determination of 3NFs based on  $\chi$ EFT from  $d\text{-}p$  scattering data**



# Collaborators

➤ ***Tokyo Institute of Technology***

A. Watanabe, K. Sekiguchi

➤ ***Tohoku University***

S. Nakai, Y. Wada, T. Akieda, D. Etoh, M. Inoue, Y. Inoue, K. Kawahara, H. Kon, K. Miki, T. Mukai, D. Sakai, S. Shibuya, Y. Shiokawa, T. Taguchi, H. Umetsu, Y. Utsuki, M. Watanabe

➤ ***CYRIC, Tohoku University***

M. Itoh

➤ ***National Institute of Radiological Science***

T. Wakui

➤ ***RCNP, Osaka University***

K. Hatanaka, H. Kanda, H. J. Ong, D. T. Tran

➤ ***University of Miyazaki***

Y. Maeda, K. Nonaka

➤ ***RAP, RIKEN***

Y. Ikeda, Y. Otake, A. Takeda, Y. Wakabayashi

➤ ***KEK***

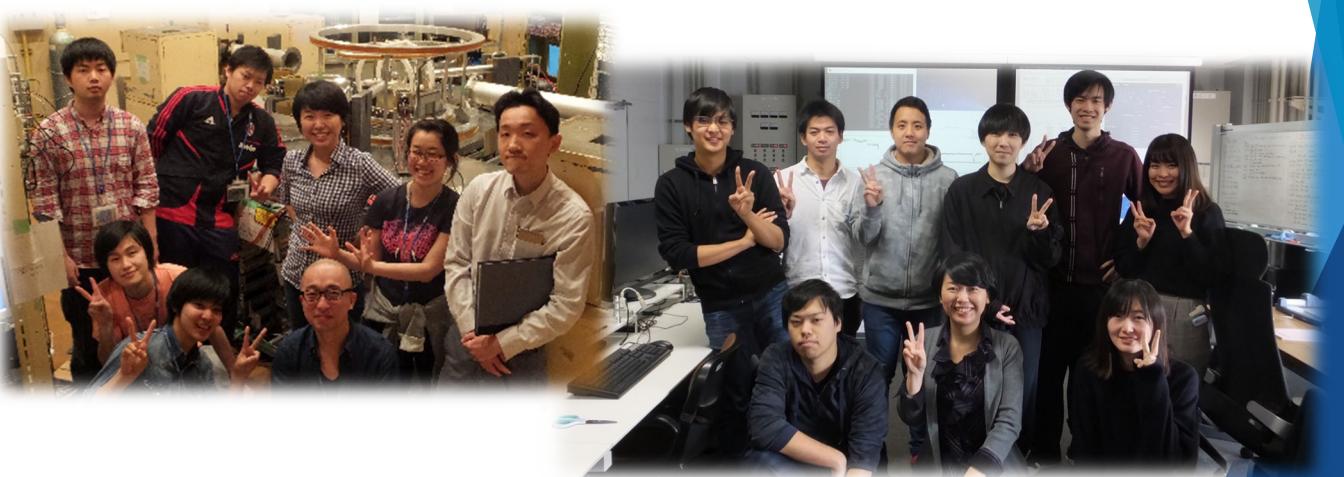
T. Ino

➤ ***Kyushu University***

S. Goto, Y. Hirai, D. Inomoto, H. Kasahara, S. Mitsumoto, H. Oshiro, T. Wakasa

➤ ***RIKEN Nishina Center***

H. Sakai, T. Uesaka



*Thank you for your attention.*